

Additive Manufacturing – Module 6

Spring 2015

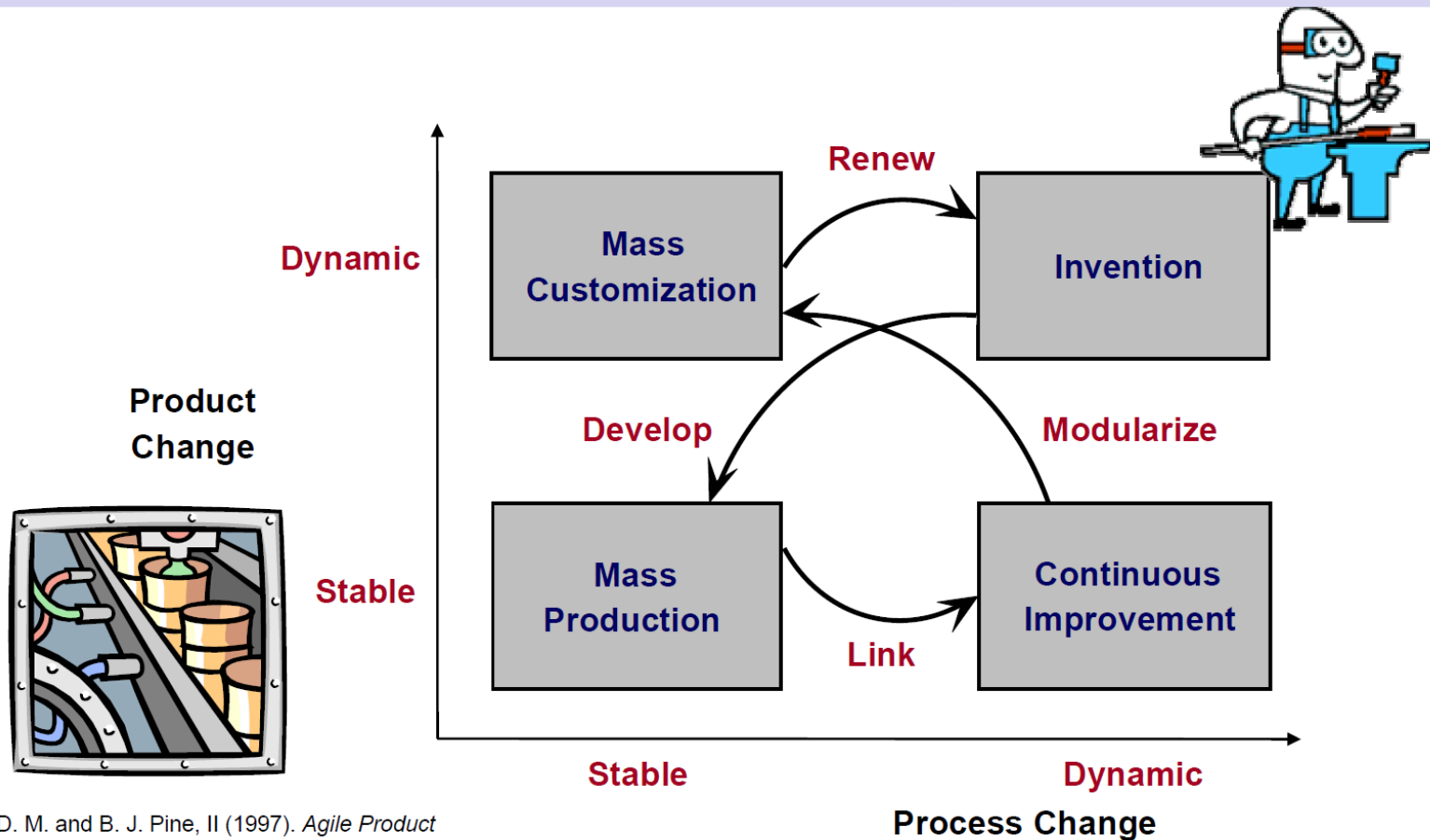
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University of Arkansas, Fayetteville

❖ Manufacturing paradigms

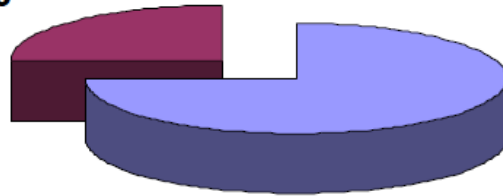


Anderson, D. M. and B. J. Pine, II (1997). *Agile Product Development for Mass Customization*. Chicago, Irwin.

❖ Design for Manufacturing

Manufacturing

20 - 30%



Design
70 - 80%

Concept Design



**Design for
Assembly**

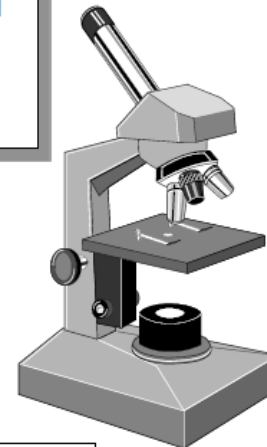


**Design for
Manufacturing**



Detailed Design

Optimize Design for
Part Count and
Assembly



Optimize Design for
Production Readiness

❖ Design for Assembly (DFA) Principles

- ❖ Minimize part **count**
 - ❖ Design parts with **self-locating features**
 - ❖ Design parts with **self-fastening features**
 - ❖ Minimize **reorientation** of parts during assembly
 - ❖ Design parts for **retrieval, handling, & insertion**
 - ❖ Emphasize '**Top-Down**' assemblies
 - ❖ **Standardize** parts...minimum use of fasteners.
 - ❖ Encourage **modular** design
 - ❖ Design for a **base** part to locate other components
 - ❖ Design for component **symmetry** for insertion
-
- ❖ Minimize DFA complexity: $\sqrt{\sum N_p \cdot \sum N_i}$
 - ❖ N_p : number of parts
 - ❖ N_i : number of part to part interfaces

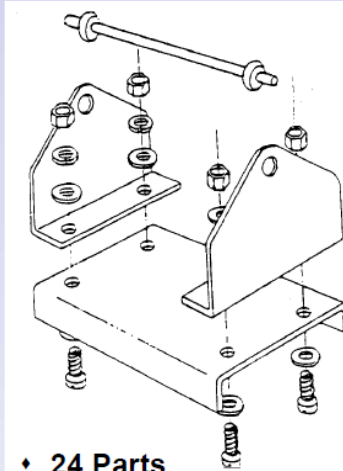
Design for Assembly Principles

Design

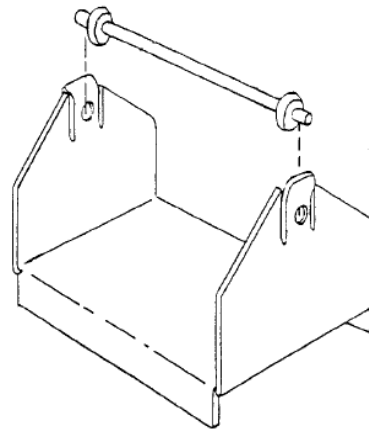
Optimization

Geometry

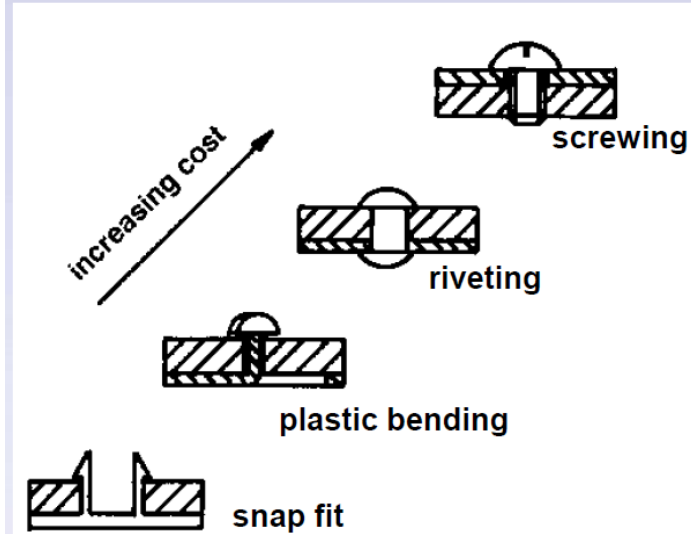
Materials



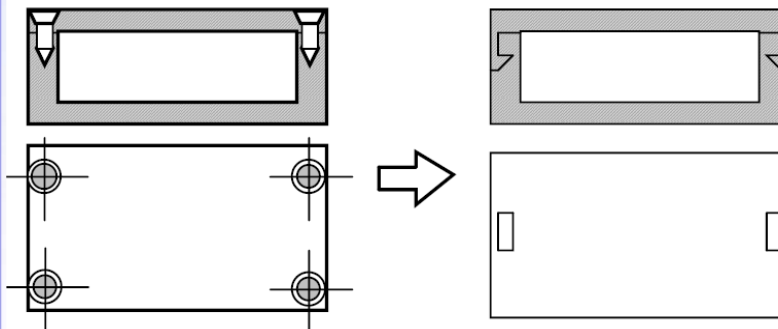
- ♦ 24 Parts
- ♦ 8 different parts
- ♦ multiple mfg. & assembly processes necessary



- ♦ 2 Parts
- ♦ 2 Manufacturing processes
- ♦ one assembly step



Component elimination



Self-fastening feature

Fastener cost

Pareto by Part Cost

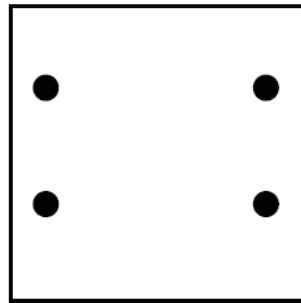
- | | |
|--------------|------|
| 1. Castings | \$\$ |
| 2. Forging | \$\$ |
| 3. | |
| | |
| | |
| | |
| n. Fasteners | c |

Pareto by Total Cost

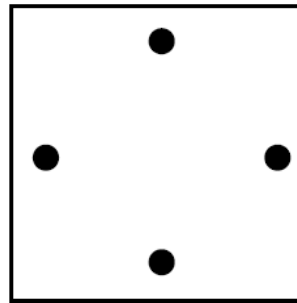
- | | |
|--------------|------------|
| 1. Fasteners | \$\$\$\$\$ |
| 2. | |
| 3. | |
| | |
| | |
| | |
| n. Castings | \$\$ |

Cost of fastening

Design for Assembly Principles

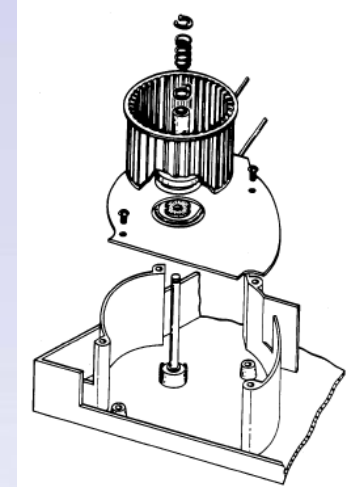


Asymmetric Part

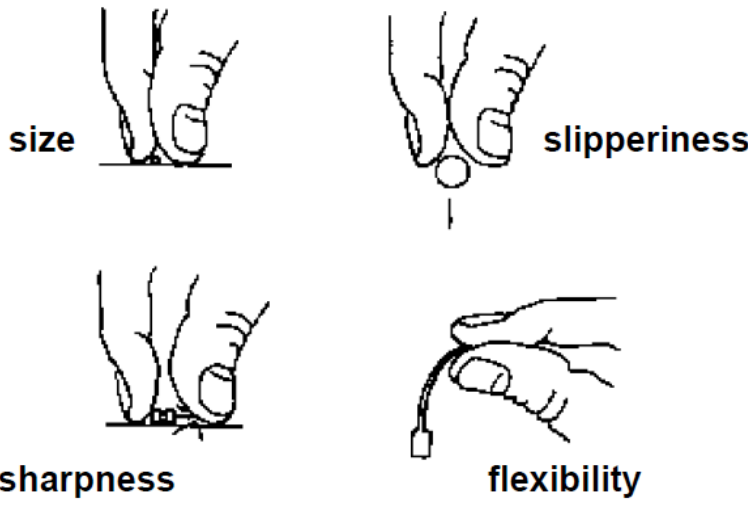


Symmetry of a part
makes assembly easier

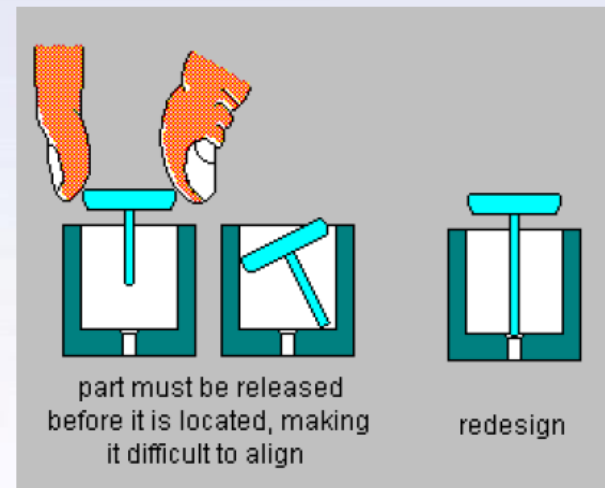
Symmetry eliminates reorientation



Top-down assembly



Handling difficulty



Self-locating

❖ Manufacturing processes

Machining	Casting	Bulk Def	Sheetmetal	Polymer	Assembly
Turning	Sand	Forging	Blanking	Extrusion	Welding
Facing	Shell Mold	Rolling	Punching	Injection Molding	Brazing
Boring	Plast. Mold	Wire	Bending	Compressi-on Molding	Soldering
Planning	Ceram. Mold	Drawing	Drawing	Blow Molding	Resistance Welding
Milling	Die	Tube Drawing	Deep Drawing	Transfer Molding	Adhesive Bonding
Drilling	Perm. Mold	Extrusion	Ironing	Coating	Press/snap fit
Grinding	Centrifugal	Colming	Spinning	Thermoforming	Man. Assy
Sawing	Investment	Roll Forming	Stretching		Flex. Assy
EDM					
Wire EDM					
Chem. milling					
ECM					
Laser					

Source: Dixon and Poly

Shaping	Forming	RP	Treatment	Assembly
Casting	Forging	SLA	Harden	Welding
Sintering	Extruding	SLS	Heat Treatment	Brazing
Electrolytic Deposition	Bending	3D Printing	Sintering and burning	Soldering
	Shearing	LENS	Magnetizing	Resistance Welding
	Pressing	UC	Photochemical Reactions	Adhesive Bonding
			Lazing	Press/snap fit

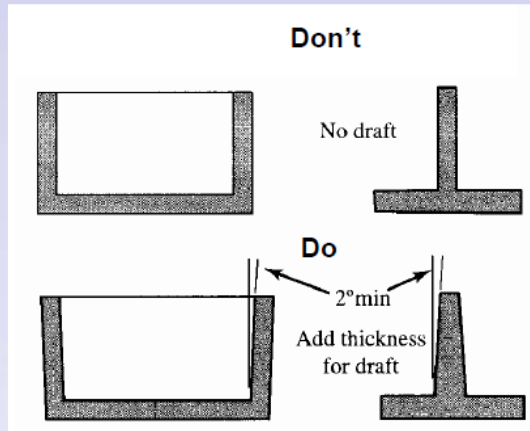
Design for Manufacturing (DFM) – injection molding

Design

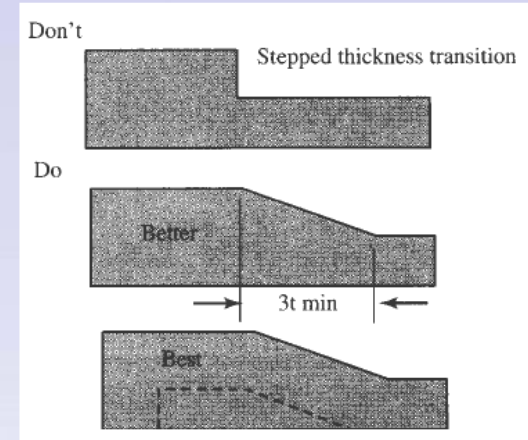
Optimization

Geometry

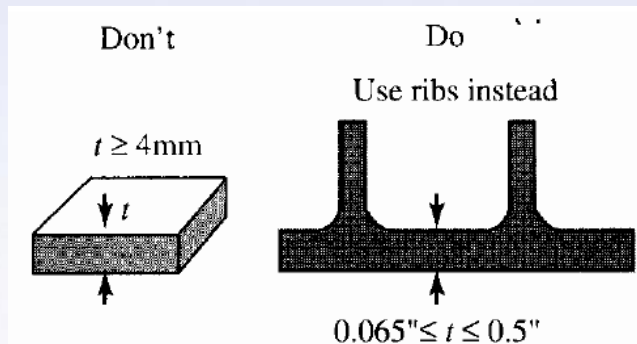
Materials



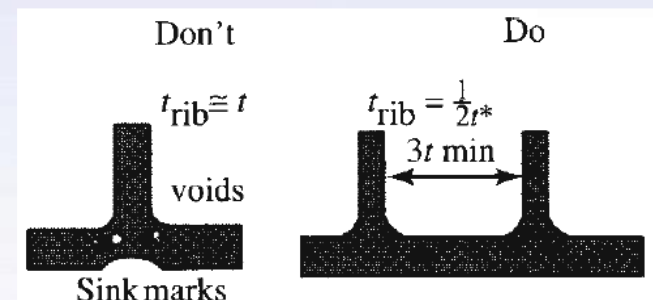
Provide adequate draft angle for easier part removal



Provide smooth transition, avoid changes in thickness when possible

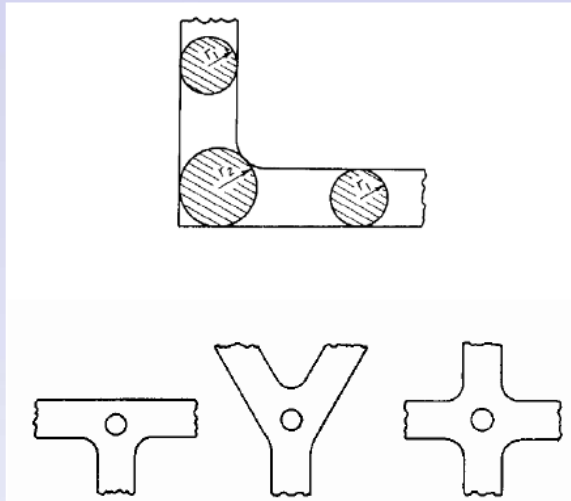


Minimize section thickness; cooling time is proportional to the square of the thickness. Reduce cost by reducing the cooling time.

