Effect of Branching on Mutual Solubility of Alkane–CO$_2$ Systems by Molecular Simulations

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**ABSTRACT:** Mutual solubilities of hydrocarbon–CO$_2$ systems are important in a broad range of applications. Experimental data and theoretical understanding of phase behavior of large hydrocarbon molecules and CO$_2$ are limited. This is especially true in relation to the molecular structure of hydrocarbons when the carbon number exceeds 12. In this work, the continuous fractional component Gibbs ensemble Monte Carlo simulations are used to investigate mutual solubility of different alkane and CO$_2$ systems and the molecular structure. We investigate the mutual solubility of $n$-decane, $n$-hexadecane, $n$-eicosane, and the corresponding structural isomers in the CO$_2$-rich and hydrocarbon-rich phase. The focus will be solubility of the heavy normal alkanes and their structural isomers in CO$_2$. The simulation results are verified by comparing the experimental data when measurements are available. The simulation of phase behavior of the $n$-decane–CO$_2$ system agrees with the experiments. We also present simulation results of $n$-hexadecane–CO$_2$ and $n$-eicosane–CO$_2$ systems away from the critical region partly due to the finite size effect. We establish that solubility of the hydrocarbons in CO$_2$ is improved by change of the molecular structure in heavier alkanes. The enhanced solubility is limited in decane isomers, but the isomers of hexadecane and eicosane show 2- to 3-time solubility enhancement. The molecular dynamics simulations suggest that the improvement is from a higher coordination number of CO$_2$ for methyl (CH$_3$) rather than for methylene (CH$_2$) groups. This study sets the stage for molecular engineering and synthesis of hydrocarbons that are soluble in CO$_2$ not only by considering functionality but also by changing the molecular structure. The solubility enhancement is the first step in vicosification of CO$_2$ which broadens the use of CO$_2$.

**INTRODUCTION**

Mitigation of CO$_2$ emission and removal of CO$_2$ from the atmosphere have attracted much attention because of global warming and possible disruptive effects on life on Earth. Enormous efforts are being made in capturing, storing, and utilizing CO$_2$ by the scientific community and industry. Geological storage is widely believed to significantly reduce CO$_2$ emissions over other technologies (e.g., CO$_2$ as a feedstock). In the geological storage, CO$_2$ can be stored in depleted oil and gas formations or in deep saline aquifers. Injection of CO$_2$ is also deployed in enhanced oil recovery (CO$_2$-EOR) because of higher efficiency compared to natural gas and other fluids. The efficiency of CO$_2$ injection in the subsurface can be drastically improved by enhancing the sweep efficiency. CO$_2$ does not provide an efficient displacement in the subsurface because of gas-like viscosity even at high density in the supercritical state. The result is low efficiency in CO$_2$-EOR and the geological storage. Increase in CO$_2$ viscosity would lead to success in the geological storage and CO$_2$-EOR.

Thickeners are added to CO$_2$ for vicosification. This results in improvement in the mobility ratio. The degree of vicosification and solubility in CO$_2$ are major factors to be considered in development of direct thickeners. Low adsorption to the rock is a major requirement. For decades, much effort has been made to search for polymers to vicosify CO$_2$. The published thickeners may not meet the three requirements (solubility, degree of vicosification, and low adsorption) simultaneously. Low solubility especially limits applications of polymers for direct thickening. Al Hinai et al. have investigated the solubility of 26 polymers including poly(vinyl acetate), poly(vinyl alcohol), and poly(1-decene). They show that only four polymers (poly(1-decene) with six repeat units, poly(vinyl ethyl ether), poly(iso-butyl vinyl ether), and poly(dimethylsiloxane)) are soluble in CO$_2$ at a temperature of 377 K and at a pressure of 55 MPa. In their study, poly(1-decene) has the highest solubility of 5 wt% at ~48 MPa and ~358 K. Out of the four polymers, the poly(1-decene) and poly(vinyl ethyl ether) vicosify carbon dioxide by about 1.2–2.8-fold and 1.2–2.1-fold, respectively, at very high pressures (>50 MPa). The required concentrations to achieve the increase in viscosity stated above are 5 and 2 wt% for poly(1-decene) and poly(vinyl ethyl ether), respectively. The solubility of polymers is low in CO$_2$ for all but a few. Fluorinated polymers rather than the hydrocarbon framework

