

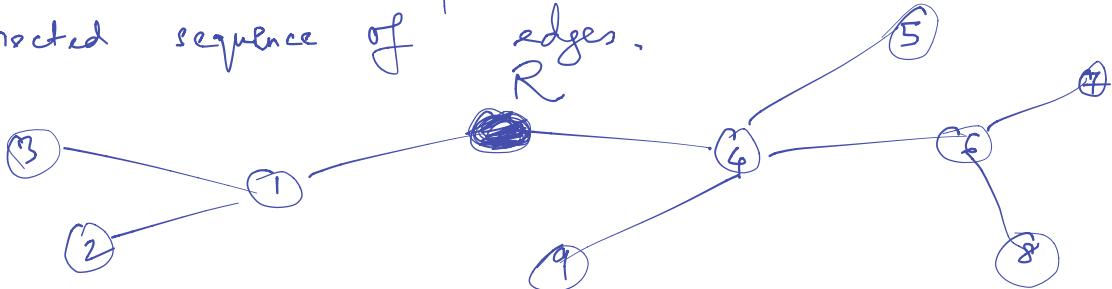
# TREES

## Rooted Trees

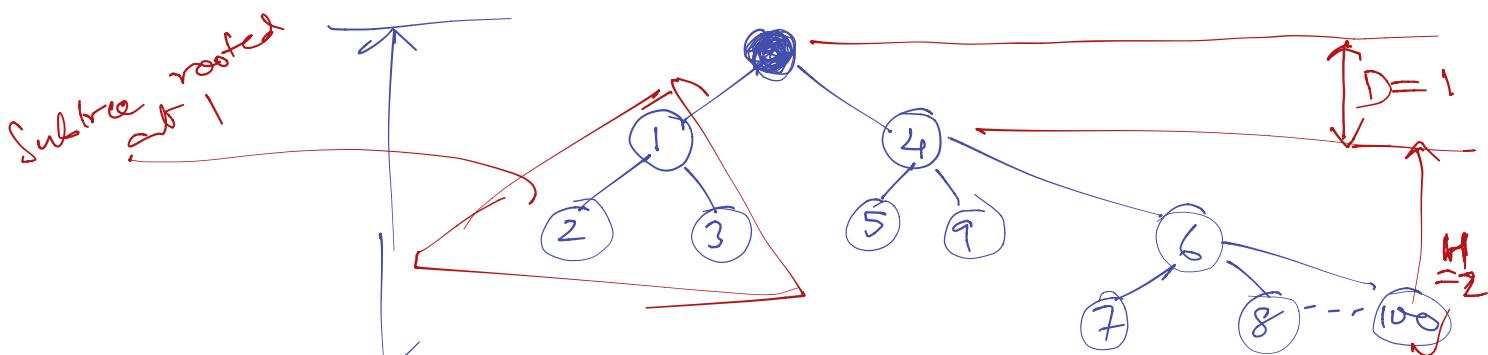
Tree : Set of nodes and edges that connect them.

→ Exactly one path between two nodes.

Path : Connected sequence of edges.



Rooted tree : One distinguished node is called the Root



Every node  $n$ , except Root, has ONE parent,  $p$ ;  
the first node on the path from  $n$  to the root.

$n$  is  $p$ 's child.

Root has NO parent.

A node can have ANY number of children.

Leaf : Node with NO children.

Siblings : Nodes with the same parent.

Ancestors : of a node  $n$  are the nodes on the path from  $n$  to the root (including  $n$  itself and the root).

If  $a$  is an ancestor of  $n$ ,  $n$  is a descendent

of a.

Length of a path: Number of edges on the path.

Node to itself  $\rightarrow$  Path length = 0

Depth of node n: Length of the path from n to the Root. Depth of the Root = 0.

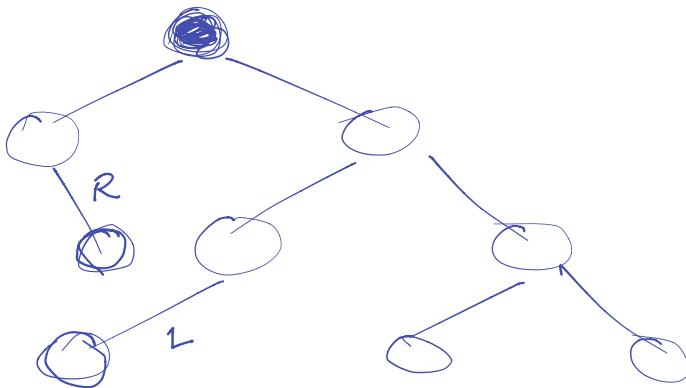
Height of node n: Length of path from n to its deepest descendent. Height of a leaf node = 0.

Height of a tree = Height of the Root

Subtree rooted at n: Tree formed by n and its descendants.

Binary tree: No node has  $\geq 2$  children  
 $\hookrightarrow \leq 2$  children

Every child is either the left or the right child  
(even if it is the ONLY child)



Representation of Rooted trees

- Item
- Parent
- Siblings are directly linked.



```
class TreeNode {
```

```
    Object item;
```

```
    TreeNode * parent;
```

```
    TreeNode * firstChild; } Linked
```

```
    TreeNode * nextSibling; } chain
```

```
}
```

```
class RootedTree {
```

```
    TreeNode * Root;
```

```
}
```