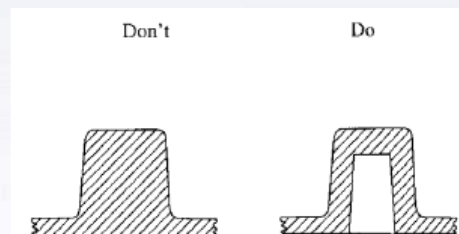
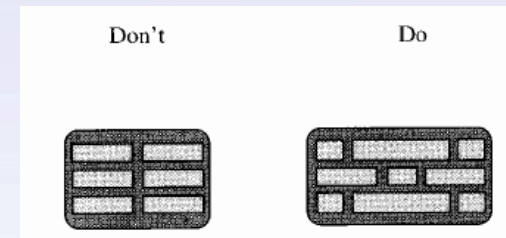
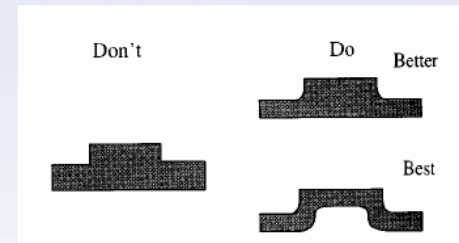
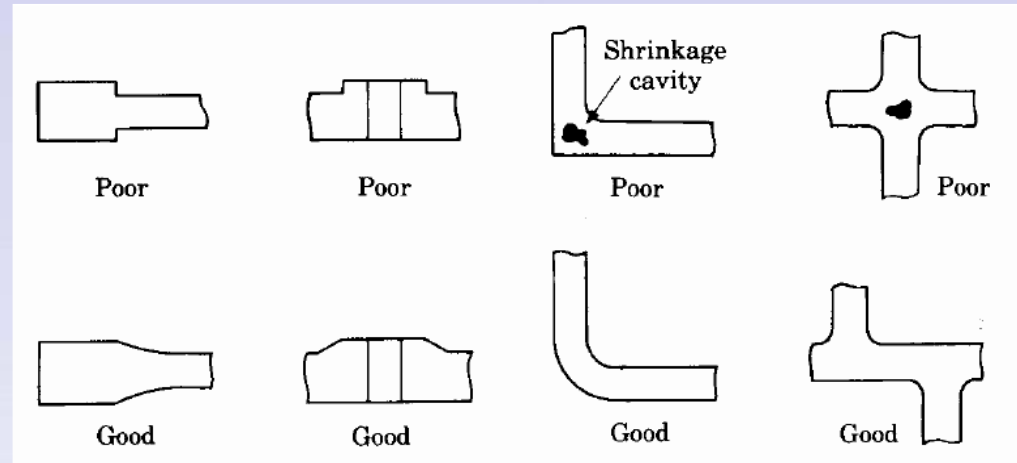


Keep rib thicknesses less than 60% of the part thickness in order to prevent voids and sinks.

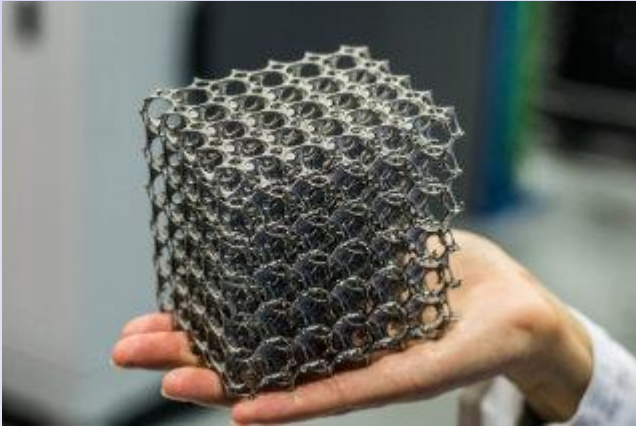
Design for Manufacturing (DFM) – Casting



Hot spots –thick sections cool slower than other sections causing abnormal shrinkage. Defects such as voids, cracks and porosity are created.



◆ Design for Additive Manufacturing (DFAM)



Complex geometry



Multimaterial (Stratasys)



Assembly



Functionality (credit: UTEP)

◆ **Need next-generation CAD**

◆ **Need to find ways to use the overwhelming design freedom**

❖ Geometry Optimization

Minimize $f(\mathbf{x})$

Subject to $g(\mathbf{x}) \leq 0$

$h(\mathbf{x}) = 0$

$f(\mathbf{x})$: Objective function to be minimized

$g(\mathbf{x})$: Inequality constraints

$h(\mathbf{x})$: Equality constraints

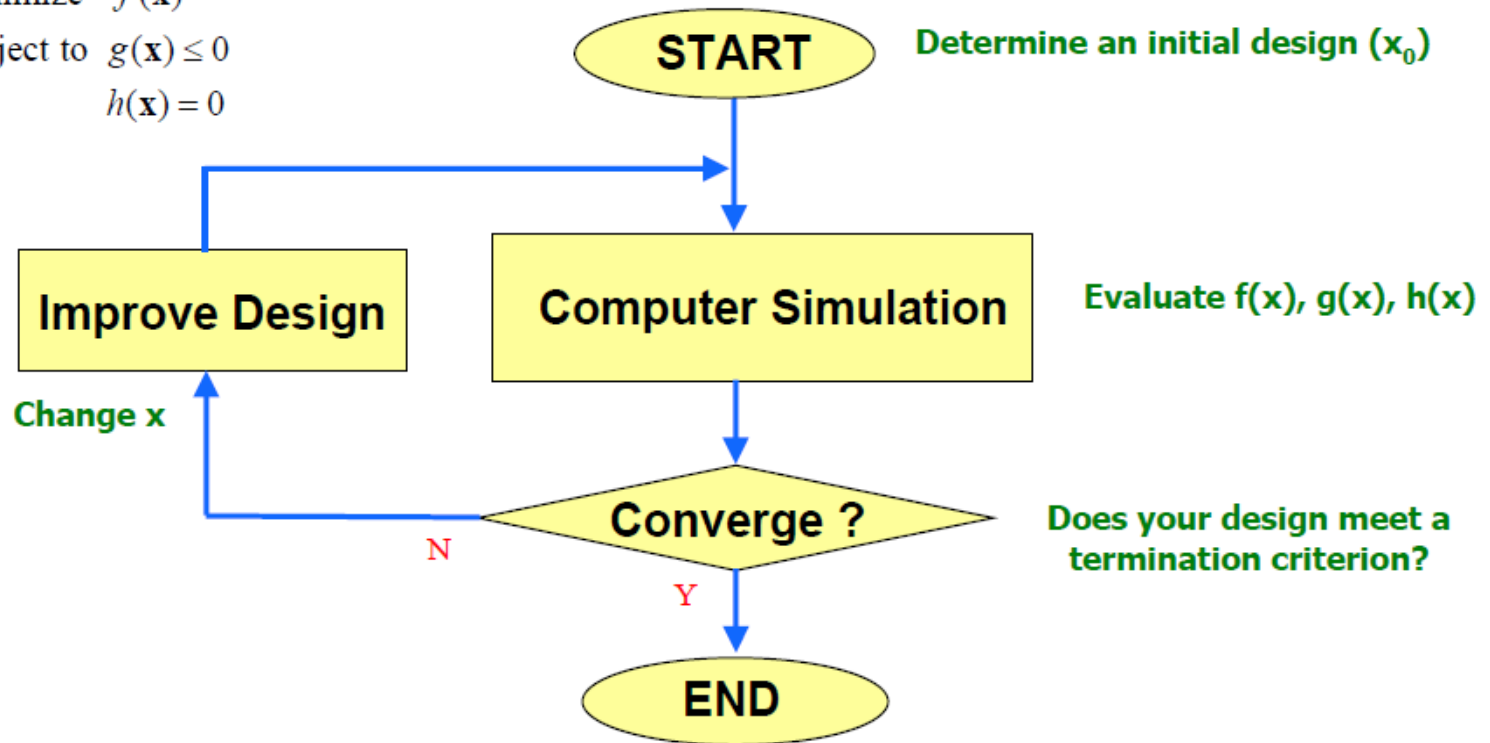
\mathbf{x} : Design variables

❖ Geometry Optimization

Minimize $f(\mathbf{x})$

Subject to $g(\mathbf{x}) \leq 0$

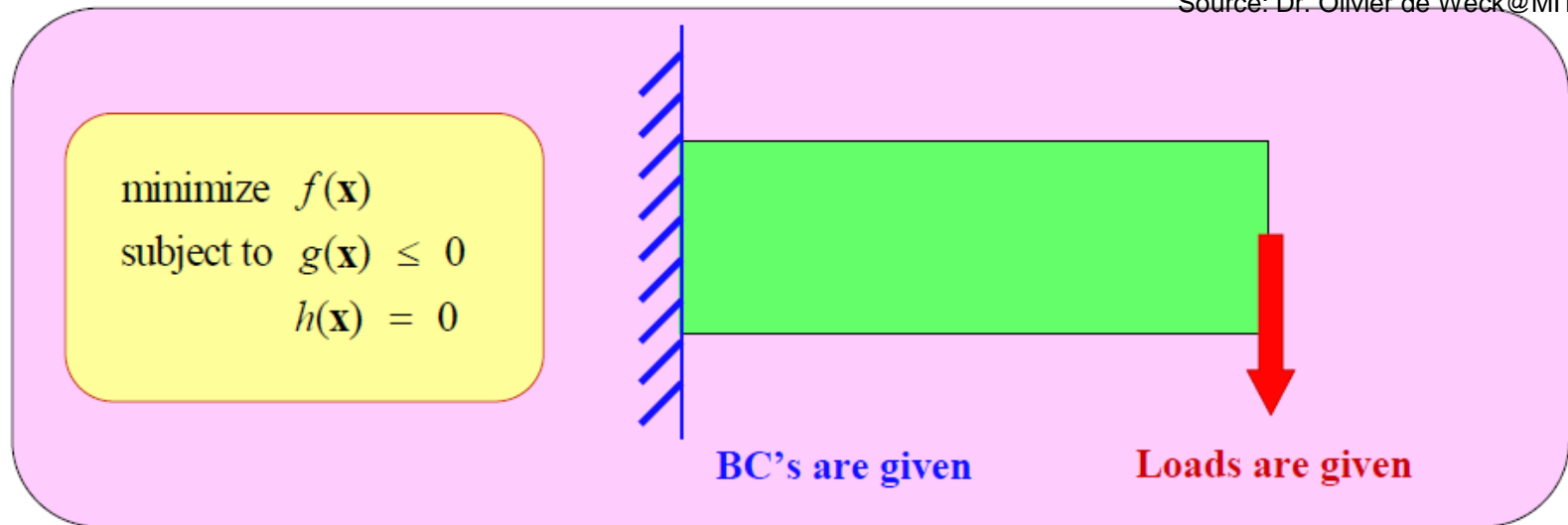
$h(\mathbf{x}) = 0$



Optimization procedure

❖ Geometry Optimization

Source: Dr. Olivier de Weck@MIT



1. To make the structure strong
e.g. Minimize displacement at the tip

➡ $Min. f(\mathbf{x})$

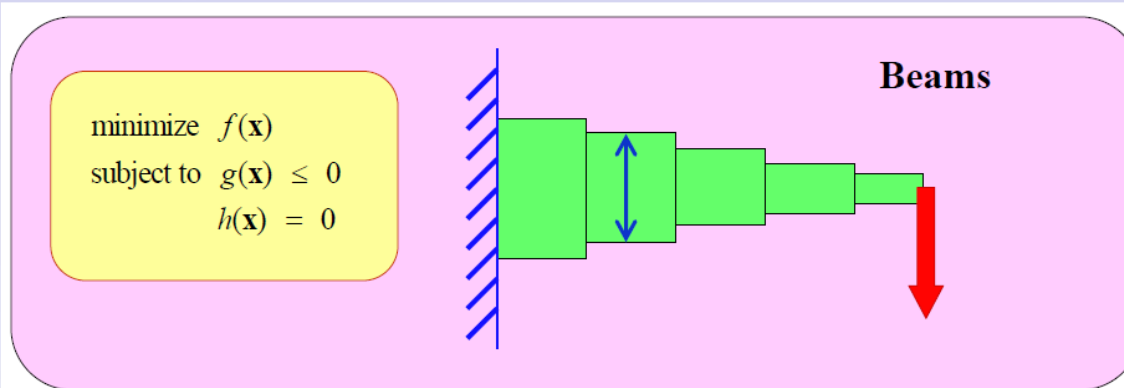
2. Total mass $\leq M_c$

➡ $g(\mathbf{x}) \leq 0$

Structure optimization

Manufacturing perspective: One of the ultimate goal of the structure optimization is that standard deviation of the stress distribution becomes zero (each members in a structure has the stress of the same level).

Geometry Optimization



Design variables (x)

x : thickness of each beam

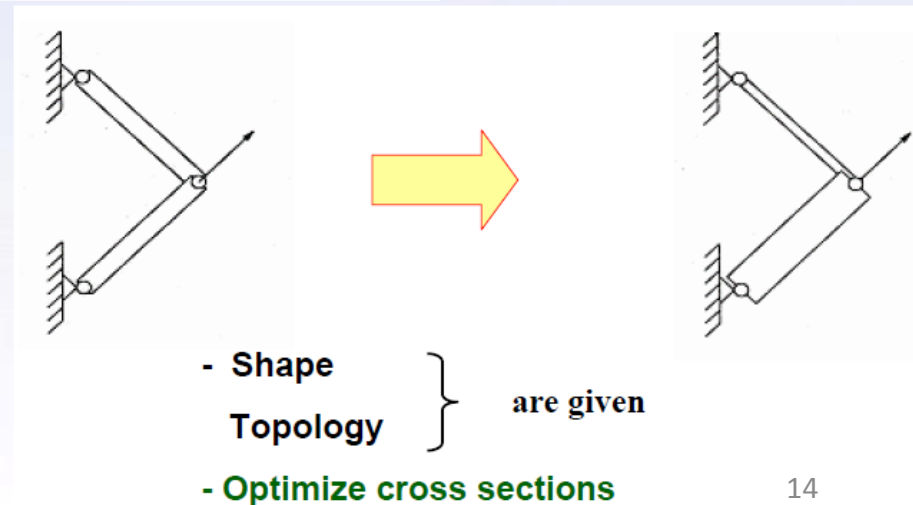
$f(x)$: compliance

$g(x)$: mass

Number of design variables (ndv)

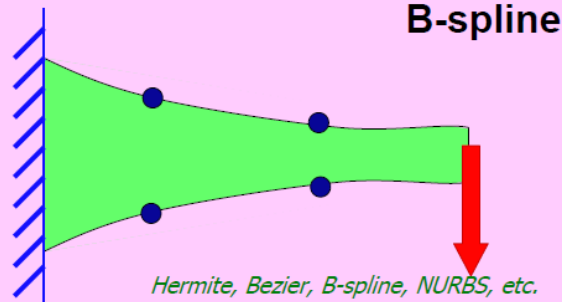
ndv = 5

Size optimization



Geometry Optimization

$$\begin{aligned} &\text{minimize } f(\mathbf{x}) \\ &\text{subject to } g(\mathbf{x}) \leq 0 \\ &\quad h(\mathbf{x}) = 0 \end{aligned}$$



Design variables (\mathbf{x})

\mathbf{x} : control points of the B-spline
(position of each control point)

$f(\mathbf{x})$: compliance

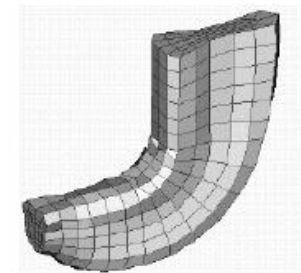
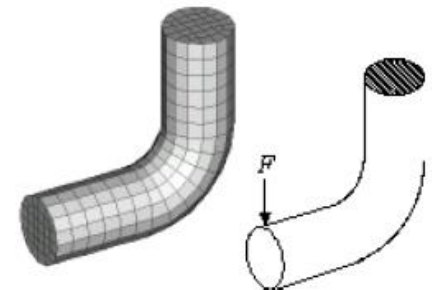
$g(\mathbf{x})$: mass

Number of design variables (ndv)

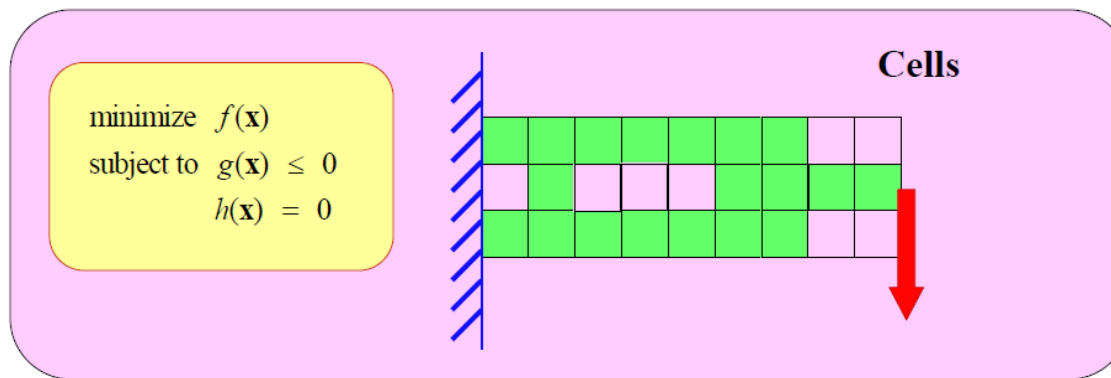
ndv = 8

Shape optimization

Hook problem



❖ Geometry Optimization



Design variables (x)

\mathbf{x} : density of each cell

Number of design variables (ndv)

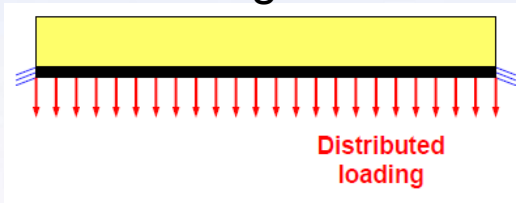
ndv = 27

$f(\mathbf{x})$: compliance

$g(\mathbf{x})$: mass

Topology optimization (online tool: <http://www.topopt.dtu.dk>)