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are an option for direct thickening because of the CO2philicity. Fluorinated polymers may viscosify CO2 to the desirable level. However, the fluorinated polymers are expensive and have a high environmental impact. They also become more effective at concentrations above 2 to 3 wt %. Non-fluorinated polymers such as poly(1-decene) and poly(vinyl ethyl ether) have received more attention in recent years partly due to current economic and environmental requirements. Very recently, Kar and Firoozabadi suggested that increase in CO2 solubility of poly(1-decene) can be achieved by a higher number of methyl groups. It is pointed out that squalane (C30H62) with eight methyl groups is around 8 times more soluble in supercritical CO2 than n-dotriacontane (C32H66). The understanding of solubility mechanisms of hydrocarbons including polymers in CO2 is the first important step to finding a direct thickener.

The molecular structure in hydrocarbon–CO2 systems which is based on interactions between neighboring atoms is the key to improving the solubility of functional molecules in CO2. Experimental and simulation studies have been conducted to draw a unified picture of the relationship between hydrocarbon solubility in CO2 and the molecular structure. Girard et al. have reviewed experimental data and presented the heuristics on the solubility of polymers in CO2: weak polymer–polymer interaction,7,8 strong polymer–CO2 interaction,9–10 and enhanced entropy of mixing. Silva and Orr have investigated partitioning of organic molecules between the oleic and CO2 phases and shown that branched alkanes have higher solubility in the CO2-rich phase than normal alkanes with the same molecular weight. Their data show that the effect becomes more pronounced in alkanes larger than n-dodecane. The molecular structure can affect the molecular interactions and the entropy of mixing. The understanding of the relationship between hydrocarbon solubility in CO2 and the molecular structure is limited. In heavy hydrocarbons and polymers, solubility measurement in CO2 is a challenge. Phase behavior of CO2 with n-alkanes such as n-decane,12–28 n-hexadecane,12,17,26,29–34 and n-ecicosane17,29,33–37 has been investigated over decades. However, there are limited experimental data as the molecular weight of alkanes increases. There are few reports of experiments for the structural isomers especially for dodecane and larger ones. To the best of our knowledge, experimental data for phase behavior of structural isomers of alkanes with a carbon number larger than 10 are limited to isomers of decane24 and triacontane.34,38–40 A complete list of references for experimental data of phase behavior between alkanes and CO2 is presented in the Supporting Information. There is limited discussion in the literature on improvement in CO2 solubility from change of the molecular structure.8,41 Molecular dynamics simulations suggest that interaction between fluorinated groups and CO2 is stronger than that of poly 1-decane and poly vinyl ethyl ether.41 This is in line with the experimental observation that fluorinated molecules have higher solubility in CO2 than others. Solubility mechanisms in CO2 from the molecular structure point of view have been rarely investigated. The focus has been on the effect of different chemical species on solubility in CO2.

Molecular simulations provide molecular-scale insights in addition to properties of interest with an appropriate interaction parameter (forcefield). The simulations can be conducted under high-temperature and high-pressure conditions.42 Equilibrium molecular dynamics,43–46 thermodynamic integration,49–52 Gibbs–Duhem integration,53–57 and Gibbs ensemble Monte Carlo (GEMC)58–62 can be used to investigate solubility and/or solubilization behavior by molecular simulations. We select GEMC in our investigation of solubility of hydrocarbons in CO2. GEMC implicitly reproduces a two-phase equilibrium state and provides composition of both phases without creating an interfacial system. The method can be parallelized; it is efficient.

The conventional molecular simulations may not be viable for phase behavior simulations of large molecules such as polymers and CO2. The solubility calculation is limited to small hydrocarbons like n-decane,61,63 coarse-graining models63 and simple systems without consideration of a specific molecule.64 Surprisingly, there have been very few attempts using molecular simulations in phase-split calculations of a mixture of a large molecule and a small solvent molecule such as CO2. It must be emphasized that only a few studies discuss the branching effect on solubility.64 There have been very limited measurements of solubility of heavily branched alkanes in CO2.

In this work, GEMC simulations are conducted to investigate the relationship between hydrocarbon solubility in CO2 and the molecular structure. The effect of branching on the solubility in CO2 is the focus of our investigation. Our study has two parts: (1) the GEMC results are examined by comparison with experimental data and (2) the effect of branching on solubility in CO2. We perform continuous fractional component (CFC) GEMC simulations for hydrocarbons including n-decane, n-hexadecane, and n-ecicosane and their structural isomers and CO2 systems. The CFC-GEMC is the method of choice for large molecules because of partial insertion. The technique has not been used in phase-split computations for heavy hydrocarbons and CO2 systems in the past to the best of our knowledge.

