

# Learned Impatience? Dispersed Reinforcement and Time Discounting

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David Poensgen (Goethe University Frankfurt)

February 22, 2019

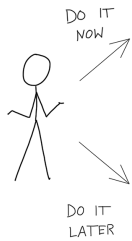
Sloan-Nomis Workshop on the Cognitive Foundations of Economic Behavior

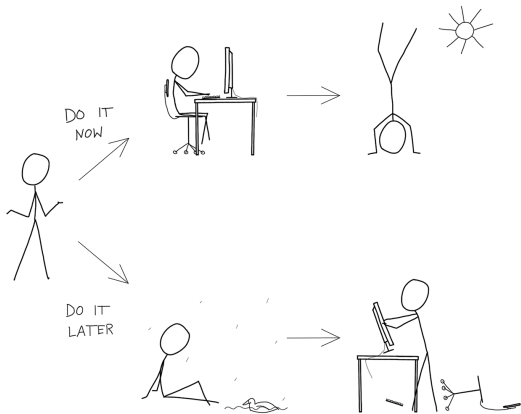
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2. Actions often have a series of consequences: some follow soon, some later.
3. How does this ordering affect learning?  
Plausibly: Easiest to learn from soonest consequences.
4. Then: Immediate consequences will be over-weighted.  
Behavior biased towards impatience.

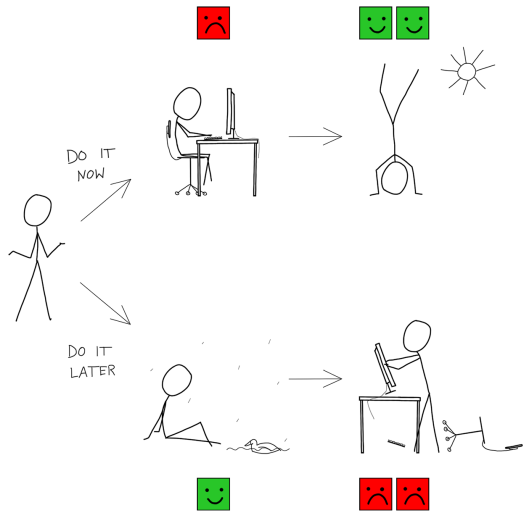
May help explain why myopic behavior is so widespread and persistent.

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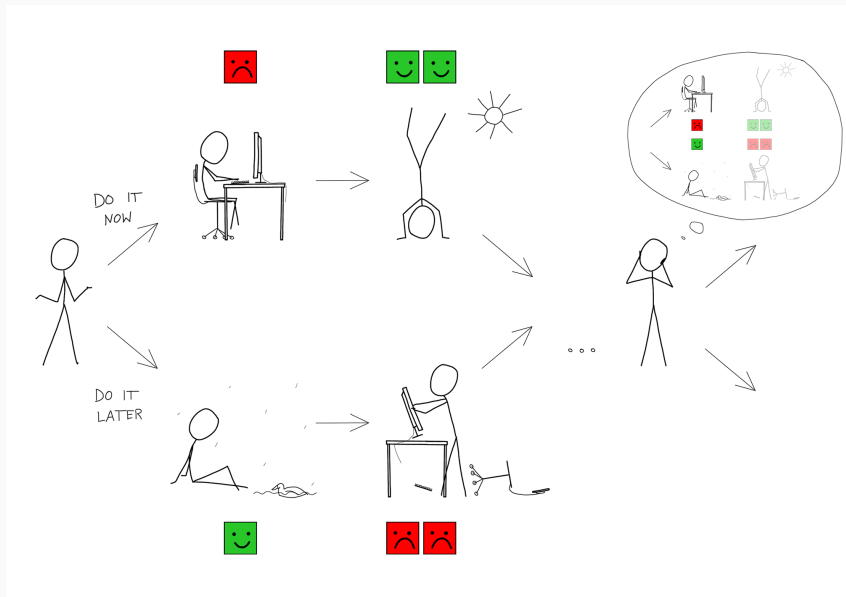
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## Background