Bridge



$$\text{Minimize } \int_{\Gamma} F^i z^i d\Gamma,$$

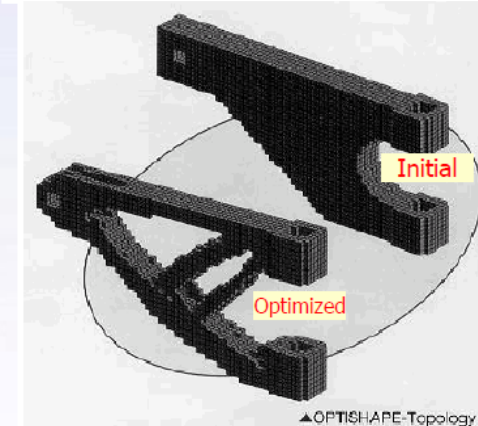
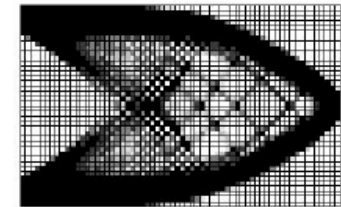
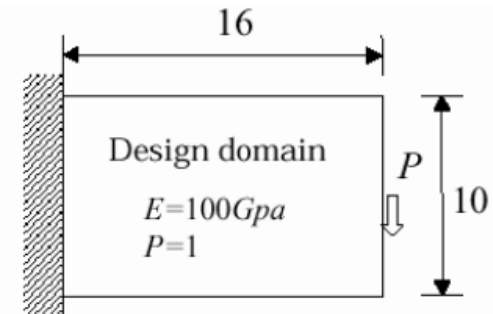
$$\text{Subject to } \int_{\Omega} \rho(x) d\Omega \leq M_o,$$

$$0 \leq \rho(x) \leq 1$$

Mass constraints: 35%



Short cantilever problem

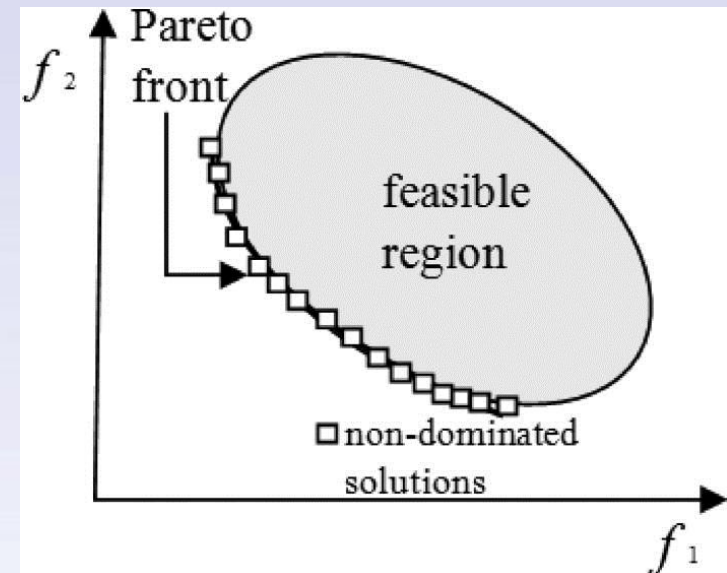
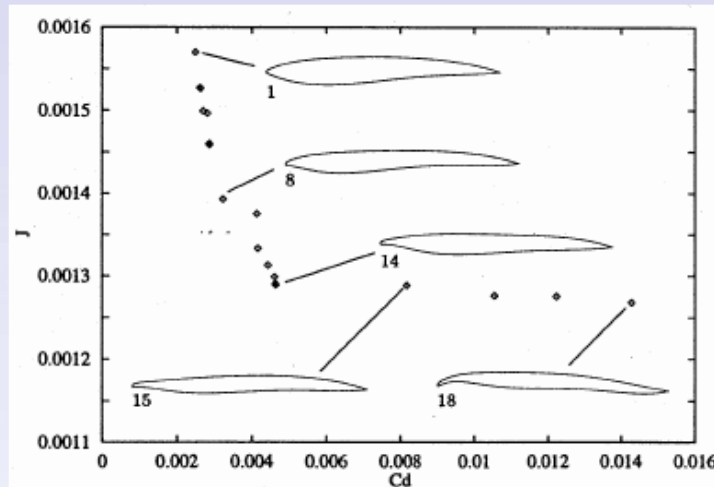


❖ Geometry Optimization

❖ Multiobjective:

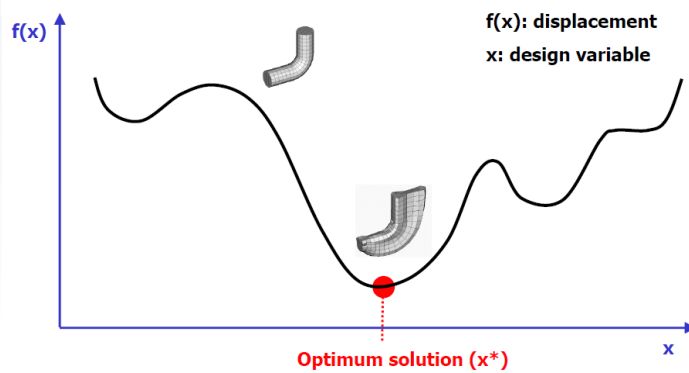
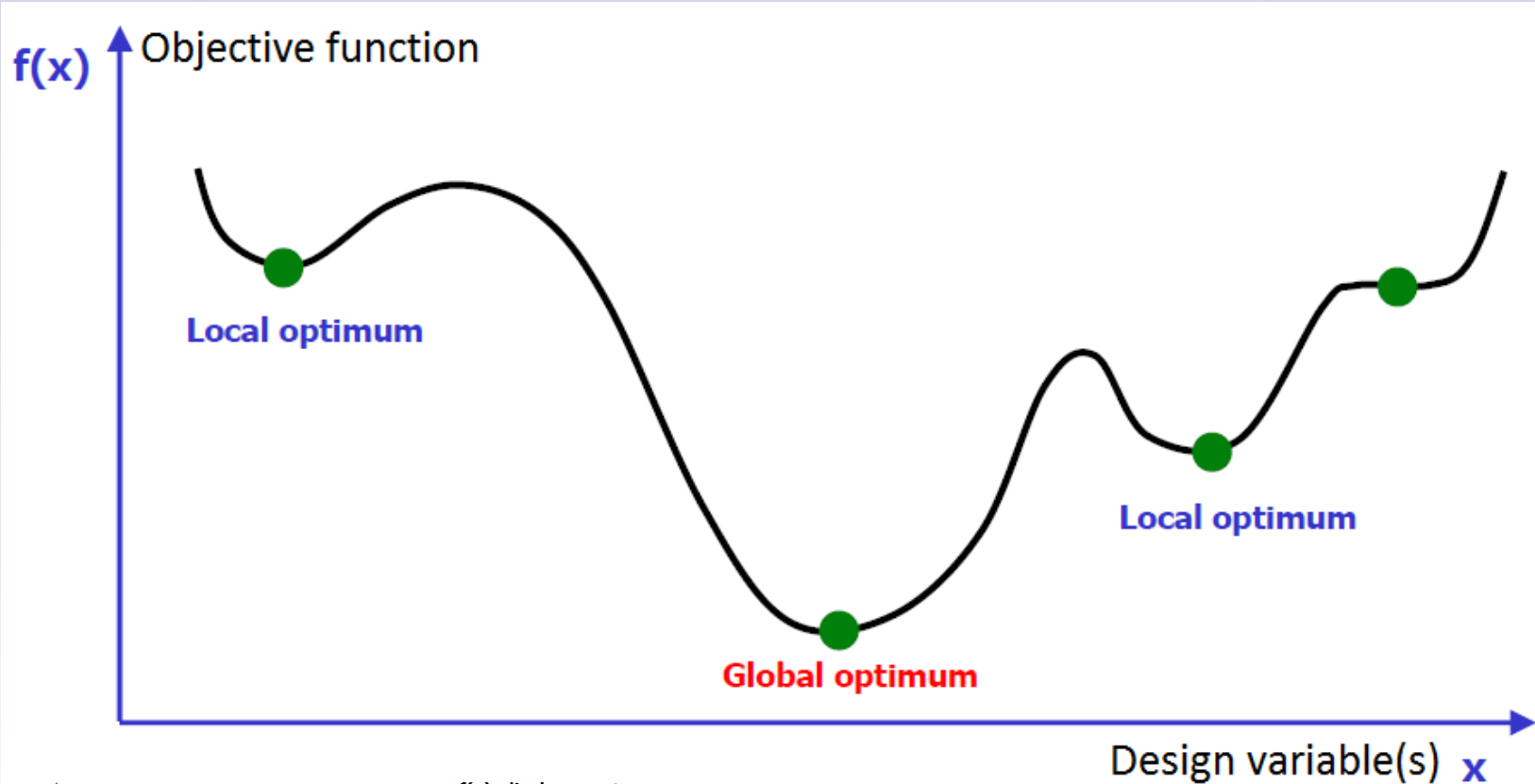
❖ Drag coefficient

❖ Amplitude of backscattered wave



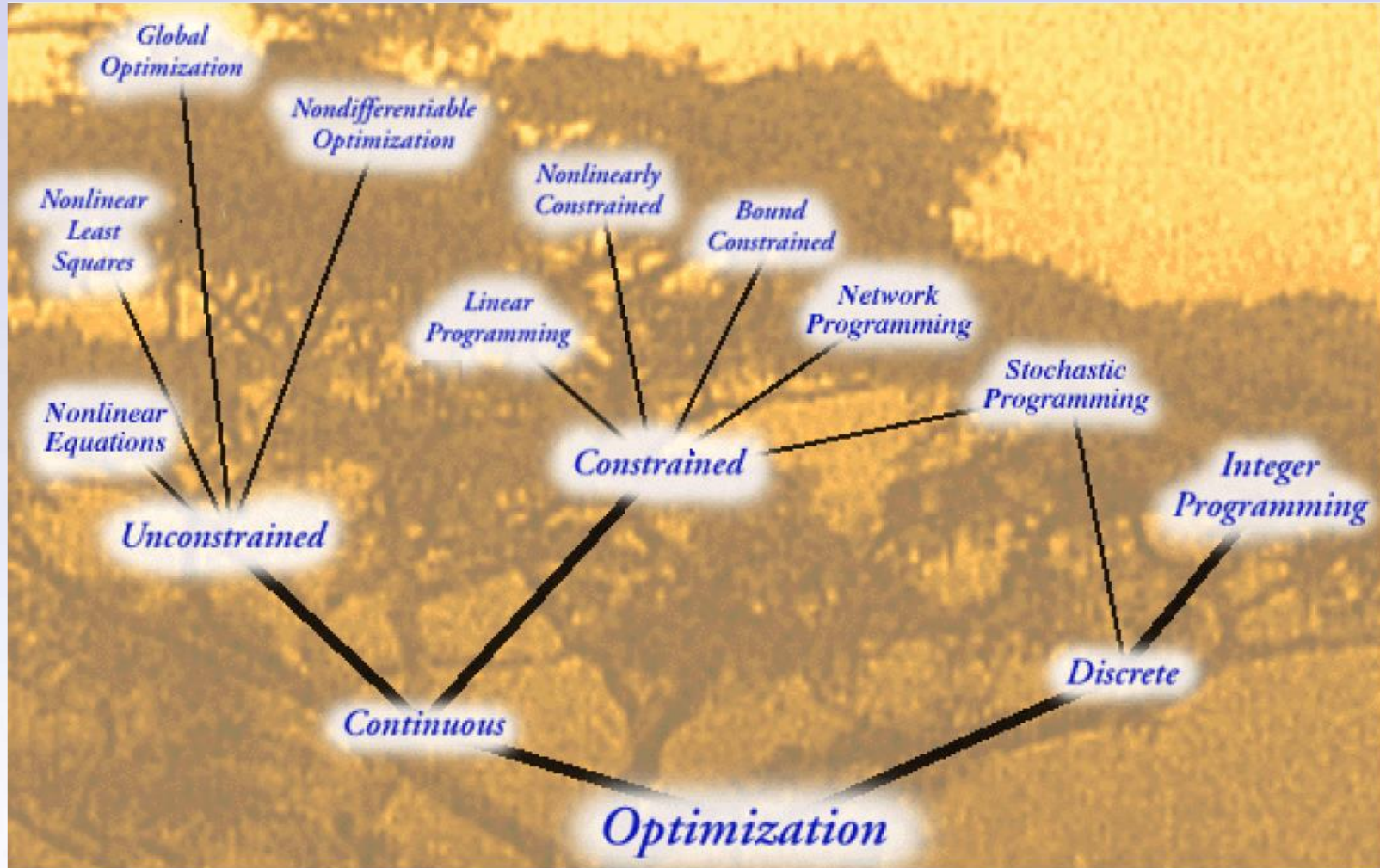
Pareto efficiency, or **Pareto optimality**, is a state of allocation of [resources](#) in which it is impossible to make any one individual better off without making at least one individual worse off. The term is named after [Vilfredo Pareto](#) (1848–1923), an Italian economist. (From Wikipedia)

❖ Geometry Optimization



Example

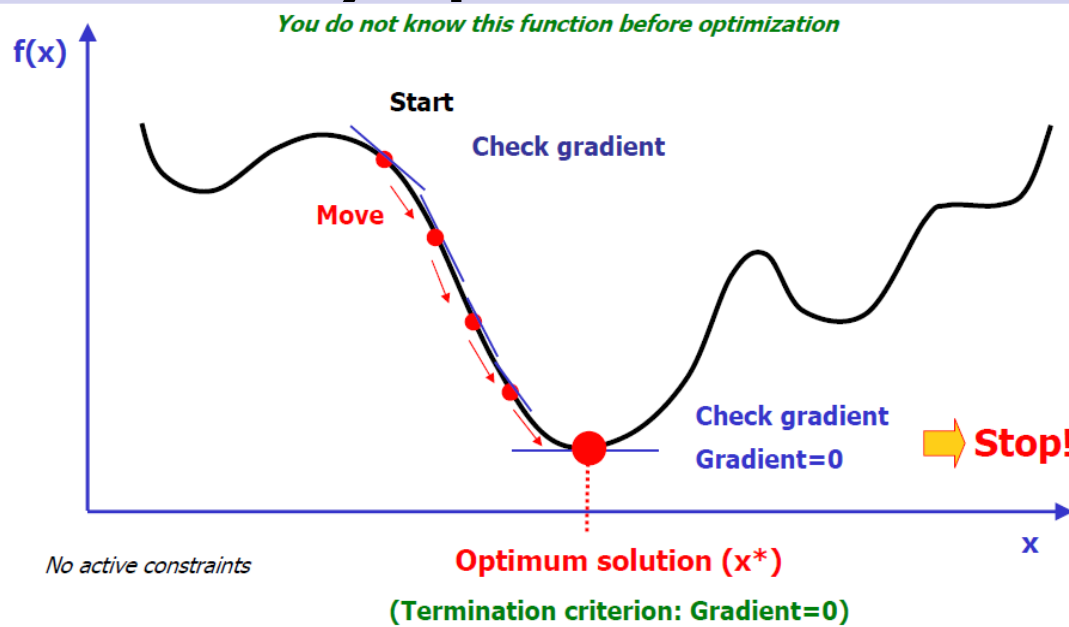
❖ Geometry Optimization – how



Optimization algorithms and methods: (Over 100)

[http://en.wikipedia.org/wiki/Category:Optimization algorithms and methods](http://en.wikipedia.org/wiki/Category:Optimization_algorithms_and_methods)

❖ Geometry Optimization – how



Gradient-based method

Steepest Descent
Conjugate Gradient
Quasi-Newton
Newton

UNCONSTRAINED

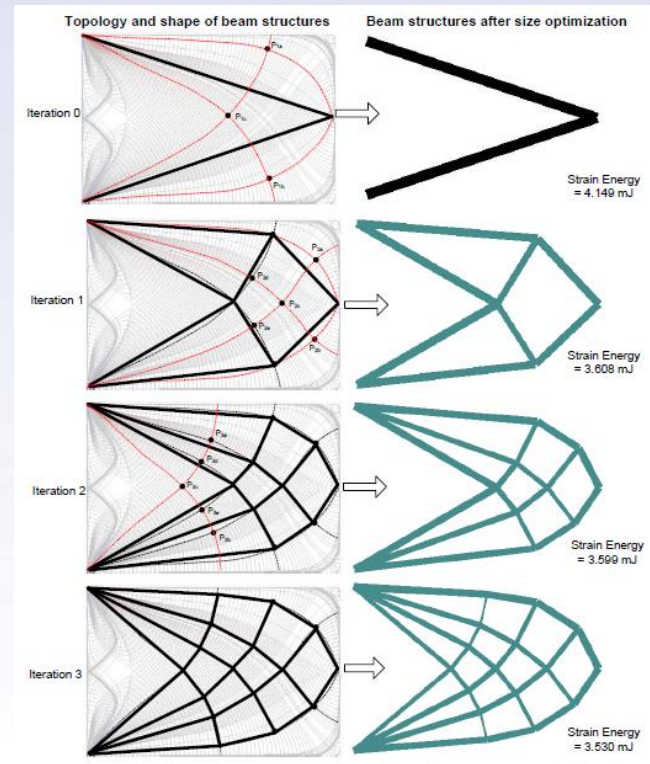
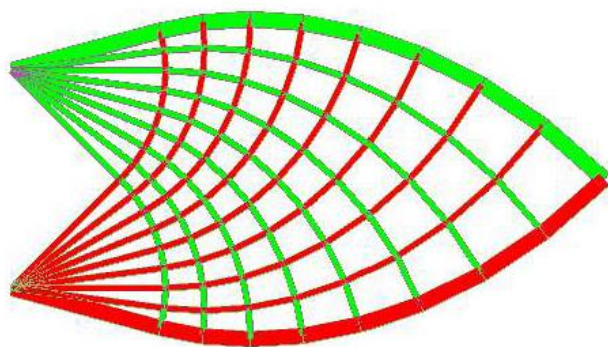
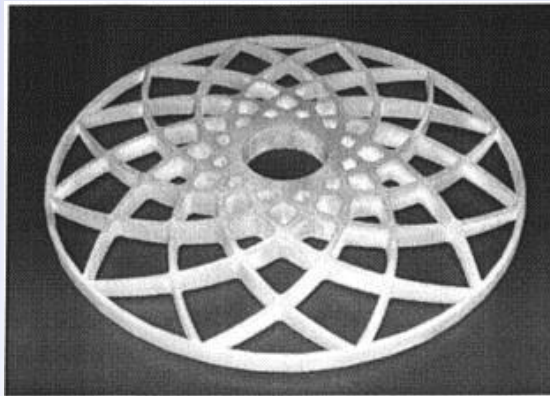
Simplex – linear
SLP – linear
SQP – nonlinear, expensive, common in engineering applications
Exterior Penalty – nonlinear, discontinuous design spaces
Interior Penalty – nonlinear
Generalized Reduced Gradient – nonlinear
Method of Feasible Directions – nonlinear
Mixed Integer Programming