## Simulation Details

The CFC method allows insertion of fractional molecules in GEMC to improve the efficiency of particle transfers. The fractional molecules have a fractional parameter (λ) between 0.0 and 1.0. The interactions of the fractional molecules with other molecules are controlled by the fractional parameter. There is no interaction between the fractional molecules and other molecules when λ = 0 and full interaction when λ = 1.0. The reduction of the interactions results in efficient transfer of molecules (i.e., insertion and deletion) in GEMC simulations. In addition to the conventional MC moves (e.g., translation, rotation), CFC-GEMC implements the lambda move, swap move of fractional molecules, and identity the exchange move. The moves attempt to change the fractional parameter, to move a fractional molecule to the other box, and to swap a fractional molecule and a full molecule, respectively. The swap move is conducted when λ is small (<0.3), and the identity exchange move is conducted when λ is large (>0.7). The λ-controlled choice can improve efficiency of sampling because the swap move and the identity exchange move are likely accepted when λ is smaller and larger, respectively. By using fractional molecules, chemical potentials of each component become equal efficiently (i.e., equilibrium state) in different phases.

There is a concern that accuracy of simulation results is affected by the introduction of fractional molecules. It is generally accepted that impurities may improve efficiency of GEMC simulations without an appreciable effect on simulation

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results. The introduction of fractional molecules does not affect simulation results. Not limited to the CFC method, impurity is sometimes introduced even in the conventional GEMC simulations to enhance molecular swap move from one box to the other box. Our simulations include a maximum of a 0.02 mole fraction of fractional molecules as impurities.

In our simulations, we use 50 to 150 organic molecules and 1000 to 1500 CO$_2$ molecules. The number of the molecules in the systems depends on pressure. The largest system size (150 organics and 1500 CO$_2$) is selected when the system is in the near-critical region; GEMC generally suffers from system size dependency.

The value of 0.95 is suggested by Vishnyakov et al. The introduction of fractional molecules does not affect simulation results.

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Figure 1. Molecular structure of the structural isomers of n-decane, n-hexadecane, and n-eicosane. (a) 2-Methylnonane, (b) 2,2,4,6,6,8,8-heptamethylnonane, and (c) 2,2,4,4,6,6,8,10,10-nonmethylundecane.

binary mixtures of n-decane, n-hexadecane, n-eicosane, and iso-decane with CO$_2$ are conducted at temperatures at which experimental data are available for verification. Then, we predict phase behavior of the structural isomers to investigate the branch effect. The data are provided in the Supporting Information (Tables S4—S13).

RESULTS AND DISCUSSION

In Figure 2, we display the pressure—composition isotherms of nC$_{10}$—CO$_2$; experimental data are from Reamer and Sage. The past, GEMC simulations have been performed to investigate the phase behavior with the TraPPE-UA and TraPPE-small force field. The authors present the phase diagrams at a temperature of 310 K and at a pressure of 7 MPa; there is only qualitative agreement with experimental data. In this work, we demonstrate that CFC-GEMC reproduces phase behavior for the n-decane—CO$_2$ system even at a higher pressure (14 MPa) and higher temperature (377.6 K) than those in ref 61. There is good agreement in the whole range. Zhang and Siepmann report overestimation of CO$_2$ solubility in alkanes by the TraPPE-UA forcefield which most likely is due to shortcoming of the united-atom model. By modifying the LB mixing rule, the simulation results show excellent agreement with the experimental data (Figure 2). A full Carlo simulations of single-component phases in the NPT ensemble for 2 × 10$^5$ MC cycles (one MC cycle consists of the same number of trial moves as the number of molecules in a system). After the equilibration of the pure phases, more than 9 × 10$^5$ MC cycles are performed to allow the systems to reach equilibrium with molecular exchanges between the two phases. More than 5 × 10$^5$ MC cycles are required to reach the equilibrium state especially when the system is in the near-critical region. The equilibrium production runs consist of 1 × 10$^6$ MC cycles. Energy, volume, density, and composition of the systems are monitored to ensure no drift during a production run. The advantage of CFCMC over the conventional MC simulations is that it provides chemical potentials by the introduction of fractional molecules. The chemical potentials of each component in each phase are also monitored. The values are presented for all the systems in the Supporting Information (Tables S4—S13).

