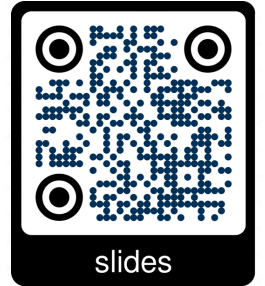


Empowering the Future: How the Distance Math Program Offers Undergraduate Courses to Advanced High School Students in Georgia

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Georgia Institute of Technology
SIMIODE Expo 2024

While we are waiting to start: use the chat to introduce yourself and where you are connecting from, experiences teaching distance and/or for high school.



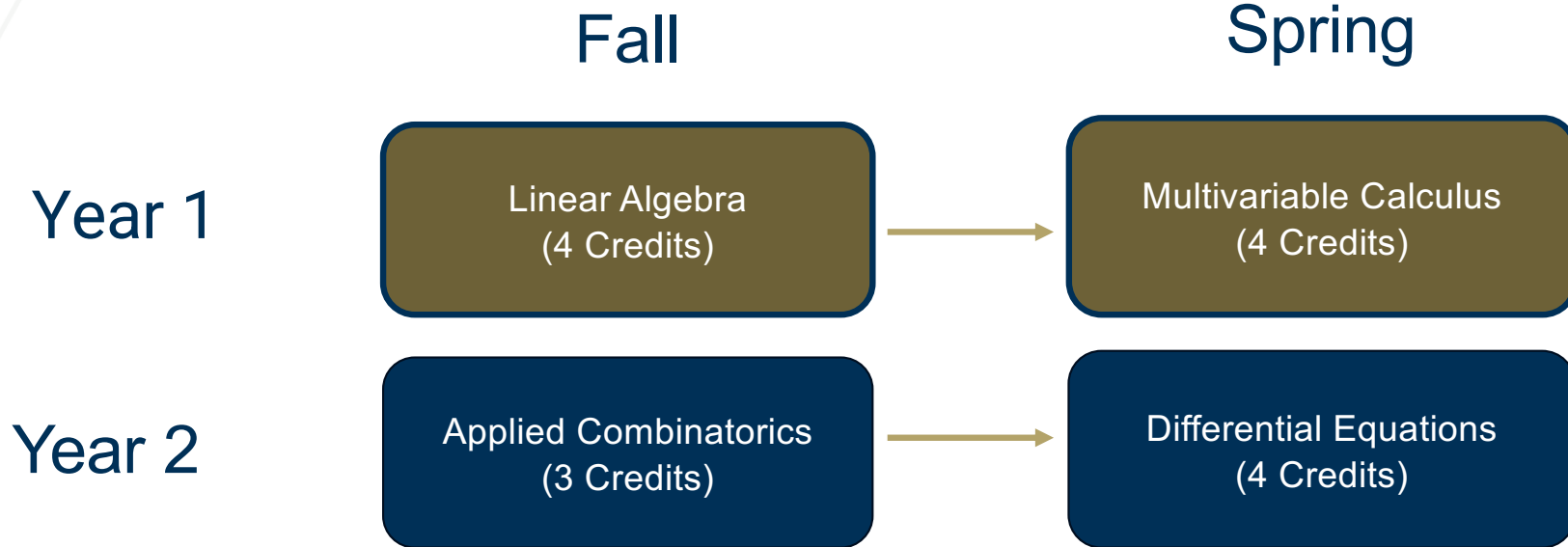
The Distance Math Program

- A distance learning program offered at Georgia Tech
- Offers undergraduate mathematics courses to Georgia high school students.
- Relies on state funding through **dual enrollment***.
 - Dual enrollment allows students to be enrolled in college(s) and high school.
 - Students receive high school and college credit simultaneously.



* More info [on GaDOE website here.](#)

Courses



Partnerships

- School of Math
 - Course curriculum and instruction
 - Assigns teaching assistants, instructors
 - Director of online learning supports teaching assistants and instructors
- Georgia Tech Professional Education
 - Course design
 - Technology support for students, assistants, instructors
 - Exam administration
- Georgia Tech Admissions
 - Application and enrollment processes