CONSTRAINED

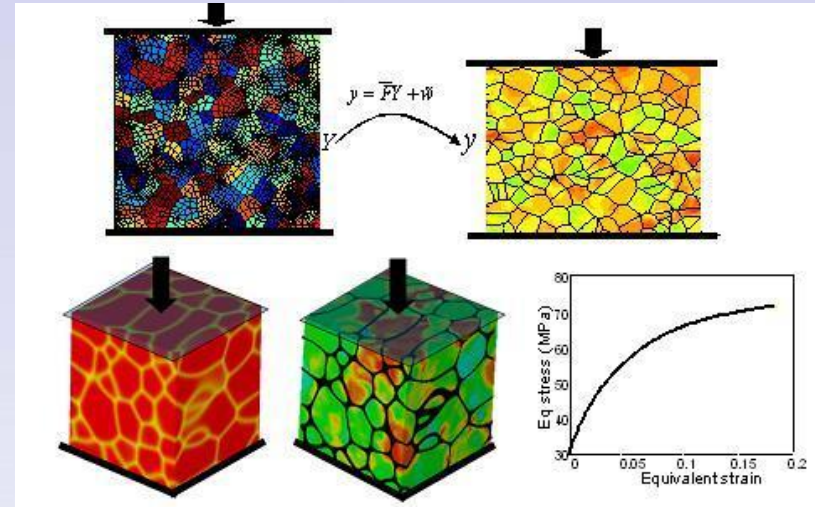
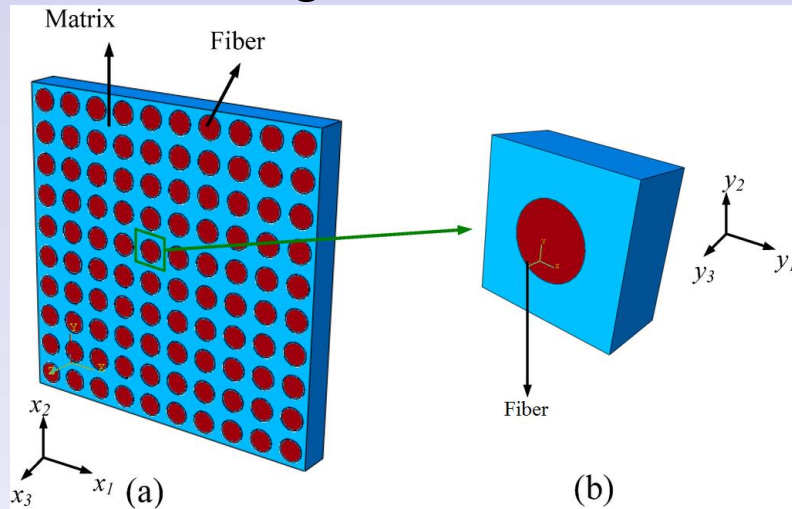
❖ Geometry Optimization – how

❖ Michell truss

- ❖ Proposed in 1904
- ❖ Only tensile and compressive members
- ❖ Intersect at right angle
- ❖ Corresponds to slip lines (max shear stress)
- ❖ Analytical solution (minimum weight for given load)
- ❖ Benchmark for code verification

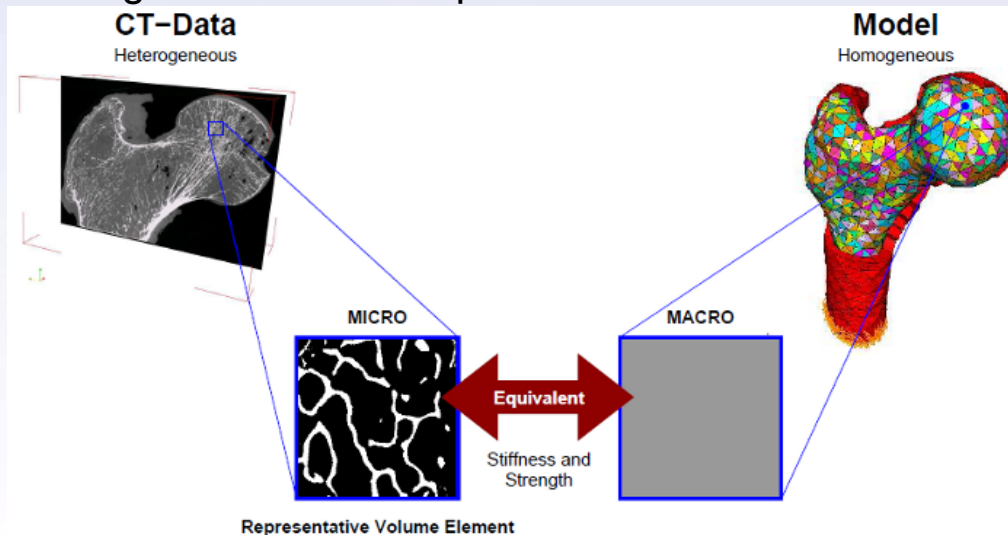


❖ Geometry Optimization – how ❖ Homogenization method



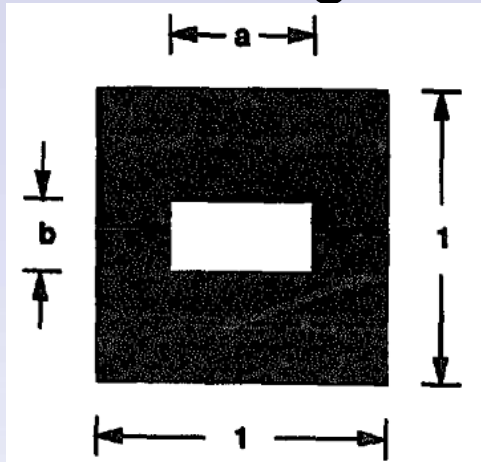
Calculate equivalent stress-strain relationship

Homogenization of composite materials

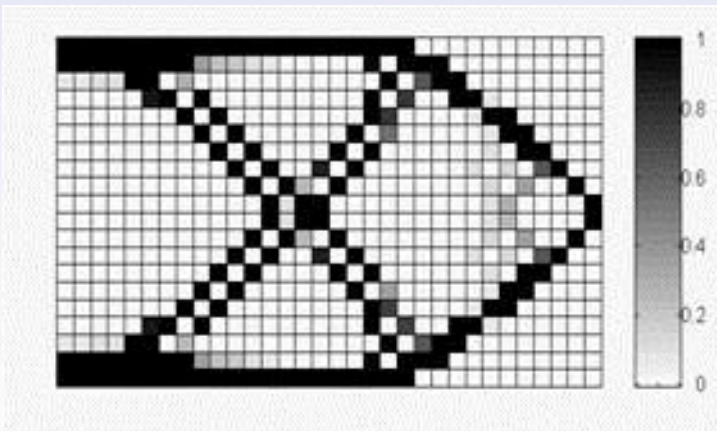


Example

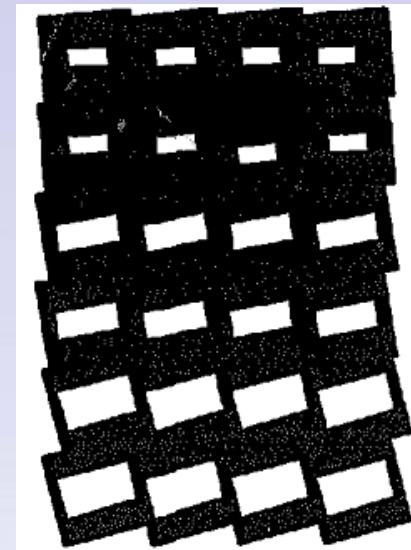
❖ Geometry Optimization – how ❖ Homogenization method



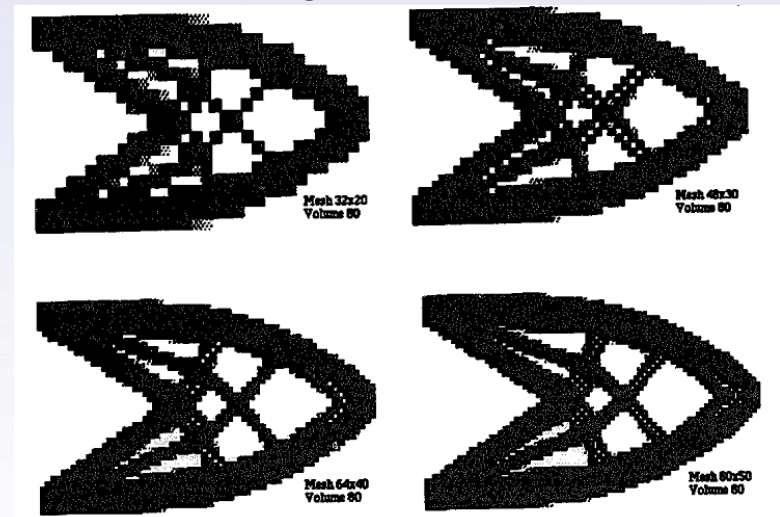
Unit cell microstructure



Consider structure as a
composite of material and
voids (volume fraction)



Change in microstructure



Convergence of optimal design

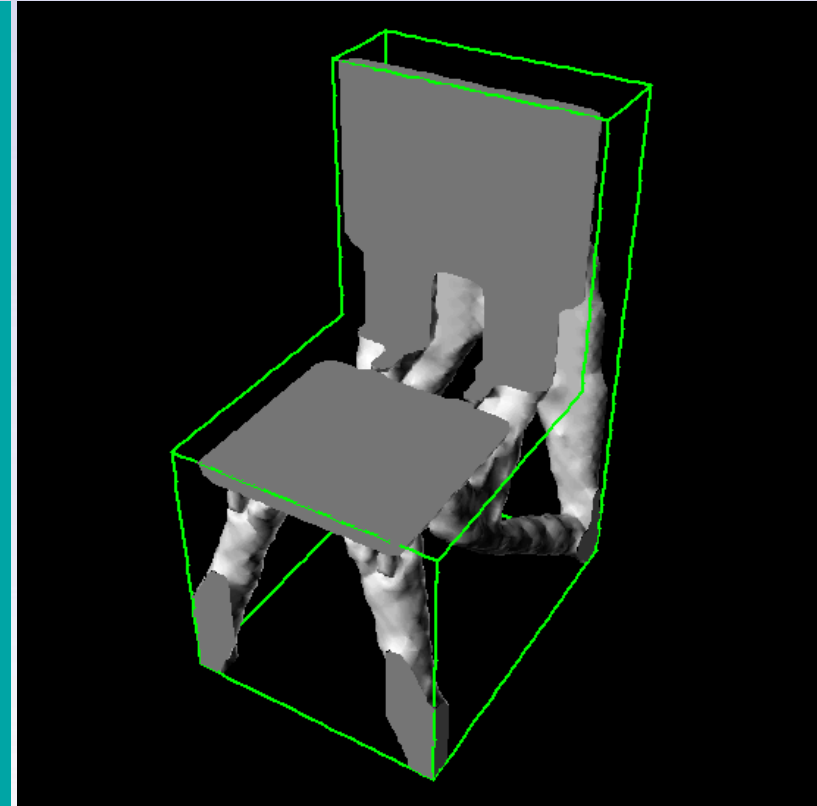
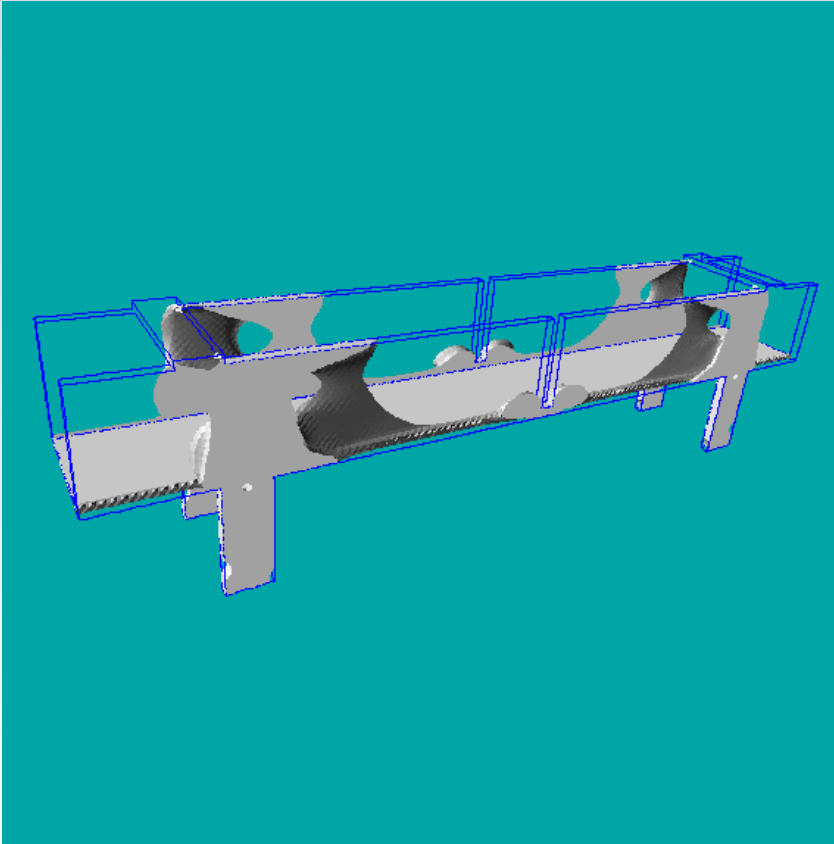
❖ Geometry Optimization – how ❖ Homogenization method

Design

Optimization

Geometry

Materials



http://www.cmap.polytechnique.fr/~optopo/homog_en.html

❖ Geometry Optimization – how

❖ Genetic Algorithm

- ❖ A class of probabilistic optimization algorithms
- ❖ Inspired by the biological evolution process
- ❖ Uses concepts of “Natural Selection” and “Genetic Inheritance” (Darwin 1859)
- ❖ Originally developed by John Holland (1975)
- ❖ Particularly well suited for hard problems where little is known about the underlying search space
- ❖ Widely-used in business, science and engineering



❖ Geometry Optimization – how

❖ Genetic Algorithm – steps

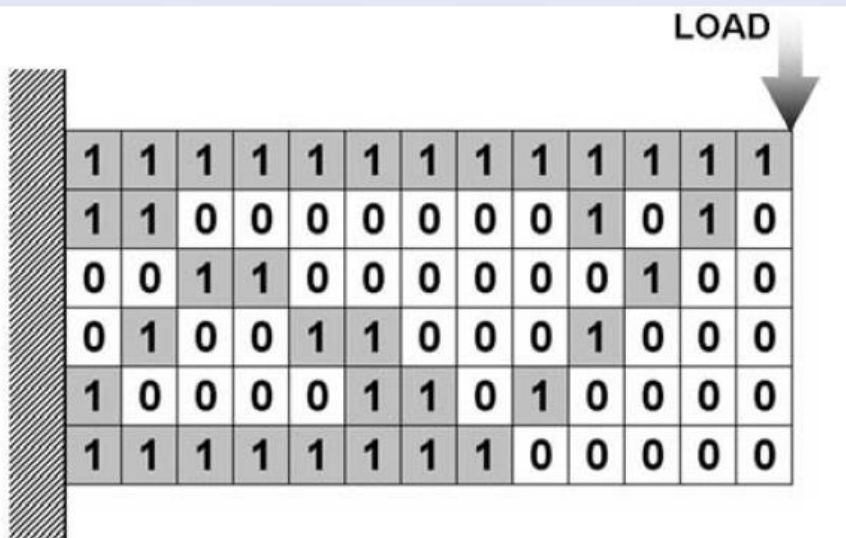
- ❖ **Encoding technique** (gene, chromosome)
- ❖ **Initialization procedure** (creation)
- ❖ **Evaluation function** (environment)
- ❖ **Selection of parents** (reproduction)
- ❖ **Genetic operators** (mutation, recombination)
- ❖ **Parameter settings** (practice and art)

```
{  
    initialize population;  
    evaluate population;  
    while TerminationCriteriaNotSatisfied  
    {  
        select parents for reproduction;  
        perform recombination and mutation;  
        evaluate population;  
    }  
}
```

❖ Geometry Optimization – how

❖ Genetic Algorithm – population

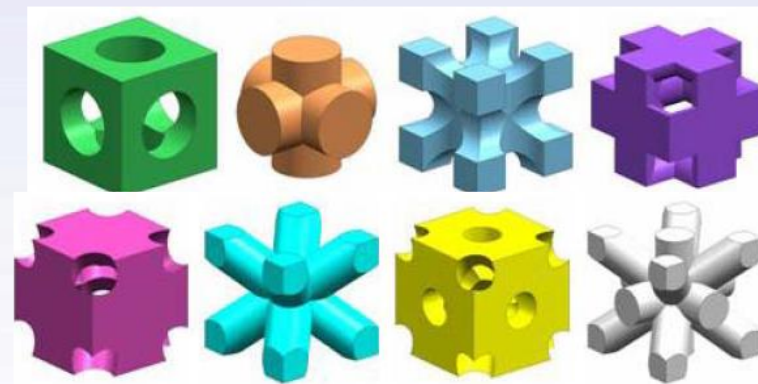
- ❖ Bit strings {0101 ... 1100}
- ❖ Real numbers {43.2 -33.1 ... 0.0 89.2}
- ❖ Permutations of element {E₁₁ E₃ E₇ ... E₁ E₁₅}
- ❖ Lists of rules {R₁ R₂ R₃ ... R₂₂ R₂₃}
- ❖ Program elements {genetic programming}
- ❖ ... any data structure ...