We perform simulations of n-decane, n-hexadecane, n-eicosane, and their structural isomers which are iso-decane (2-methylnonane), 2,2,4,6,6,8,8-heptamethylnonane, and 2,2,4,4,6,6,8,10,10-nonmethylundecane with CO$_2$. Molecular structures of the isomers are shown in Figure 1. Simulations of

![Figure 1](https://example.com/figure1.png)
The atomistic model (TraPPE-EH) may not require modifications of the mixing rule to reproduce experimental data in CO$_2$–alkane systems. However, we recommend the use of the united atom with the mixing rule modification. The united atom reduces computational cost in simulations of phase behavior of mixtures of heavier alkanes and CO$_2$.

We also perform simulations of phase behavior of the structural isomer of the $n$-decane and CO$_2$ system. To the best of our knowledge, no studies by GEMC have been conducted for branched alkane and CO$_2$ systems. Recently, experimental data have been published for the $iso$-decane and CO$_2$ system. Figure 3 shows the comparison of the phase behavior of $iso$-decane (2-methylnonane) and CO$_2$. Our simulations reproduce the experimental data.

Pressure–composition isotherms of heavy alkanes (i.e., $n$-hexadecane and $n$-eicosane) are shown in Figures 4 and 5. The simulation results agree with the experiments. Due to limited system size, the simulations are carried out at pressures below that of the near-critical region. In contrast to those of $n$-decane and $iso$-decane systems, the simulations become unstable at higher pressures even in the very large system size (150 alkane and 1500 CO$_2$ molecules).

We like to point out that experimental data are sometimes inconsistent in the heavier alkanes because of high critical pressure of the binary system (over 15 MPa), and solubility of heavier alkanes in CO$_2$ is extremely low. Figure 4 shows experimental data for the pressure–composition diagram in $n$-hexadecane–CO$_2$ systems measured at 333.2 and 343.2 K. The data are from two different groups. We like to point out that the measurements in ref 31 are significantly different from measurements in refs 12 and 32. There are challenges in high-pressure phase behavior measurements of heavy alkane–CO$_2$.

It is widely known both experimentally and theoretically that molecules become less soluble in CO$_2$ with increasing molecular weight. Flory–Huggins theory suggests that solubility will decrease with the increasing polymerization degree. However, solubility in CO$_2$ depends not only on molecular weight but also on the molecular structure which is not accounted for in Flory–Huggins theory. Pressure–composition isotherms for the isomers of $n$-hexadecane and $n$-eicosane are provided in the Supporting Information (Figures S1 and S2). The solubility of CO$_2$ in the hydrocarbon-rich phase is not appreciably affected by the molecular structure, while solubility of hydrocarbons in the
CO₂-rich phase is significantly affected as we will discuss in the following.

The solubility of normal alkanes and branched alkanes in CO₂ is presented in Figure 6. This a key plot in our work which reveals the difference in solubility of normal alkanes and branched alkanes. The plot demonstrates that branching improves the solubility in CO₂. The simulation results suggest that branching enhances solubility in CO₂ as molecular weight of an alkane increases. Decane (C₁₀) systems have no significant solubility improvement from branching (filled and open circles in Figure 6). In contrast, hexadecane and eicosane (C₁₆ and C₂₀) systems clearly show solubility improvement by branching (filled and open squares for C₁₆ and filled and open triangles for C₂₀). The improvements are more than 3 times. Quantitatively, 0.33 wt% of n-hexadecane (at T = 344.3 K) can dissolve in CO₂ at 12 MPa, while 2,2,4,6,8,8-heptamethylno-nane has a solubility of 1.6 wt% at the same pressure. The solubility of eicosane improves from 0.95 to 3.7 wt% at 14.8 MPa (T = 344.3 K) by the molecular structure change from linear to branching with the same molecular weight. Our results are consistent with branched alkane measurements in a crude oil which shows higher solubility in a CO₂-rich phase when molecular weight of alkanes is higher than that of dodecane.⁷ The data by Silva and Orr show that there is no significant difference between partitioning of iso-alkanes and normal alkanes of lower molecular weight (less than that of dodecane), whereas there is about 2- to 3-time difference in partitioning of C₁₆ and C₃₀. One may reason that 2-methylnonane (structural isomer of n-decane) because of one branch has CO₂ solubility close to that of n-decane (Figure 1). To examine the effect of further branching in decane, we simulate a highly branched structural isomer of n-decane (2,3,4,5-tetramethylhexane). Figure S3 in the Supporting Information shows that the solubility of a highly branched decane in CO₂ does not improve from the increase in branched structures.