- Decreasing effectiveness of reinforcement with delay (e.g. MAZUR 2002).
  - Typically not connected to time discounting, but speed of learning.
- Explained via accumulation of noise by COMMONS, WOODFORD ET AL. (1982, 1991).
- Feedback delay modulates neural circuitries involved in learning (FOERDE/SHOHAMY 2011, FOERDE ET AL. 2013, ARBEL ET AL. 2017).
  - Associative learning tasks; singular feedback. Performance not affected.
- GABAIX & LAIBSON (2017) also link time discounting and information frictions.
  - Formally applicable here; different interpretation on source of noise.
- Melioration theory: Behavior guided by immediate, not overall reinforcement rate (HERRNSTEIN ET AL.).
  - Important experimental paradigm: “Harvard game” (Review: PRELEC 2014).
  - Critique by SIMS ET AL. (2013): Bayesian algorithms need 1000s of trials for solution. Melioration as rational response to task complexity.







## Design: Overview

- 6 abstract options (= colors): {  ,  ,  ,  ,  ,  }
- Subjects faced with sequence of 105 binary choices.
- Payoff and feedback mechanism:
  - Each color  $x$  associated with a payoff vector  $(x_1, x_2)$
  - Values initially unknown, but can be learned.
  - Choosing  $x$  has 2 consequences:
    - $x_1 + \epsilon$  points shown and awarded immediately.
    - $x_2 + \epsilon'$  points shown and awarded with one round delay.
  - $\epsilon, \epsilon'$  are disturbances drawn uniformly from  $\{1, 2, 3, 4\}$ .
  - Total value of  $x$  is  $x_1 + x_2$
- Goal: Collect as many points as possible.
  - All points rewarded simultaneously after the experiment.
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# Design: Example Screen

61 / 105  
Round

Current options:




Time




807  
Total points

Chosen last round:

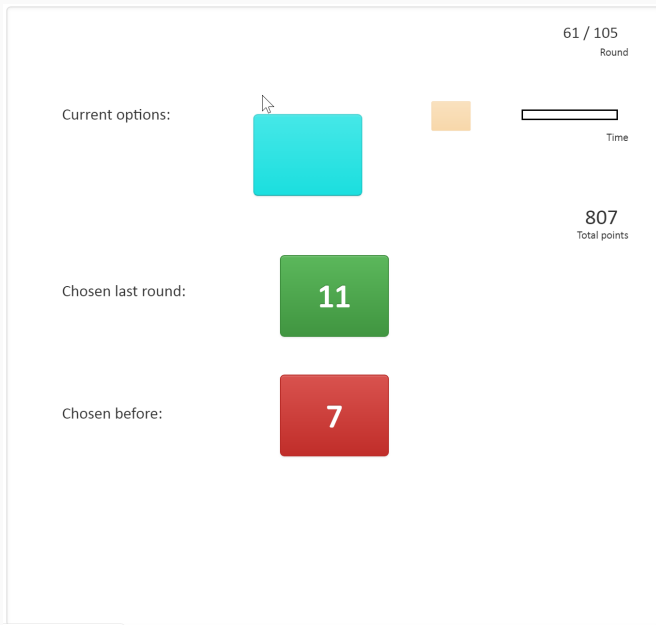


Chosen before:

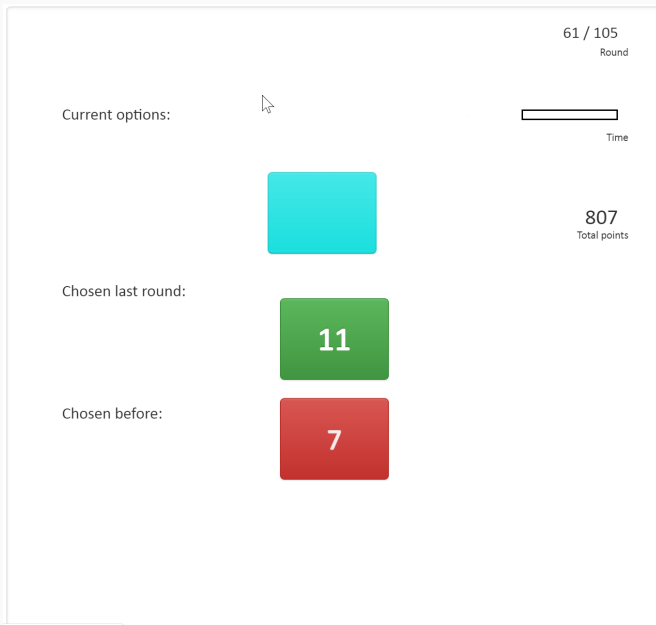




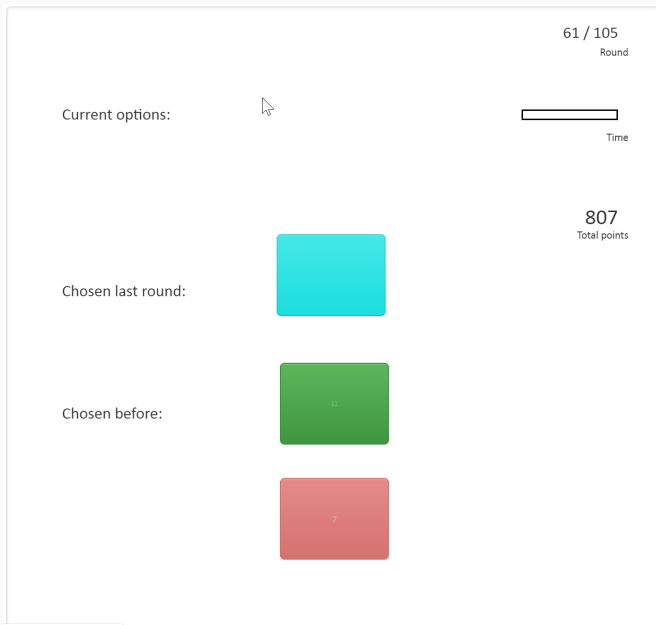
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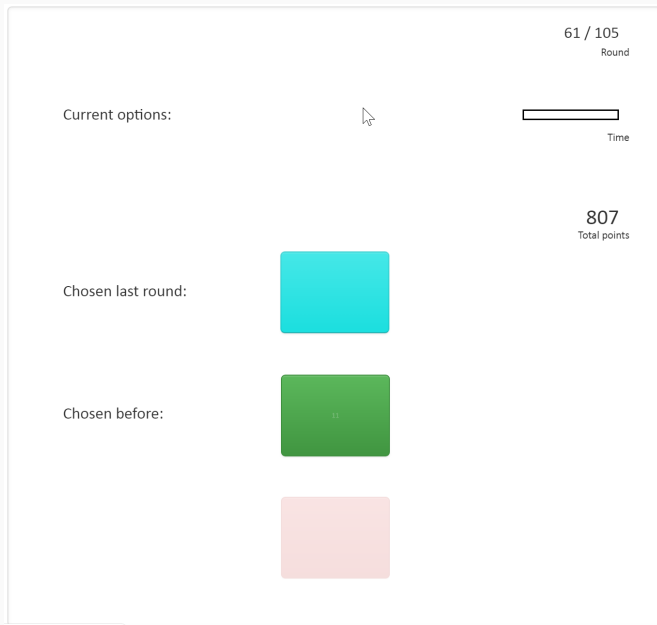
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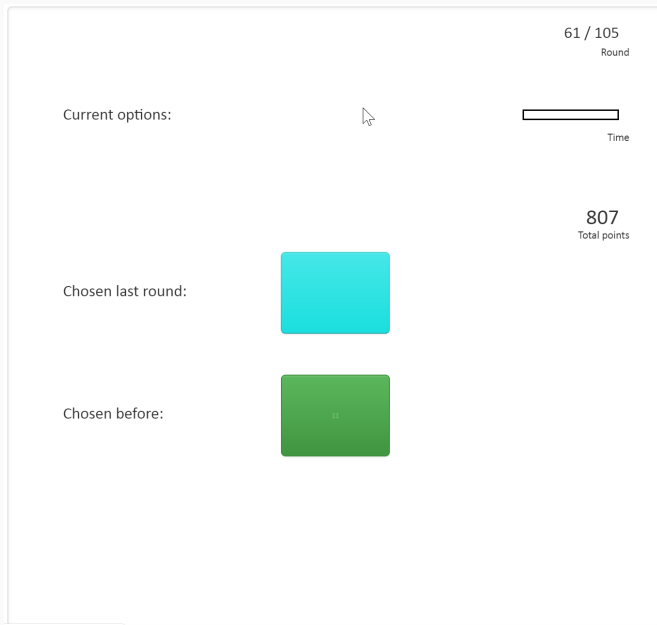