Encoding a structure using one bit string:
structure – phenotype; bit string – genotype.
One bit string (individual) is a design solution



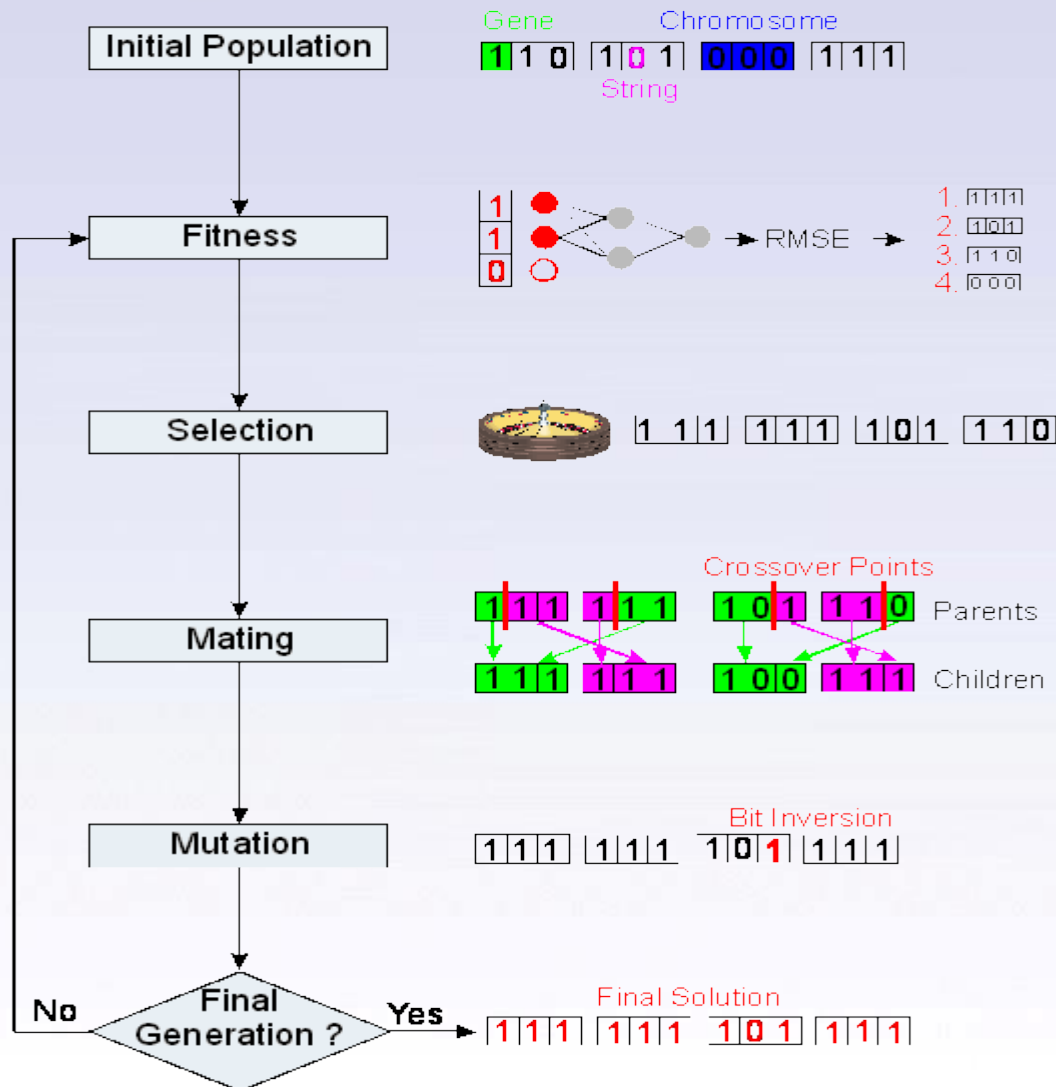
Encode with multiple materials



Other types of cell structure (bit)

❖ Geometry Optimization – how

❖ Genetic Algorithm – architecture



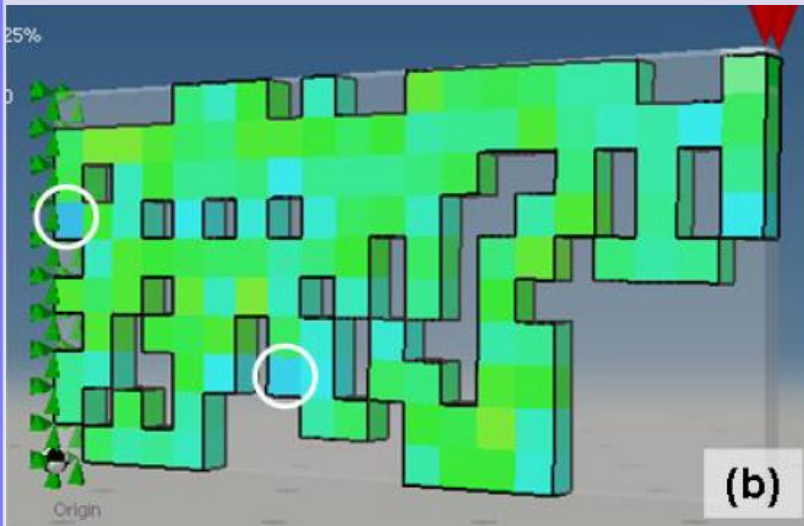
❖ Geometry Optimization – how ❖ Genetic Algorithm – results

Design

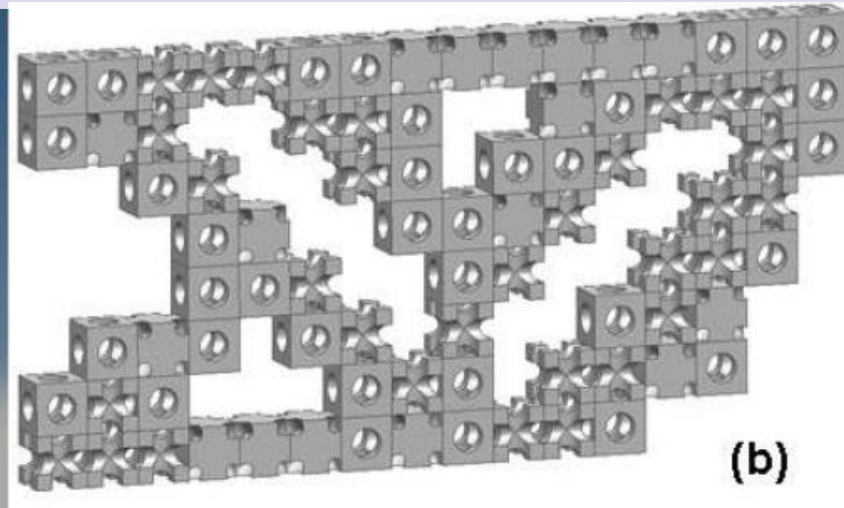
Optimization

Geometry

Materials

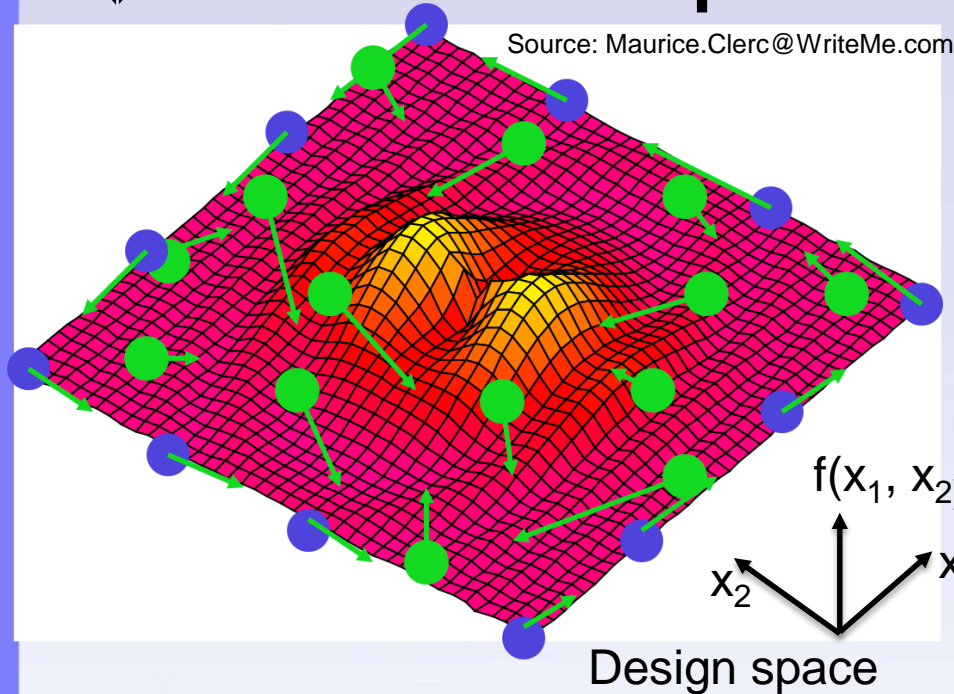


Cantilever Beam Result from DesignLab for a Single Material with Areas of Local High and Low Stress Circled



Possible Cantilever Beam Geometry Created From Three Cellular Structures each with 50% Volume Fractions

❖ Geometry Optimization – how ❖ Particle Swarm Optimization



Eq. (a):

$$v[] = c0 * v[] + c1 * \text{rand}() * (pbest[] - present[]) + c2 * \text{rand}() * (gbest[] - present[])$$

Eq. (b):

$$present[] = present[] + v[]$$

- ❖ Each particle is a design
- ❖ Each particle is moving in the design space with a velocity V in search for optimal
- ❖ Each particle remembers its personal best
- ❖ Particle V depends on its current V , the positions of the global best, position of its personal best, and maybe best neighbour

❖ Geometry Optimization – how ❖ Particle Swarm Optimization

For each particle
 Initialize particle
END

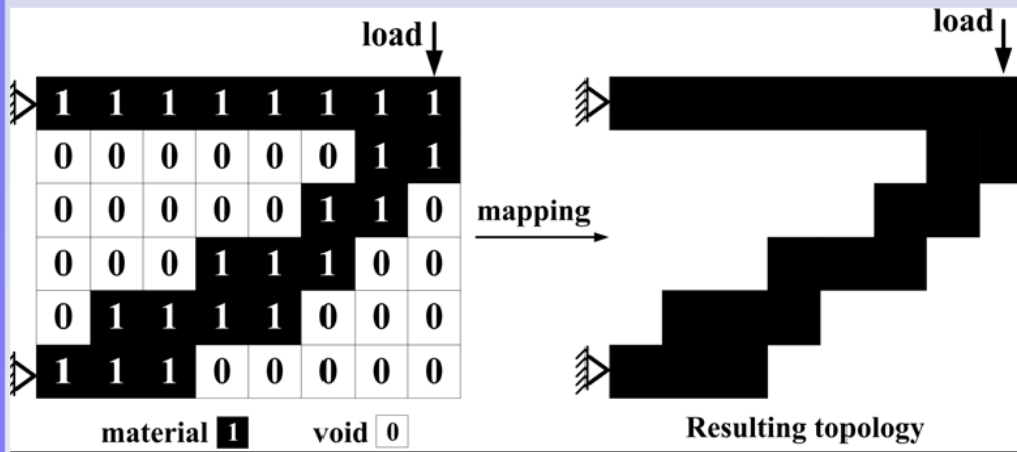
Do
 For each particle
 Calculate fitness value
 If the fitness value is better than its personal best
 set current value as the new **pBest**
 End

Choose the particle with the best fitness value of all as **gBest**
For each particle
 Calculate particle velocity according equation (a)
 Update particle position according equation (b)
End

While maximum iterations or minimum error criteria is not attained

❖ Geometry Optimization – how

❖ Particle Swarm Optimization – Binary for topology optimization



Eq. (a):

$$V_i^{k+1} = \mathbf{c}_1 \otimes \left(P_{best,i}^k \oplus X_i^k \right) + \mathbf{c}_2 \otimes \left(G_{best}^k \oplus X_i^k \right)$$

Eq. (b):

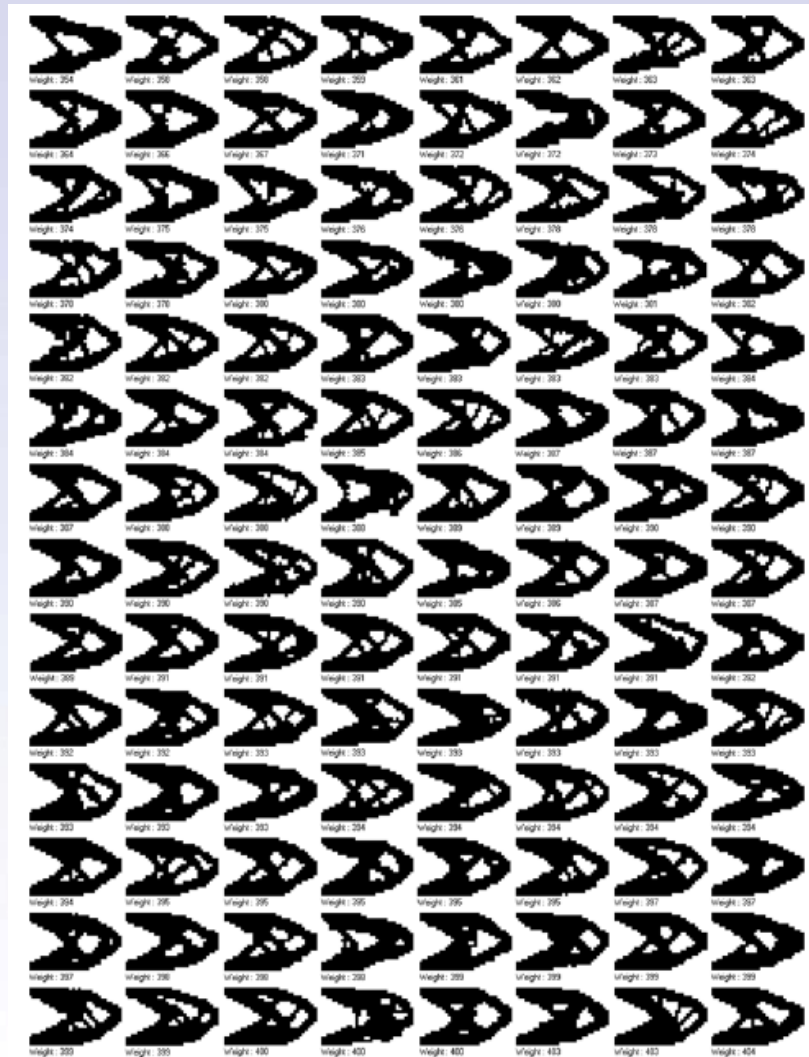
$$X_i^{k+1} = X_i^k \oplus V_i^{k+1}$$

\otimes (AND)

\oplus (XOR)