Application Requirements

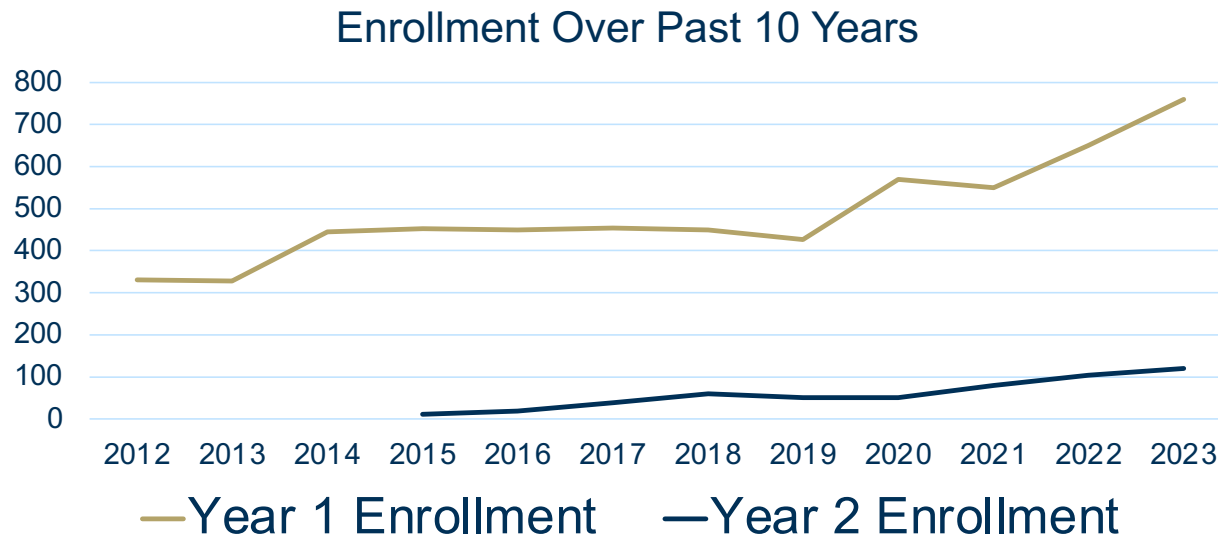
- To apply for distance math, students must
 - Be a Georgia resident (out-of-state students not eligible).
 - Have completed AP Calculus BC with **score of 4 or 5**.
 - Submit high school transcript
 - Submit SAT, ACT, or PSAT scores
- More information about application process [on GT Admissions website](#).

Impact

- Roughly half of the distance math students go on to enroll at Georgia Tech.
- Among in-state students admitted to an undergraduate degree program at Georgia Tech, around **1/6 of them completed the Distance Math Program.**

Enrollment Growth

- Program began in 2005 with ~ 30 high school students
- Approximate enrollment now:
 - **Year 1:** 760 students (linear algebra, multivariable calculus)
 - **Year 2:** 120 students (applied combinatorics, differential equations)



Course Delivery Format

- Asynchronous: pre-recorded lectures
- Live studio sessions facilitated by teaching assistants

Georgia Tech

Recall: Spectral Decomposition of a Symmetric Matrix

Spectral Decomposition

Suppose A can be orthogonally diagonalized as

$$A = PDP^T = (\vec{u}_1 \ \cdots \ \vec{u}_n) \begin{pmatrix} \lambda_1 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & \lambda_n \end{pmatrix} \begin{pmatrix} \vec{u}_1^T \\ \vdots \\ \vec{u}_n^T \end{pmatrix}$$

Then A has the decomposition

$$A = \lambda_1 \vec{u}_1 \vec{u}_1^T + \cdots + \lambda_n \vec{u}_n \vec{u}_n^T = \sum_{i=1}^n \lambda_i \vec{u}_i \vec{u}_i^T$$

Can we give a more general result using the SVD?

Lecture Slides Created in LaTeX (beamer)

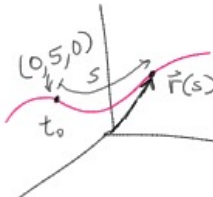
Math 2551 Studio Worksheets *Worksheet for Section 13.3*

2. Find the point on the curve

$$\vec{r}(t) = (5 \sin t)\mathbf{i} + (5 \cos t)\mathbf{j} + 12t\mathbf{k}$$

at a distance 26 units along the curve from the point (0, 5, 0) in the direction of increasing arc-length.

We want $\vec{r}(s)$ instead of $\vec{r}(t)$
 so we can find $\vec{r}(s=26\pi)$



$$s(t) = \int_{t_0 \leftarrow 0}^t \|\vec{r}'(t)\| dt$$

↓

$$\vec{r}(t_0) = (0, 5, 0) = \vec{r}(0)$$

$$\vec{r}(t) = \langle 5 \sin t, 5 \cos t, 12t \rangle = \underline{\underline{\langle 0, 5, 0 \rangle}}$$

$t_0 = 0$

Teaching Assistants Annotate
Worksheets in Live Studio

Exam Procedures

Year 1 MATH 1554 Exam 2 Version B

Work done on scratch paper will not be graded. You do not need to show your work on page 1.