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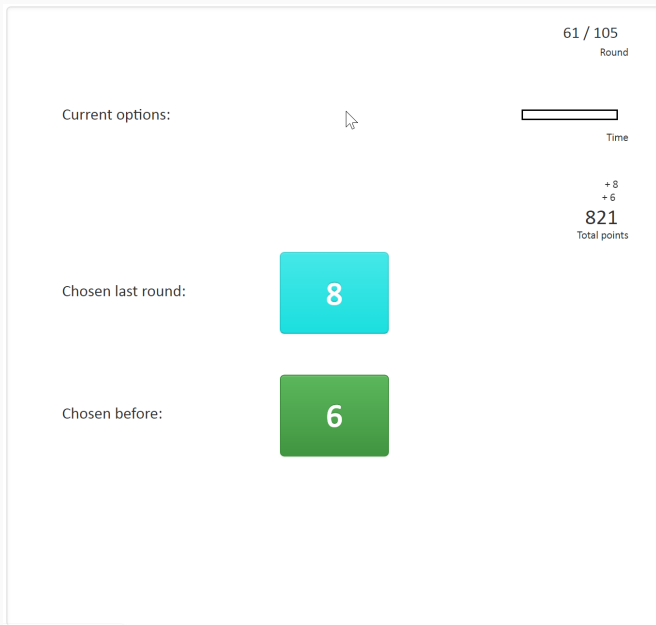
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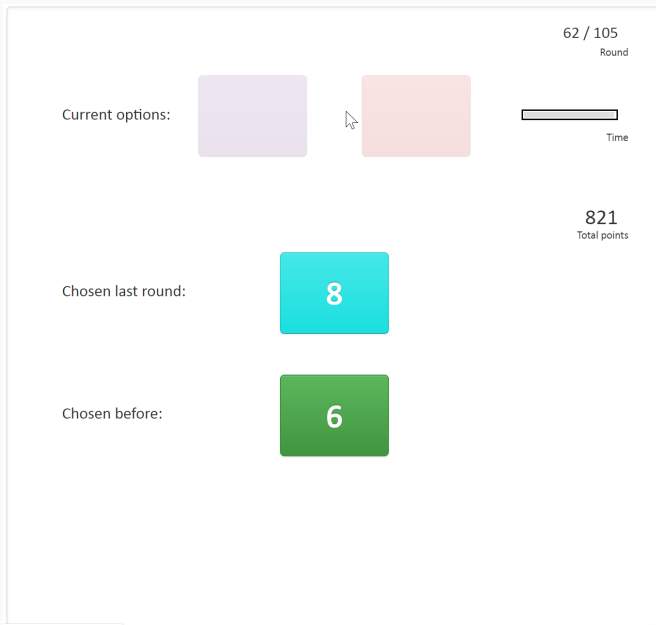
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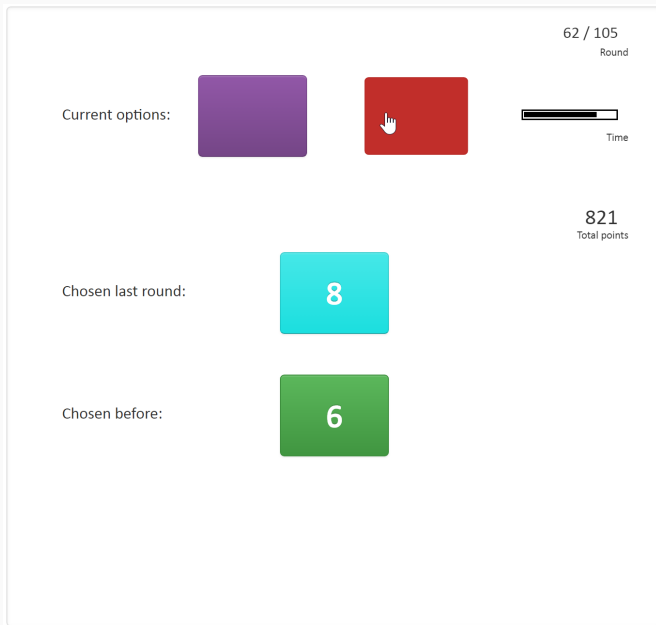
# Design: Example Screen