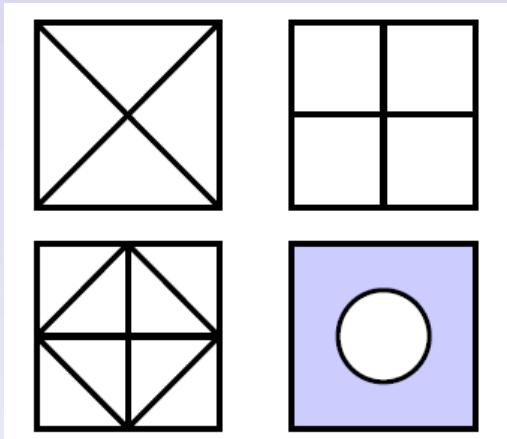
❖ Geometry Optimization – how

❖ Particle Swarm Optimization – example results

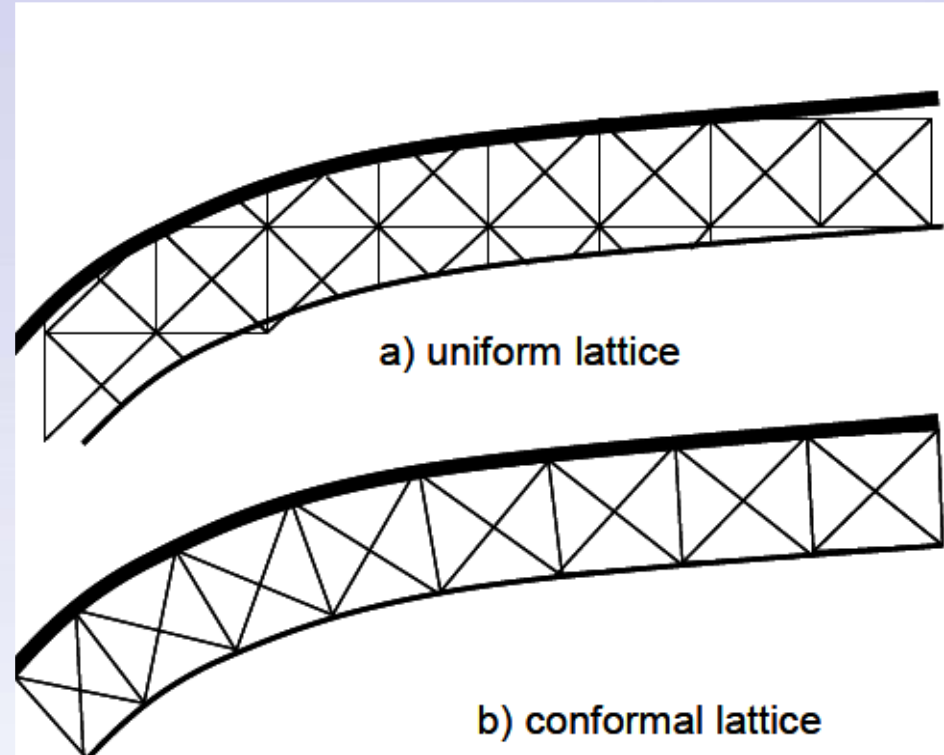


❖ Geometry Optimization – how

❖ Cellular structure



Cell types



a) uniform lattice

b) conformal lattice

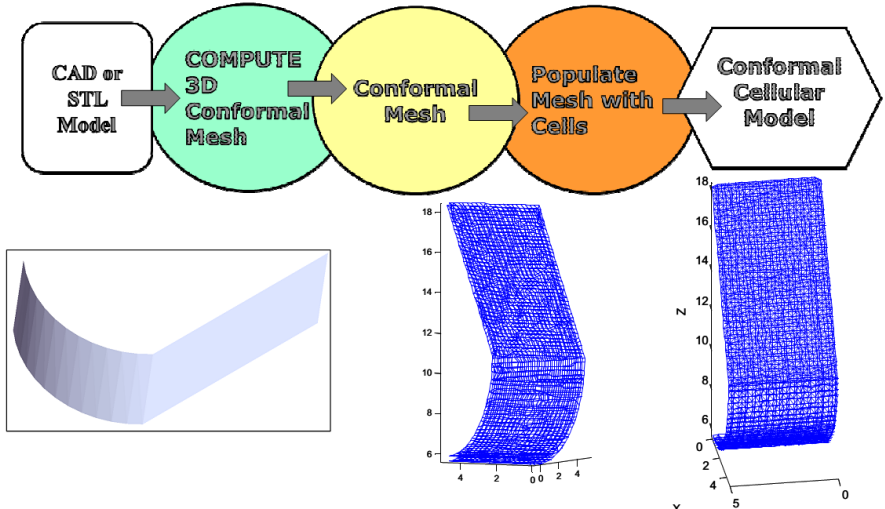
Ground structures

Topology optimization  **Size optimization**

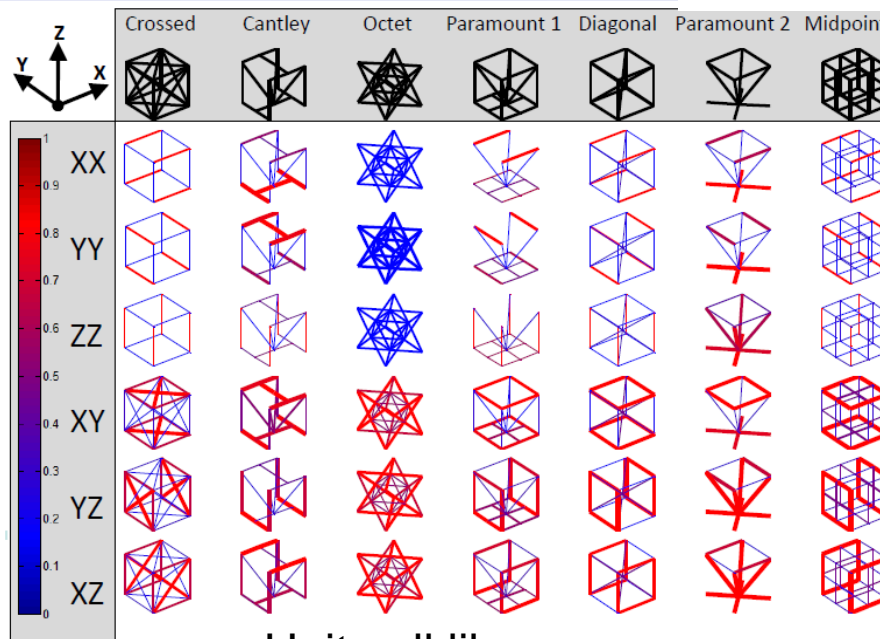
❖ Geometry Optimization – how

❖ Cellular structure

Credit: Jason Nguyen MS thesis



Generate ground structure

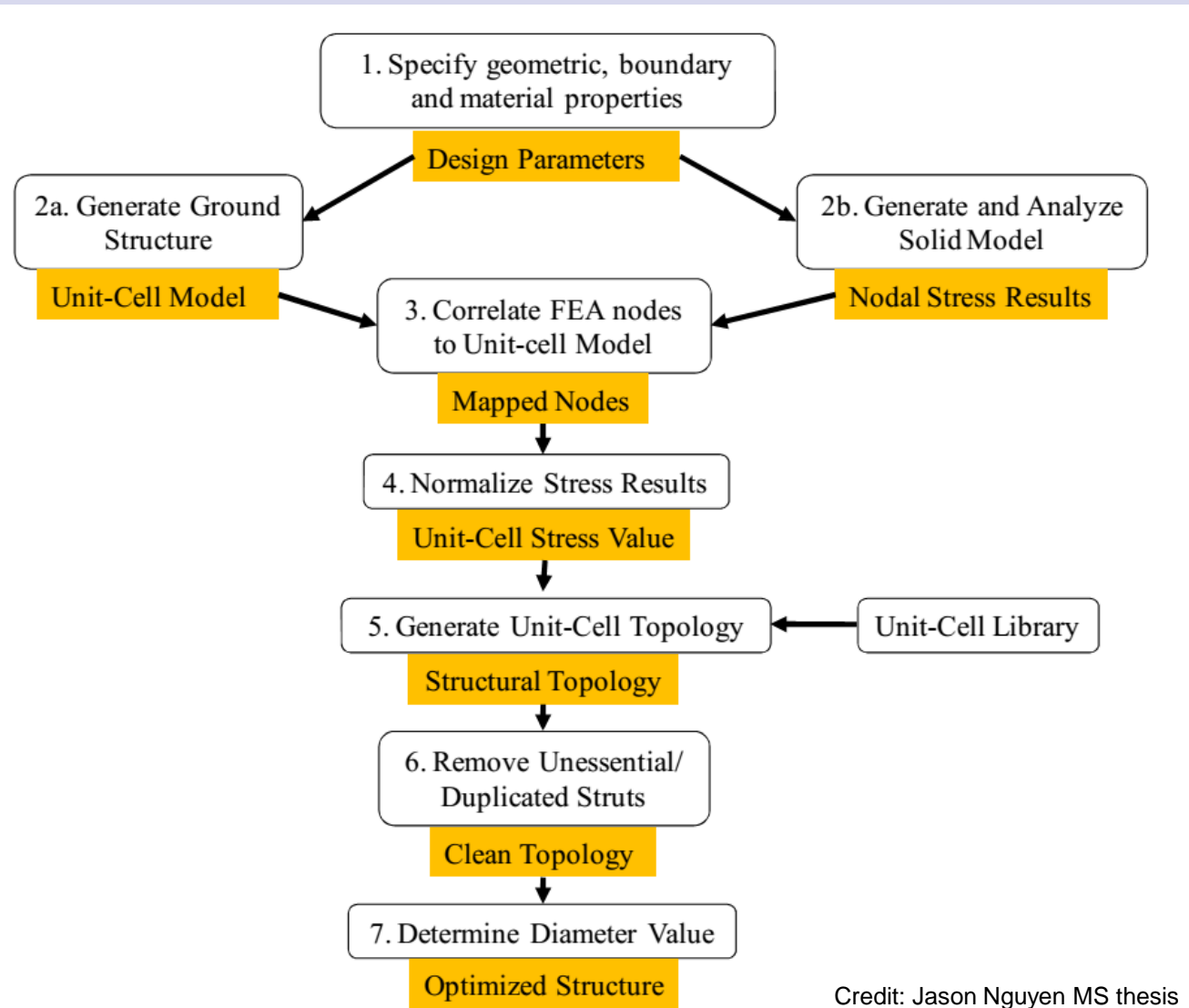


Unit cell library

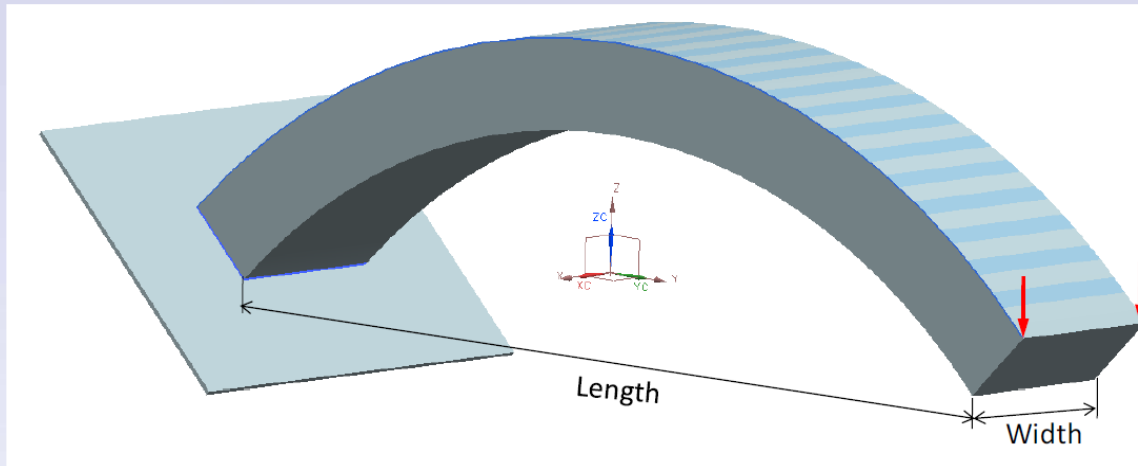
Credit: Patrick Chang MS thesis

❖ Geometry Optimization – how

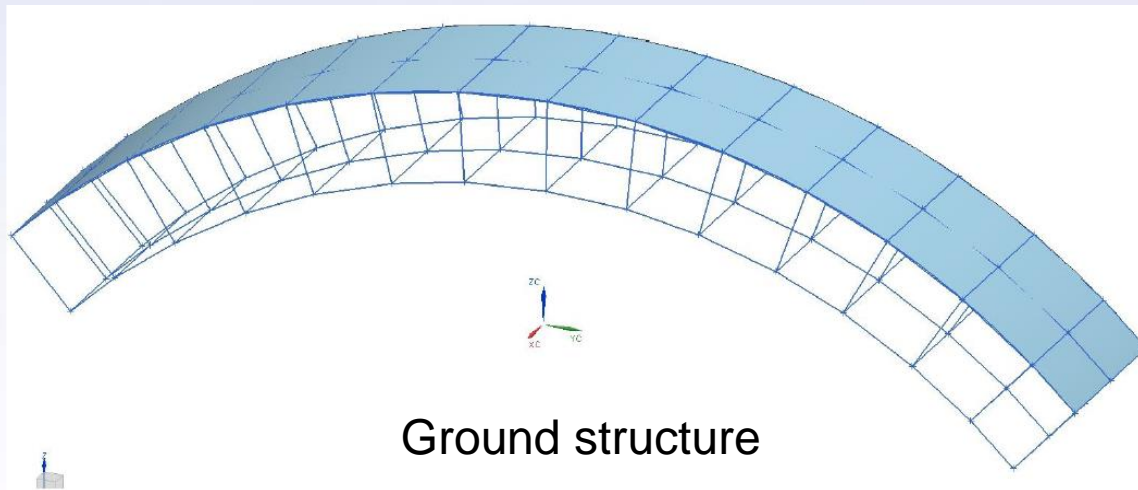
❖ Cellular structure



❖ Geometry Optimization – how ❖ Cellular structure

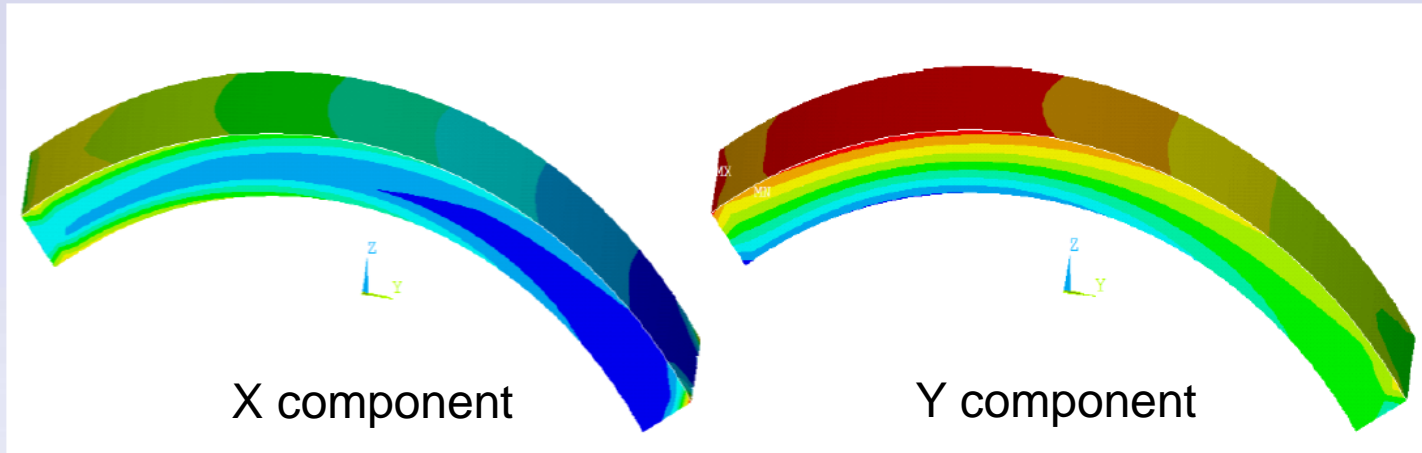


Problem

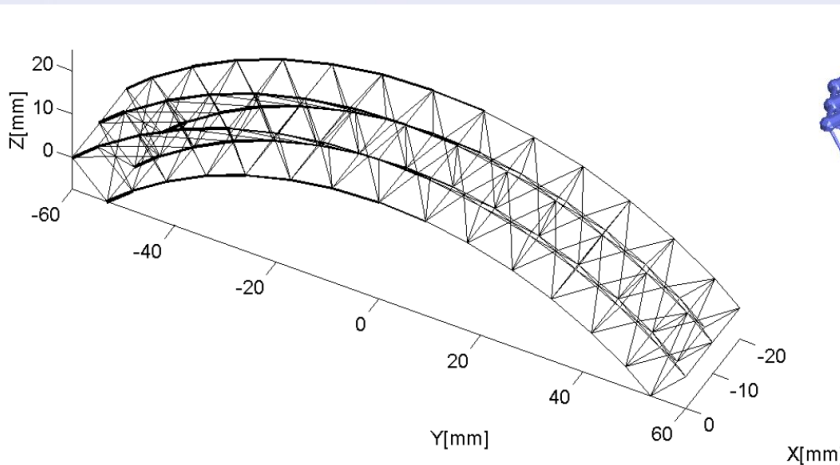


Ground structure

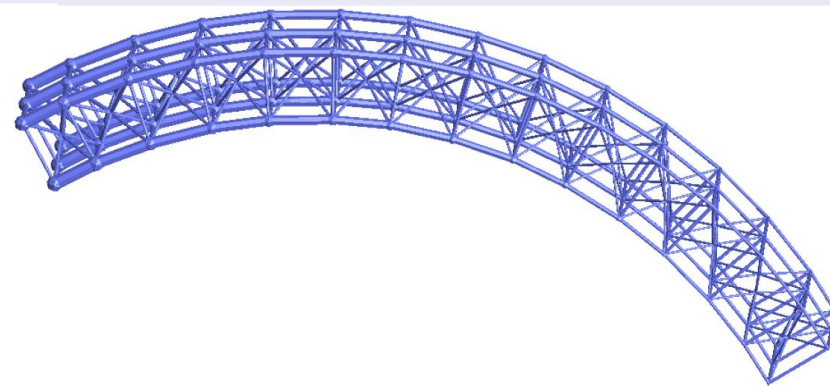
❖ Geometry Optimization – how ❖ Cellular structure



Solid body analysis



Scaling and mapping with unit cell



Final topology

Material design

Design

Optimization

Geometry

Materials

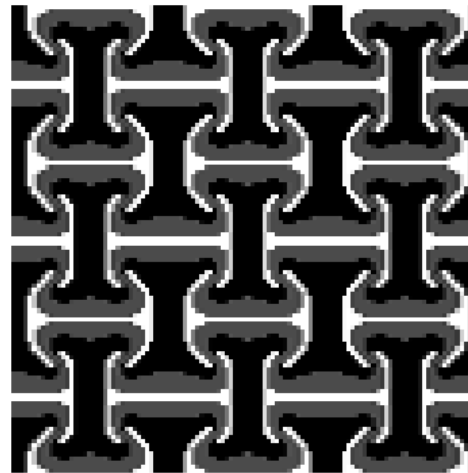


Multi-material 3D printers: Objet Connex (inkjet)

Material design



(a) Unit cell mesh 40×40



(b) Array 3×3

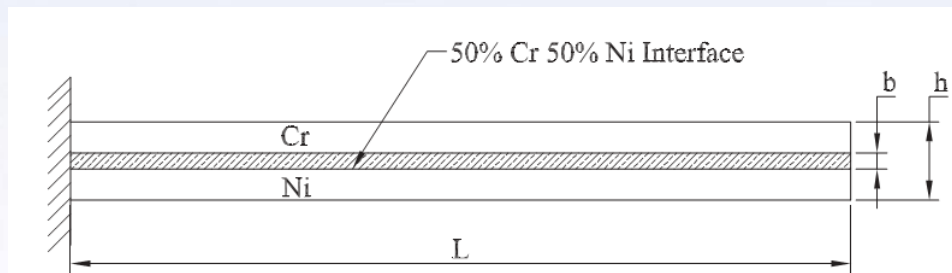
Designed material microstructure that has negative thermal expansion coefficient using homogenization method

- ◆ Mat 1: $E = 1$; $\nu = 0.3$; $\alpha = 1$
- ◆ Mat 2: $E = 1$; $\nu = 0.3$; $\alpha = 10$
- ◆ Mat 3: Void ($E = 1e-4$)

Homogenized property

$$\mathbf{E}^H = 0.01 \begin{bmatrix} 3.51 & -0.59 & 0 \\ -0.59 & 4.85 & 0 \\ 0 & 0 & 0.96 \end{bmatrix},$$

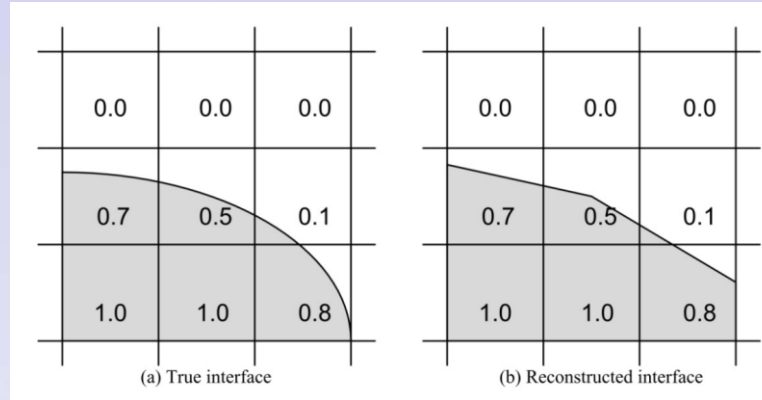
$$\boldsymbol{\alpha}^H = \begin{bmatrix} -6.276 & 0 \\ 0 & -6.529 \end{bmatrix}.$$



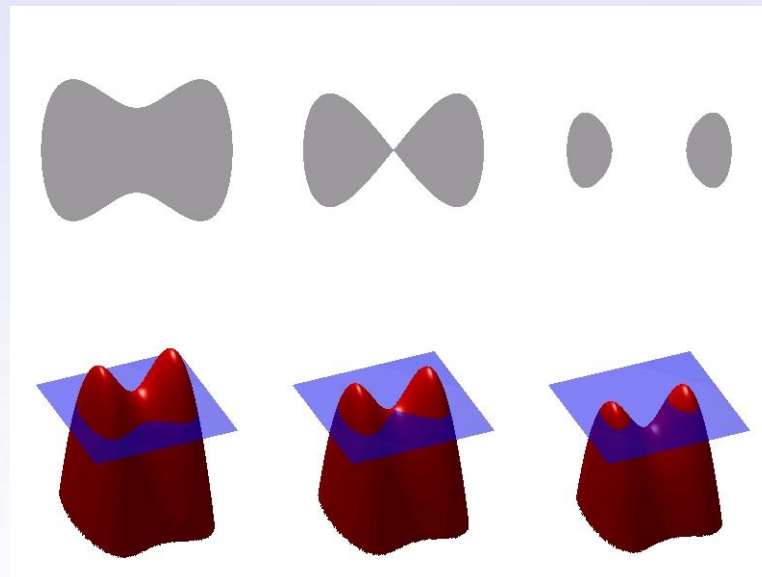
Qi, H., N. Kikuchi, and J. Mazumder. "Interface study and boundary smoothing on designed composite material microstructures for manufacturing purposes." *Structural and multidisciplinary Optimization* 26.5 (2004): 326-332.