1. (0.5 points) Fill in the blanks with a dark pen or pencil. Using only capital letters print your first name: , last name: , the remaining digits of your GTID:

9	0								
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, the High School you attend: .

2. (9 points) Indicate **true** if the statement is true, otherwise, indicate **false**.

	true	false
a) If E is a 2×2 elementary matrix, then $\det(E) = 1$.	<input type="radio"/>	<input type="radio"/>
b) 1 is always an eigenvalue for any stochastic matrix P .	<input type="radio"/>	<input type="radio"/>
c) The dimension of an eigenspace of a square matrix A is one.	<input type="radio"/>	<input type="radio"/>
d) If matrices A and B have the same eigenvalues, then A and B are similar.	<input type="radio"/>	<input type="radio"/>
e) If A is a diagonalizable $n \times n$ matrix, then A has n distinct eigenvalues.	<input type="radio"/>	<input type="radio"/>
f) If an $n \times n$ matrix has n distinct eigenvalues, then $Ax = b$ has a solution for all b .	<input type="radio"/>	<input type="radio"/>
g) A 2×2 matrix A with characteristic polynomial $\lambda^2 + 1$ has two real eigenvalues.	<input type="radio"/>	<input type="radio"/>
h) If $\det(A) = 3$ and A is a 3×3 matrix, then $\det(-A) = -3$.	<input type="radio"/>	<input type="radio"/>
i) If an eigenvalue of $n \times n$ matrix A is $\lambda = 2$, then $\dim(\text{Null}(A - 2I)) = n - 1$.	<input type="radio"/>	<input type="radio"/>

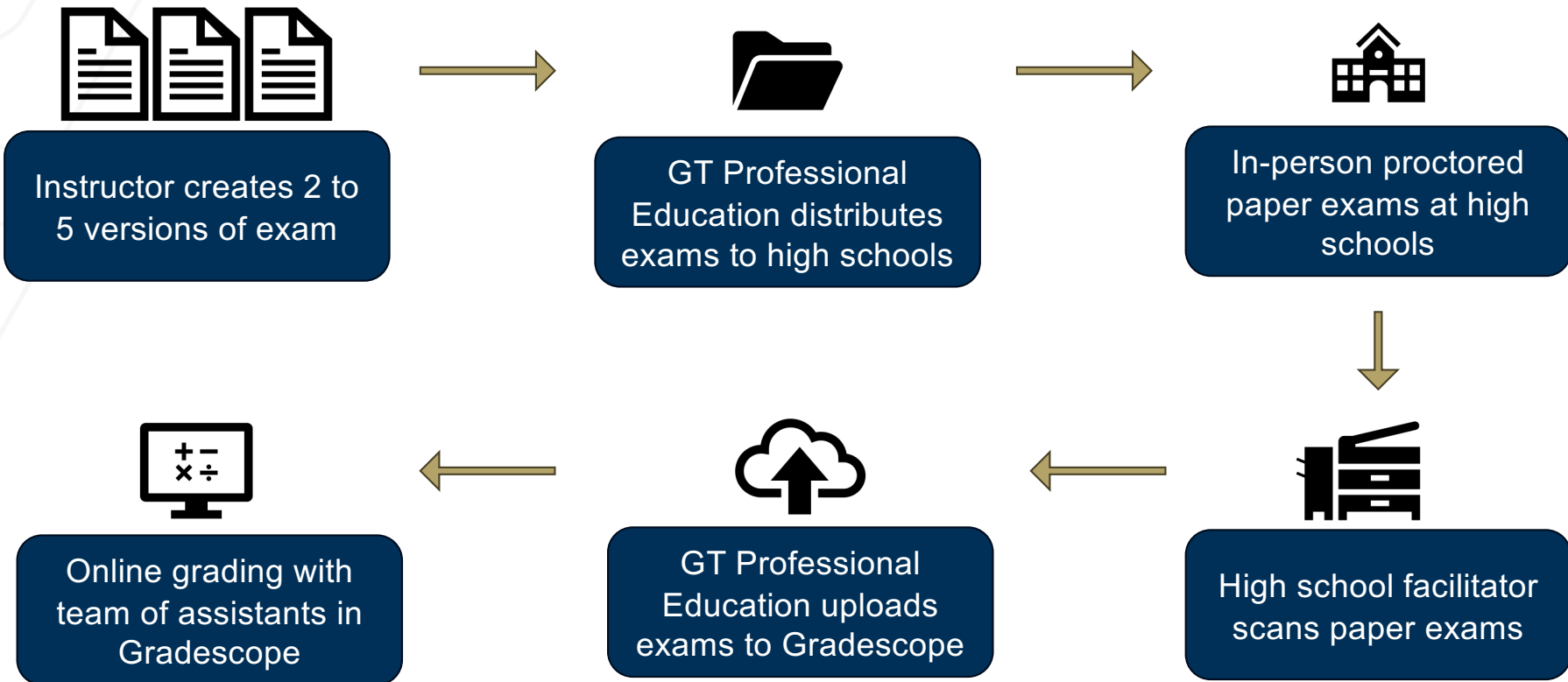
3. (6 points) Fill in the blanks. You do not need to show your work.