The largest alkane in our CFC-GEMC simulations is eicosane in the investigation into the effect of branching on CO₂ solubility. The effect of branching on CO₂ solubility increases with increase in molecular weight. Only a few studies discuss the branching effect on CO₂ solubility.⁸⁹

We have also performed molecular dynamics simulations to compare solvation structures in normal alkanes and branched alkanes. GROMACS ver 2021.8⁹⁰ is used for molecular dynamics simulations (simulation detail is presented in the Supporting Information). The force field used in our molecular dynamics simulations is the same as that used in the CFC-GEMC simulations. The LINCS⁹¹ algorithm is used to fix bond length during the simulations. Each system consists of 1 organic molecule and 5000 CO₂ molecules. Figure 7 shows the radial distribution function and coordination number of carbon atoms in CO₂ around CH₃ and CH₂ groups at two different pressures. We observe that the CH₃ group has a higher number of CO₂ atoms in the first solvation shell than the CH₂ group. The implication is that branched alkanes have higher solubility in CO₂ because of a higher number of CH₃ groups than normal alkanes. A higher coordination number indicates preferable interaction with CO₂. The difference in the coordination number becomes significant at higher pressure. This is in line with the results that solubility improvement becomes more significant at higher pressure (Figure 6). The radial distribution function and coordination number of the other normal and branched alkanes also show the same trend as that shown by the plots in Figure 6. The solvation structures for the eicosane systems are presented in Figures S4 and S5 in the Supporting Information. We like to point out that the all-atom force field (CGenFF)⁹² gives similar results to those of the united atom for the hexadecane systems shown in Figure 7. It seems that there is not much discussion in the literature on the effect of the molecular structure on solubility of hydrocarbons in CO₂.

**CONCLUSIONS**

CO₂–hydrocarbon interactions are investigated by an efficient molecular simulation approach through the CFC-GEMC method with a focus on solubility of alkanes and the branching
effect. The interactions are of importance for application of geological storage of CO$_2$ and CO$_2$-EOR through direct thickening. Surprisingly, our current knowledge of solubility of heavy hydrocarbons in CO$_2$ in relation to the molecular structure is limited. We have conducted CFC-GEMC simulations to reproduce the phase behavior of CO$_2$ with n-decane, n-hexadecane, n-eicosane, and their structural isomers. It is demonstrated that the phase behavior of the n-decane–CO$_2$ system from the simulations agrees with the experiments. Molecular simulations of n-hexadecane–CO$_2$ and n-eicosane–CO$_2$ systems also show agreement with the experiments away from the critical region. Increasing the system size may allow accurate calculations at higher pressures in the critical region.

One of the main objectives of the work has been extension of the calculations to structural isomers of n-decane, n-hexadecane, and n-eicosane to investigate molecular structure dependency of solubility in CO$_2$. We demonstrate that for heavier alkanes, the solubility is enhanced significantly by the molecular structure. The improvement is not pronounced in the n-decane isomer. The isomers of n-hexadecane and n-eicosane show 2- to 3-time improvement in solubility in CO$_2$. The molecular dynamics simulations suggest that the improvement is from increase in the coordination number of CO$_2$ for CH$_3$ rather than CH$_2$. This study proposes that the solubility improvement from branching can become significant in alkanes of higher molecular weight (e.g., polymer scale). Molecular engineering to improve the solubility in CO$_2$ can be achieved not only by considering functionality but also by changing the molecular structure.

**ASSOCIATED CONTENT**

*Supporting Information*

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.jpcb.2c05774.

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**Figure 7.** Solvation structure of n-hexadecane and its structural isomer (2,2,4,6,6,8,8-heptamethylnonane) in CO$_2$ at $P = 5.52$ and $10.34$ MPa and $T = 344.3$ K.
Reference list of experiments conducted for hydrocarbon–CO$_2$ systems; force field parameters used in this study; detailed simulation data; pressure–composition isotherms for isomers; solvation structure of C$_{20}$ systems; and simulation details of molecular dynamics (PDF)

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**Notes**
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