Interface has energy: need to consider interface thickness for homogenization method

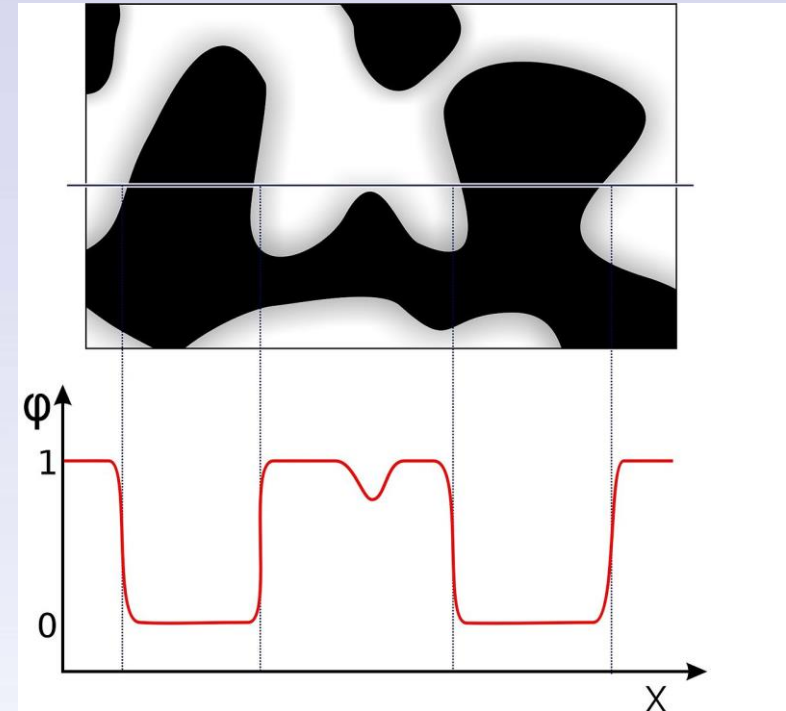
Material design – interface modeling



Volume of Fraction



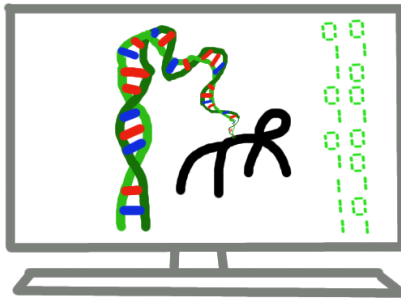
Level-set method



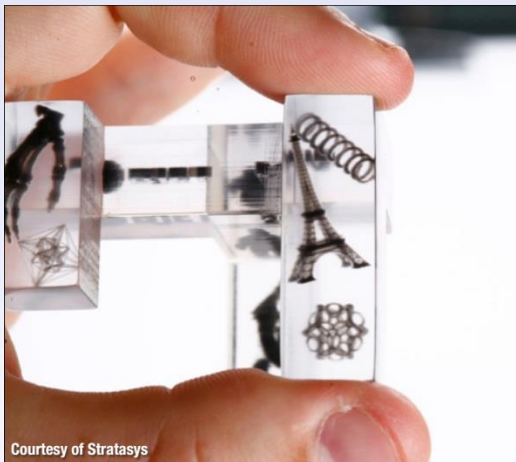
Phase-field method

Refer to Zhou, Wenchao. "Interface dynamics in inkjet deposition." (2014).chapter 2 for more details

Material design

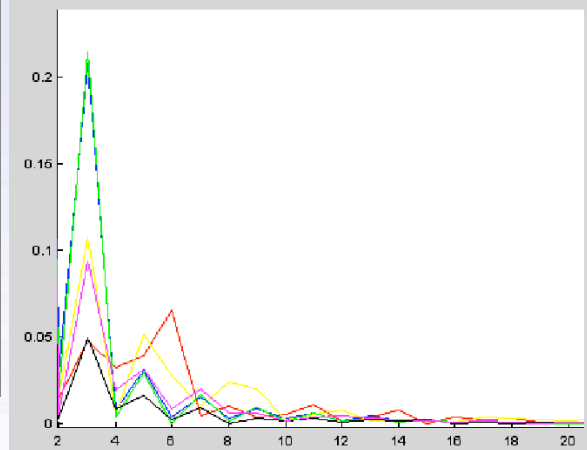
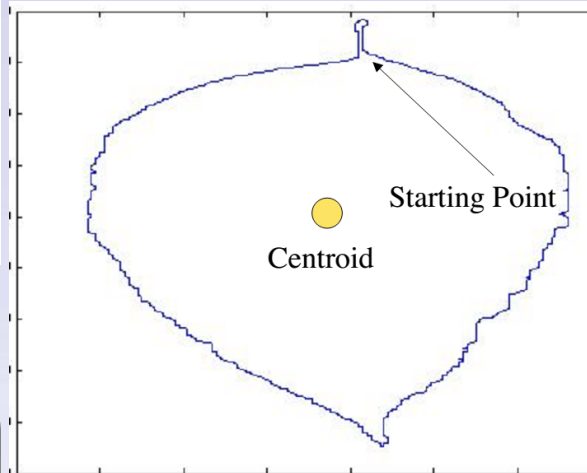


Genetic algorithm for
multi-material design

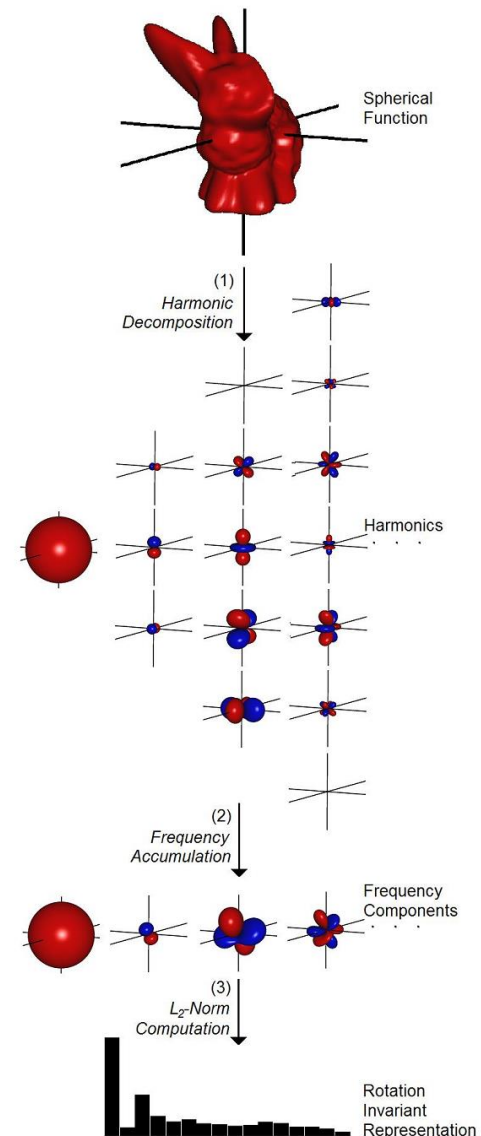


High resolution: 600dpi
~10⁸ voxels per cubic inch

Other encoding techniques



Fourier descriptor

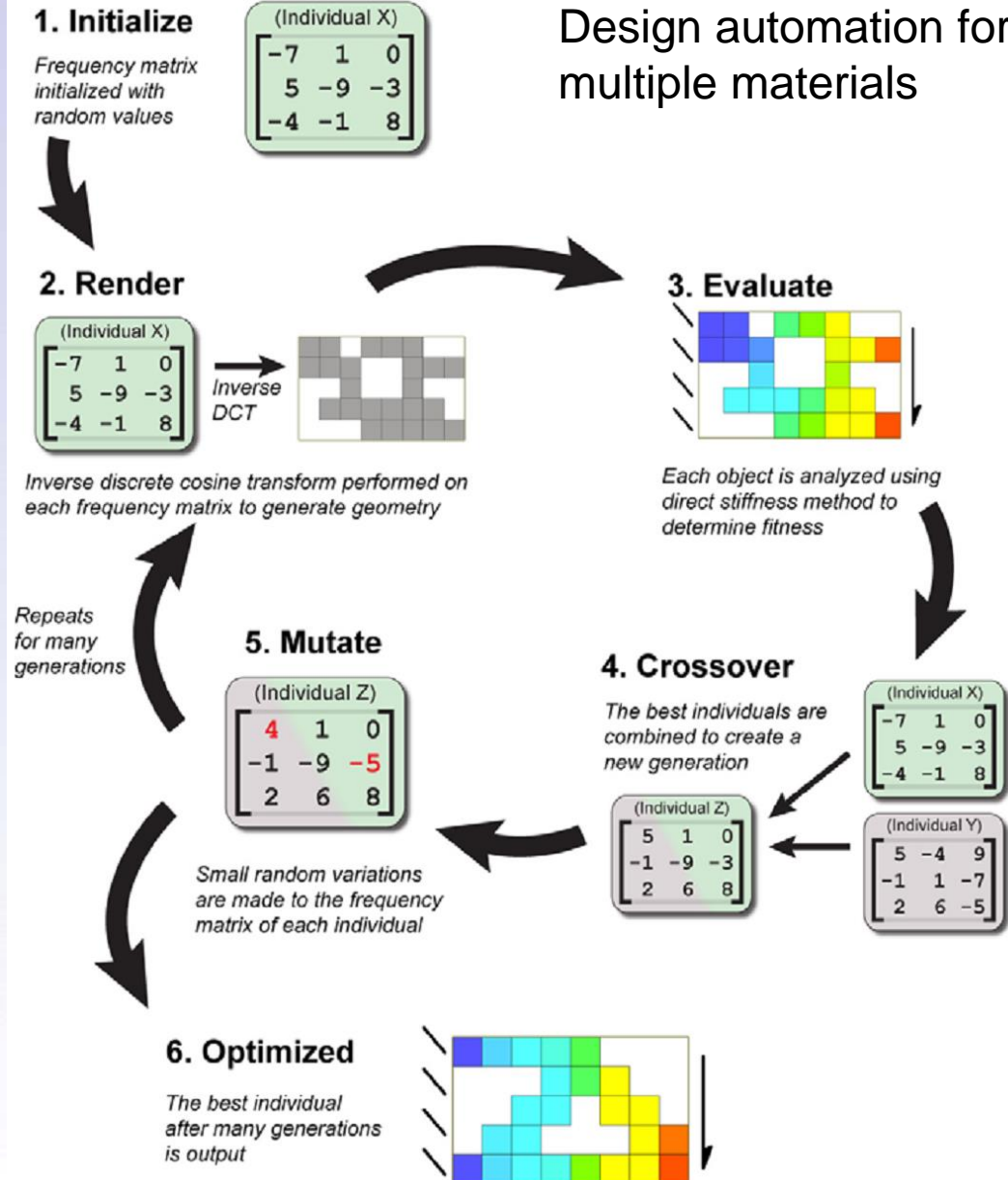


Spherical harmonics

Refer to Zhou, Wenchao. "Interface dynamics in inkjet deposition."
(2014).chapter 2 for more details

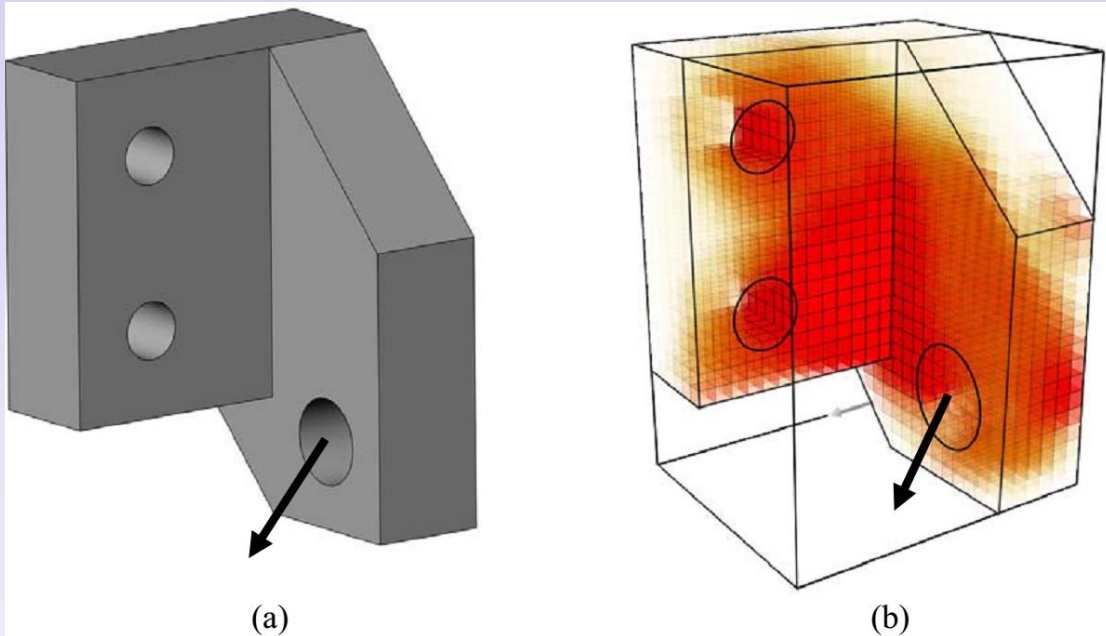
Material design

Design automation for multiple materials



Hiller, Jonathan D., and Hod Lipson.
"Design automation for multi-material
printing." *20th Annual International
Solid Freeform Fabrication Symposium*,
Austin, TX, Aug. 2009.

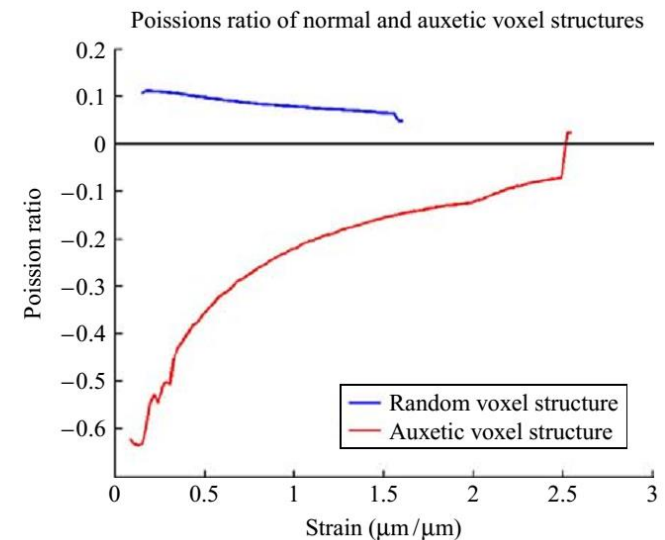
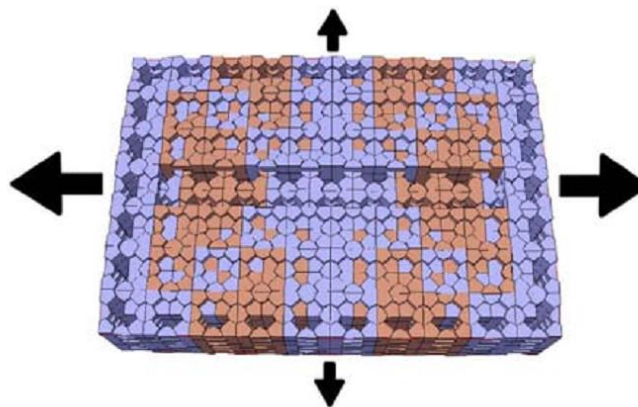
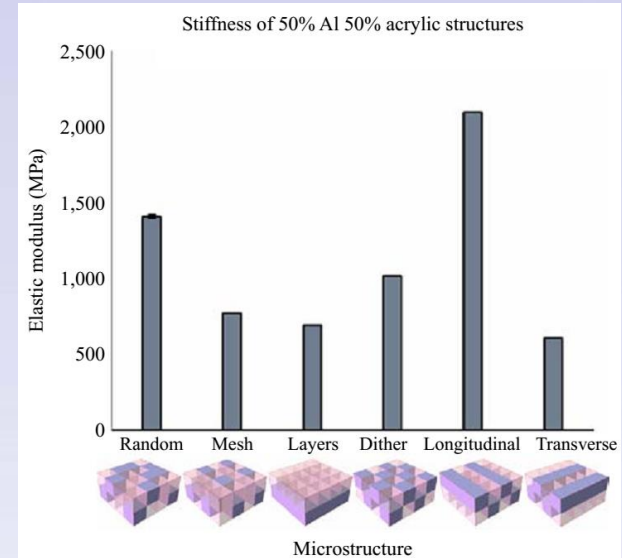
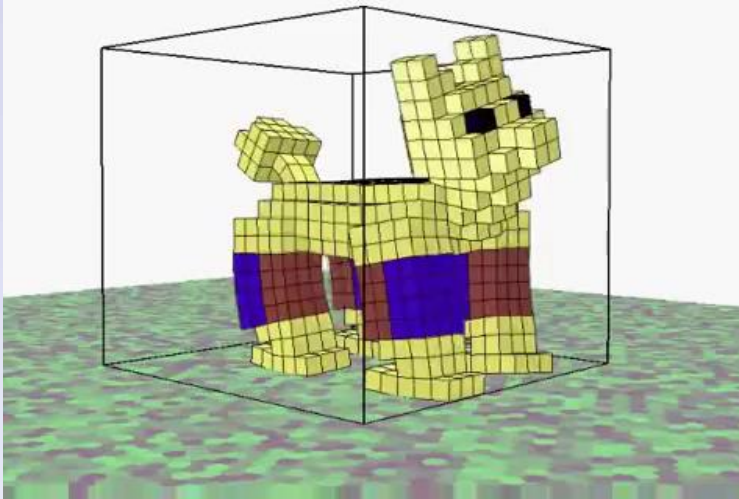
Material design



The design automation algorithm optimizes the internal material distribution of a pre-designed bracket (a), in order to maximize stiffness and minimize weight. The results are shown in (b), where red represents stiff, dense material transitioning to transparent yellow, which represents flexible, lightweight material.

Material design – digital materials

<http://www.voxcad.com/>



Hiller, Jonathan, and Hod Lipson. "Tunable digital material properties for 3D voxel printers." Rapid Prototyping Journal 16.4 (2010): 241-247.