(a) If c is a real number, $A = \begin{pmatrix} 5 & 4 \\ c & c \end{pmatrix}$, $B = \begin{pmatrix} 10 & c \\ 8 & c \end{pmatrix}$, and $\det A = 4$, then $\det B = \boxed{}$.

(b) The determinant of $A = \begin{pmatrix} 1 & 2 & 0 \\ 1 & 2 & 0 \\ 1 & 2 & 1 \end{pmatrix}$ is: .

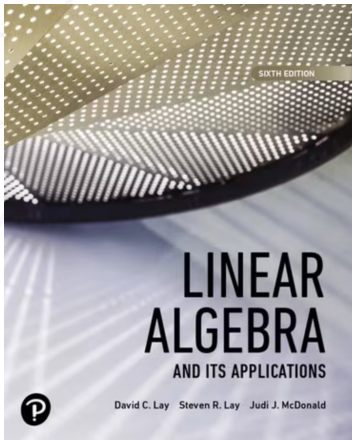
- In-person proctored.
- Each high school has a designated facilitator who is in charge of proctoring.
- Exams graded using Gradescope.

Exam Procedures

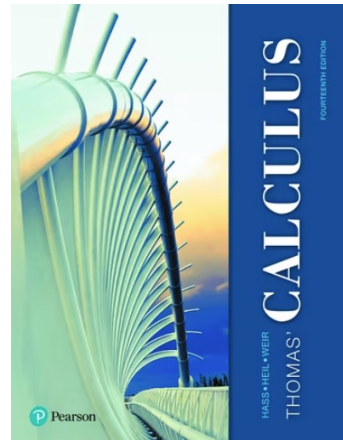


Textbooks

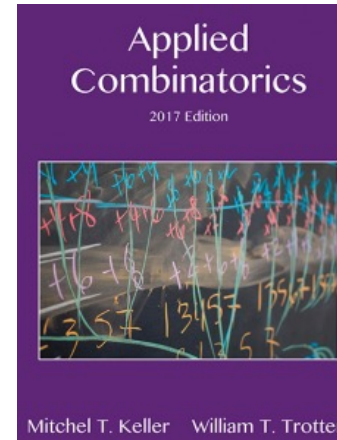
Linear Algebra
Lay 6E



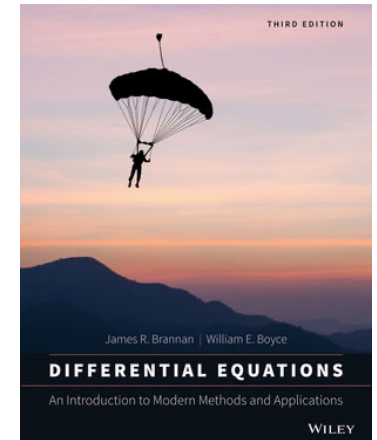
Multivariable Calculus
Thomas 14E



Applied Combinatorics
Keller & Trotter



Differential Equations
Brannan & Boyce 3E



- Using the same textbooks that the on-campus sections use.
- State policy that dual enrolled students not required to pay for textbooks.
- GT Bookstore emails e-textbook codes to students.
- Working on moving to OER ...