Figure 1.1 is a log-log plot of Young's modulus E (GPa) versus Density (g/cm³). The y-axis ranges from 10^{-4} to 1000 GPa, and the x-axis ranges from 10 to 10000 g/cm³. The plot is divided into several regions representing different material classes:

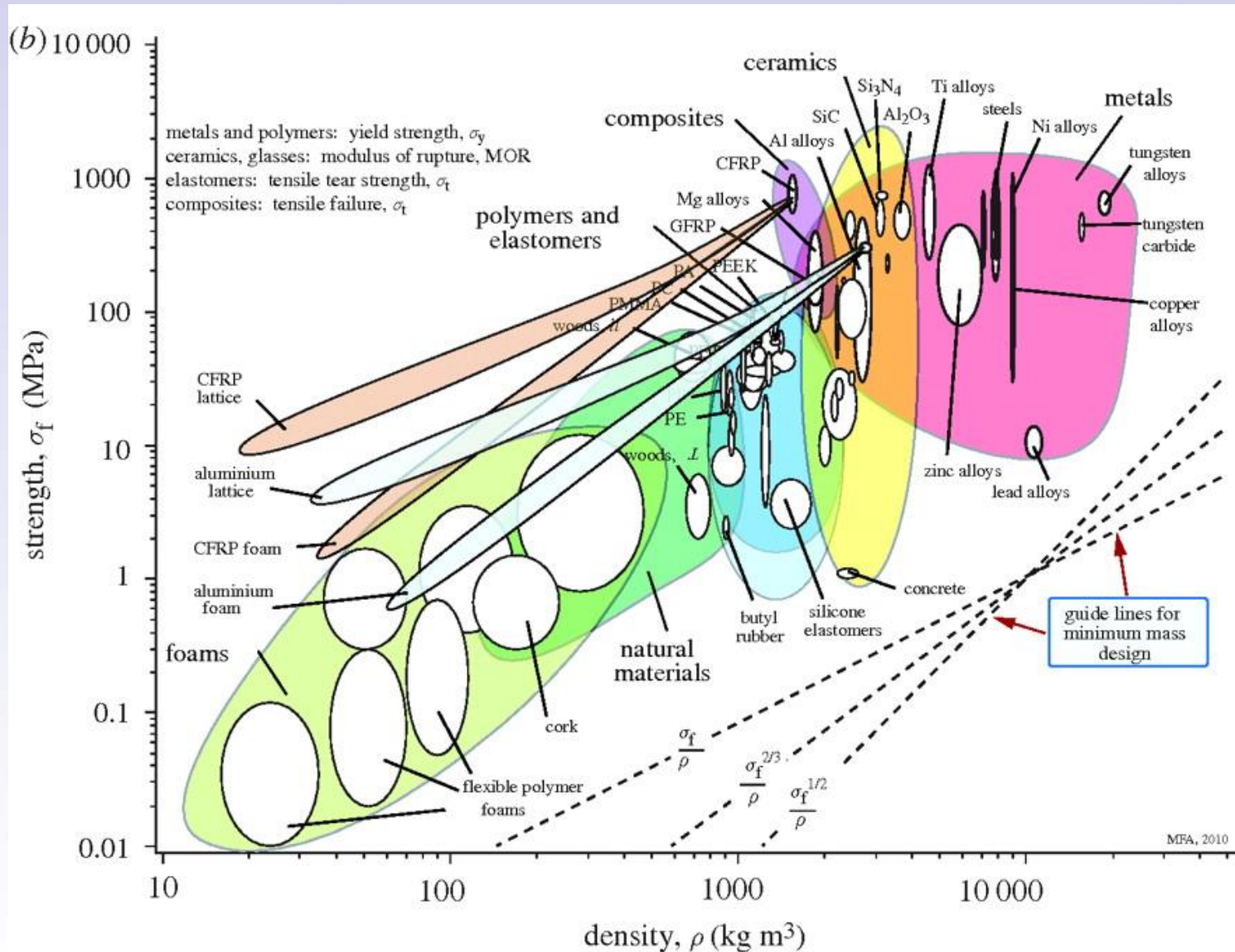
- Technical ceramics:** Located in the upper right, including materials like SiC, Al_2O_3 , steels, Ni alloys, WC, W alloys, Cu alloys, and lead alloys.
- Composites:** Located in the upper middle, including materials like B_4C , Si_3N_4 , Al alloys, CFRP, glass, Mg alloys, GFRP, bamboo, wood // grain, PMMA, PA, PS, wood (L grain), leather, and CFRP lattice.
- Metals:** Located in the upper right, including materials like steels, Ni alloys, WC, W alloys, Cu alloys, lead alloys, zinc alloys, and PEEK.
- Non-technical ceramics:** Located in the middle right, including materials like PEEK, epoxies, PC, PTFE, PET, PE, EVA, silicone elastomers, polyurethane, neoprene, butyl rubber, isoprene, cork, leather, wood, bamboo, glass, CFRP, PMMA, PA, PS, wood (L grain), leather, and CFRP lattice.
- Polymers:** Located in the middle right, including materials like PEEK, epoxies, PC, PTFE, PET, PE, EVA, silicone elastomers, polyurethane, neoprene, butyl rubber, isoprene, cork, leather, wood, bamboo, glass, CFRP, PMMA, PA, PS, wood (L grain), leather, and CFRP lattice.
- Foams:** Located in the lower left, including materials like aluminium lattice, CFRP foam, aluminium foam, and flexible polymer foams.
- Natural materials:** Located in the lower middle, including materials like cork, leather, wood, bamboo, glass, CFRP, PMMA, PA, PS, wood (L grain), leather, and CFRP lattice.

Three dashed lines represent guide lines for minimum mass design:

- $E/\rho^{1/3}$
- $E/\rho^{1/2}$
- E/ρ

A red arrow points to the $E/\rho^{1/2}$ line, labeled "guide lines for minimum mass design".

Material design – digital materials



❖ Material design – how to fabricate

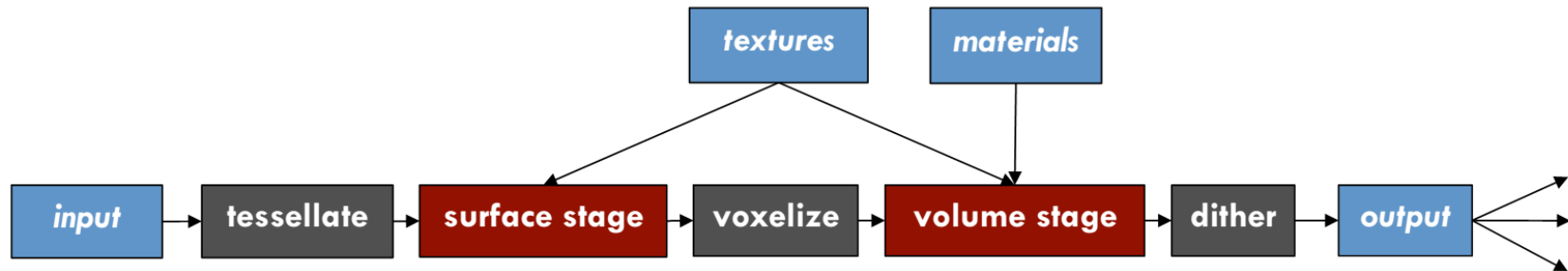
❖ File Format – AMF

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  <metadata type="author">John Smith</metadata>
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  </material>
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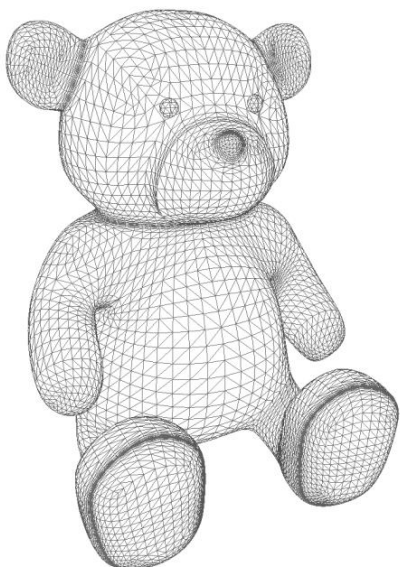
- ❖ Additive Manufacturing File
- ❖ ISO/ASTM Standard, 2011
- ❖ Machine independent (no layer or process information)
- ❖ XML-based format
 - ❖ <object>: volume of materials
 - ❖ <material>
 - ❖ <texture>
 - ❖ <metadata>
 - ❖ ...

❖ Material design – how to fabricate

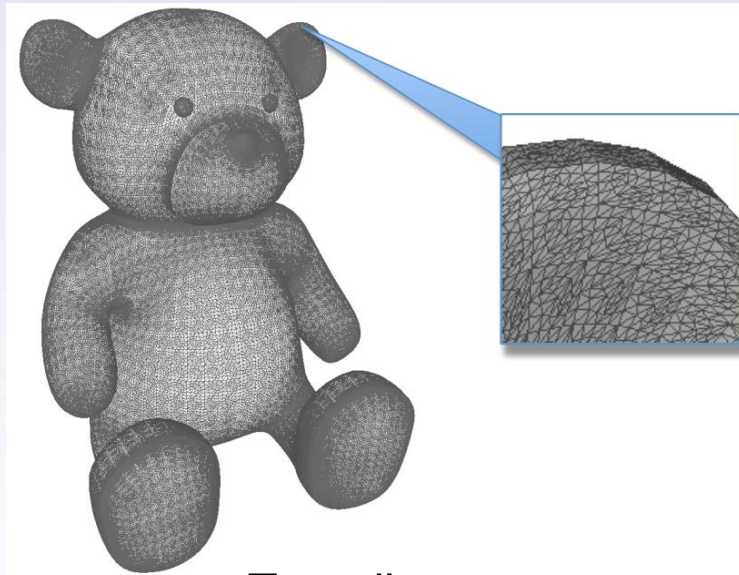
❖ The OpenFab Programming Model



To deal with large memory storage and computational cost, use pipeline (similar to streaming), that is “Not process all at one time”. Key – Local computation



Input



Tessellate

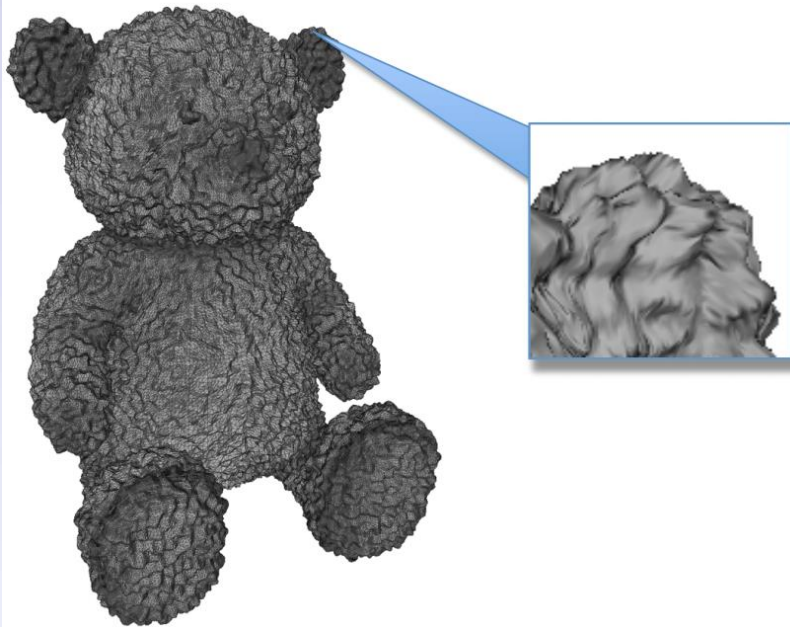
❖ Material design – how to fabricate ❖ The OpenFab Programming Model

Design

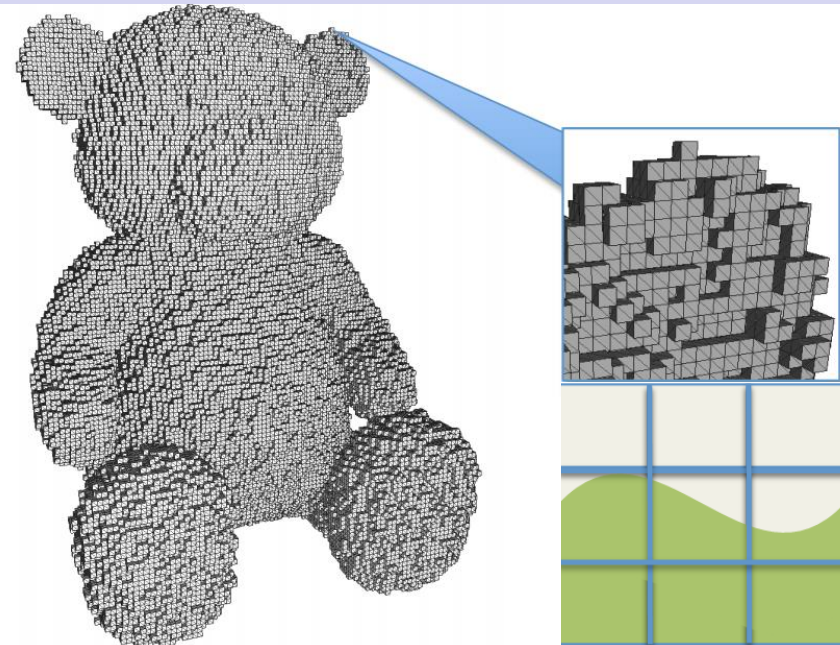
Optimization

Geometry

Materials



Surface stage: allow inputs (e.g., texture)



Voxelization

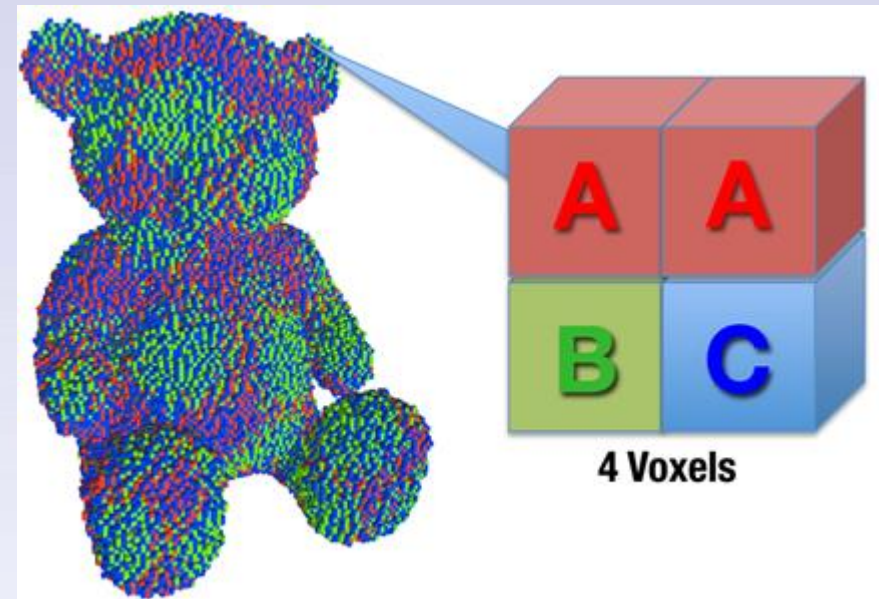
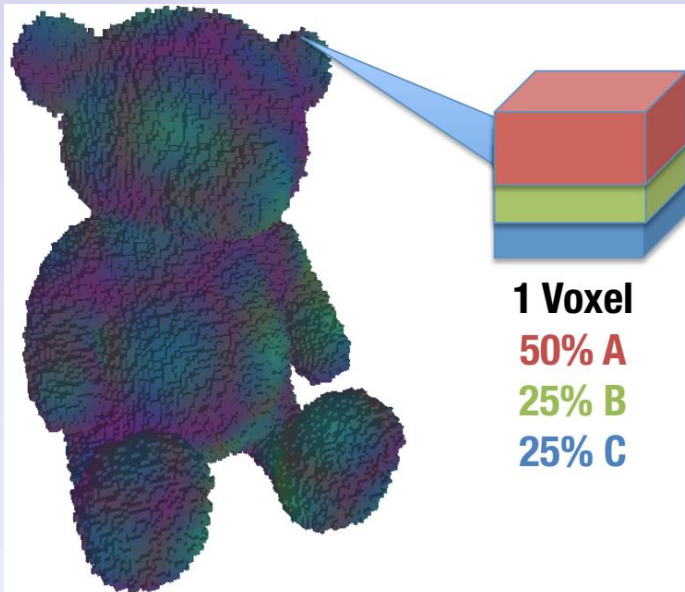
- ❖ Material design – how to fabricate
- ❖ The OpenFab Programming Model

Design

Optimization

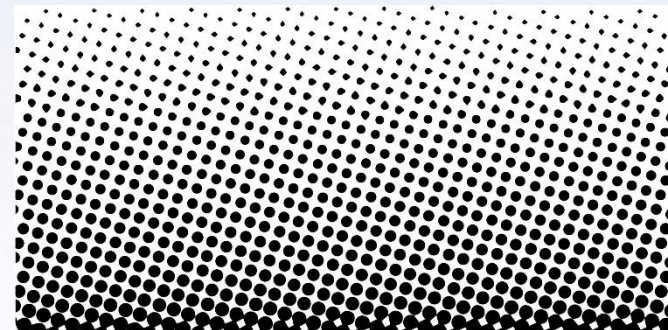
Geometry

Materials



Volume stage: allow inputs (e.g., materials)

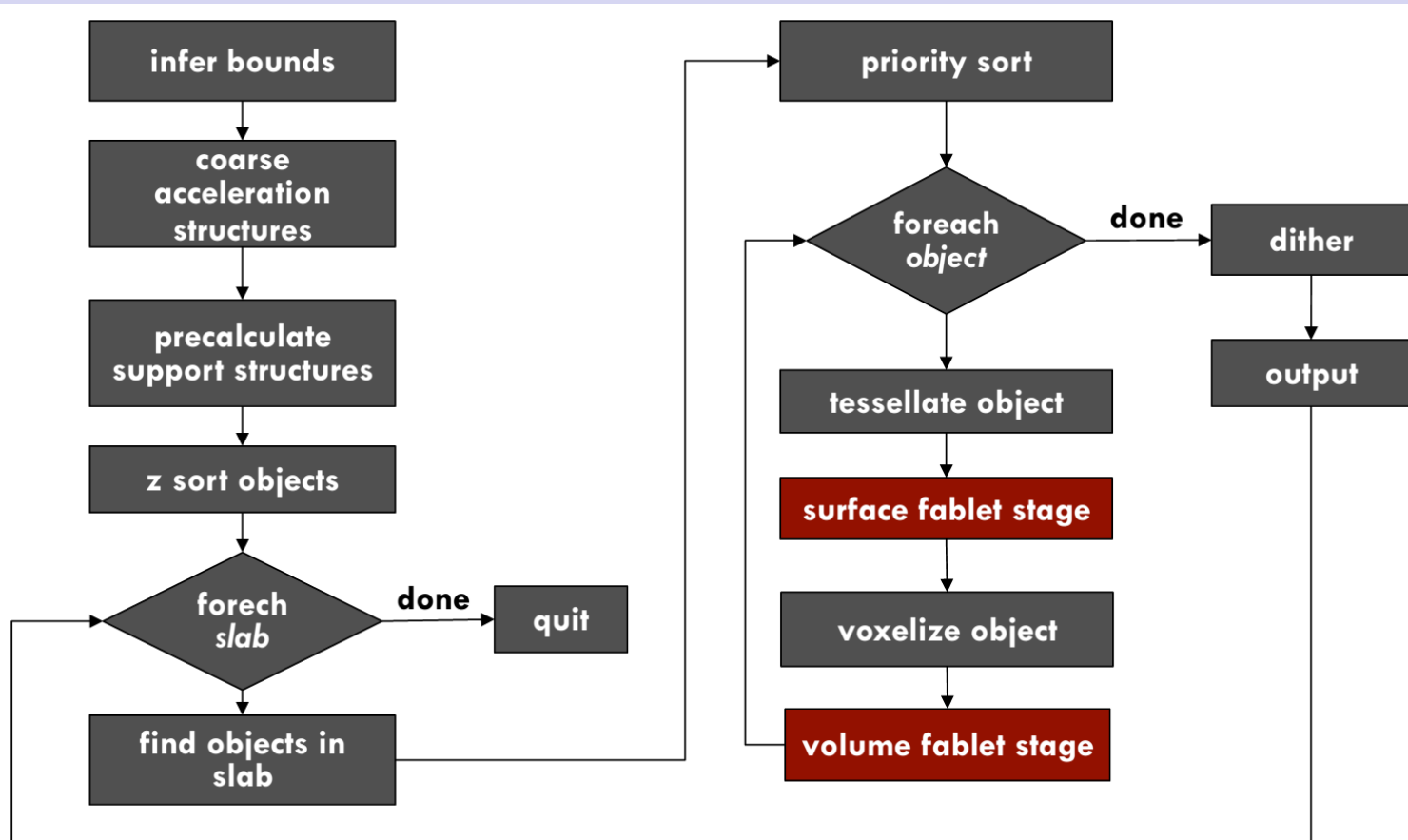
Dither



Halftoning

❖ Material design – how to fabricate

❖ The OpenFab Programming Model



❖ Material design

One material part



Opportunities

- ❖ How to automate design and optimization structures with multiple materials for non-natural properties
- ❖ How to evaluate complex multi-material structure (multiphase, interface modeling)
- ❖ How to add multi-material functionality to 3D printer (i.e., model with material information and generate machine instructions with material information)
- ❖ How to add more functionality to the structure using multiple materials

Design

Optimization

Geometry

Materials