Assistant Team

	Head TA	TAs	Lecture Assistants	Graders	Curriculum Developers
Grade	✓	✓	✓	✓	
Office Hours	✓	✓	✓		
Forum Moderation	✓	✓	✓		
Live online studios	✓	✓			
Course Admin	✓				
Develop Curriculum	✓	✓			✓

	Head TA	TAs	Lecture Assistants	Graders	Curriculum Developers
Year 1	1	1	4	4	7
Year 2	0	1	0	1	0

Current Challenges → Future Directions

Publisher homework systems
alignment to course

Textbook costs and code
distribution

Time needed to create
multiple exam versions

student assistants



WebWork

OER

AI

Impact on Other Initiatives

- Distance Math curriculum supported other undergraduate courses and generated momentum for other projects.
- For example:
 - Lecture slides, worksheets, lecture recordings shared with other mathematics faculty.
 - Four-part [linear algebra series on EdX](#).
 - [Open Course Project](#) (a DEI initiative).

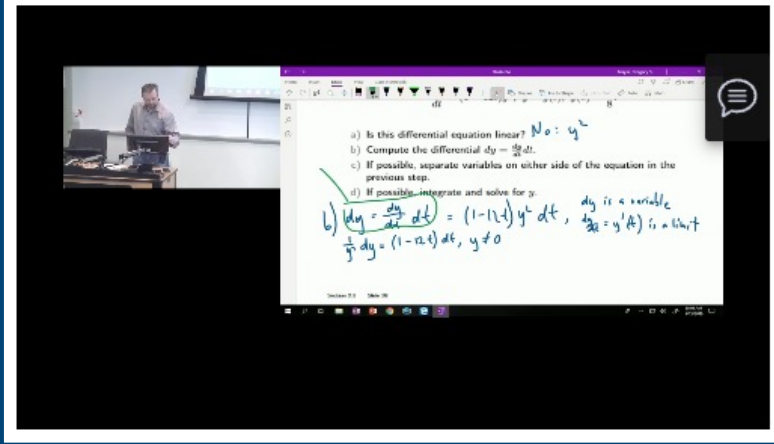
Online Differential Equations

- Spring semesters
- Pre-recorded lectures
- Covers same topics as on-campus sections
 1. First order equations
 2. Linear systems
 3. Second order equations
 4. Numerical methods
 5. Nonlinear equations
 6. Laplace Transform methods

Recorded Video Embedded in Canvas

2.1.1 Separable Equations

This video gives a quick overview of what separable equations are, a procedure for solving them, and an example. Note that it can be difficult to solve explicitly for y as a function of the independent variable. Often it will be better to leave the solution in implicit form.

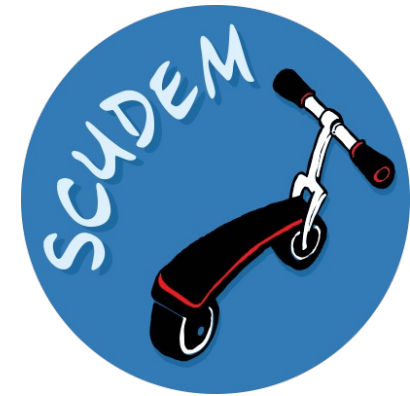


Projects in Differential Equations

Using the chat: what challenges do you encounter when you have group project, or think you would encounter, if you were to incorporate them into your class?

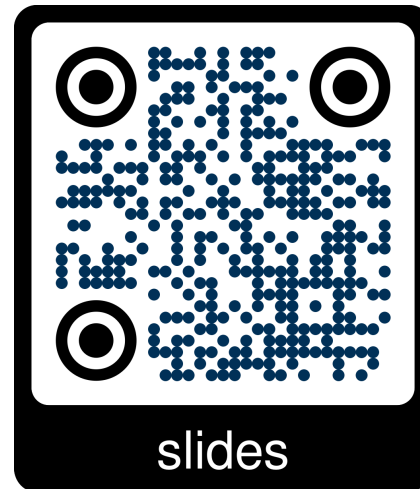
Online Differential Equations Group Project

- Modeled off of the annual SCUDEM challenge
- Students must:
 - Create numerical solution
 - Incorporate a non-linear system with at least two dependent variables
 - Work in group of 2 or 3
 - Write a ~1,500 word essay
 - Choose a topic, but we give suggestions from SIMIODE
- Final project report due at end of semester.
- Project mini-conference where students:
 - Share final report draft on course forum
 - Comment on each other's drafts
 - Reply to comments



Online Differential Equations Group Project: Rubric

- After a few semesters of grading student projects we have been working on refining a rubric
 - Based on SCUDEM challenge scoring rubric.
 - Addresses some of the common challenges students have in technical writing.
- Download our project instructions and rubric:



Questions?

- Would be happy to answer any questions that you might have!
- Greg Mayer: greg.mayer@gatech.edu