The screen displays a game interface with the following elements:

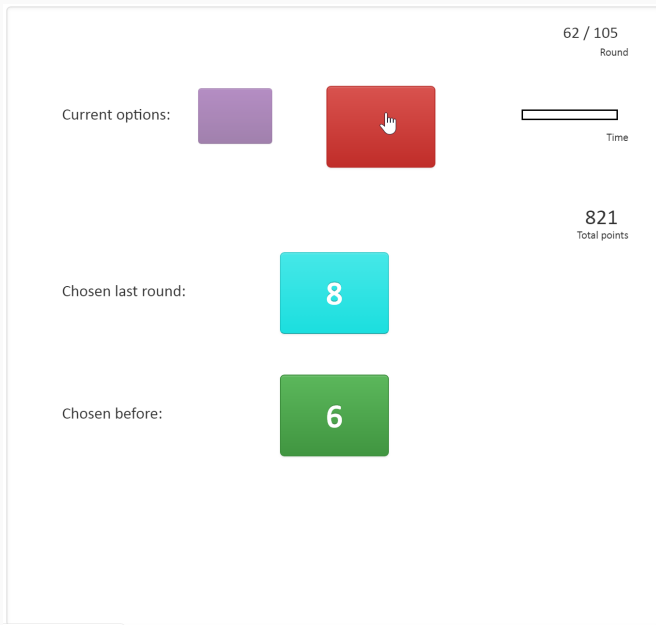
- Round:** 62 / 105
- Current options:** A purple square and a red square. A mouse cursor is hovering over the red square.
- Time:** A progress bar indicating the remaining time.
- Chosen last round:** A cyan square containing the number 8.
- Chosen before:** A green square containing the number 6.
- Total points:** 821



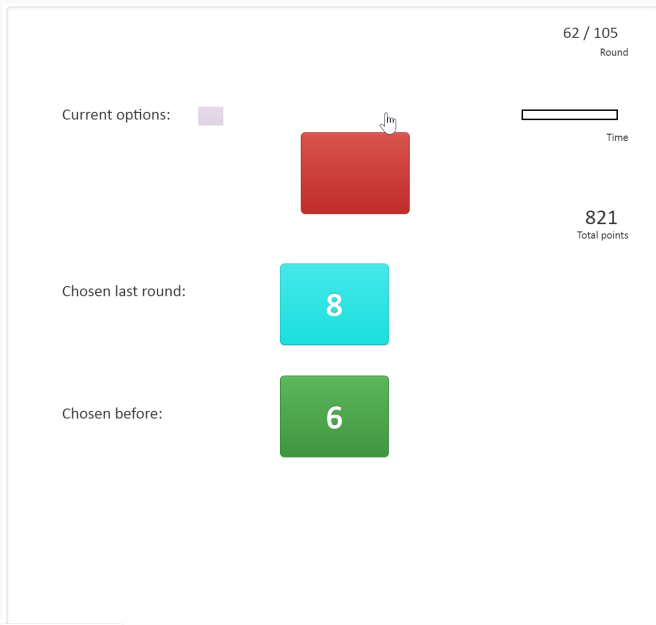
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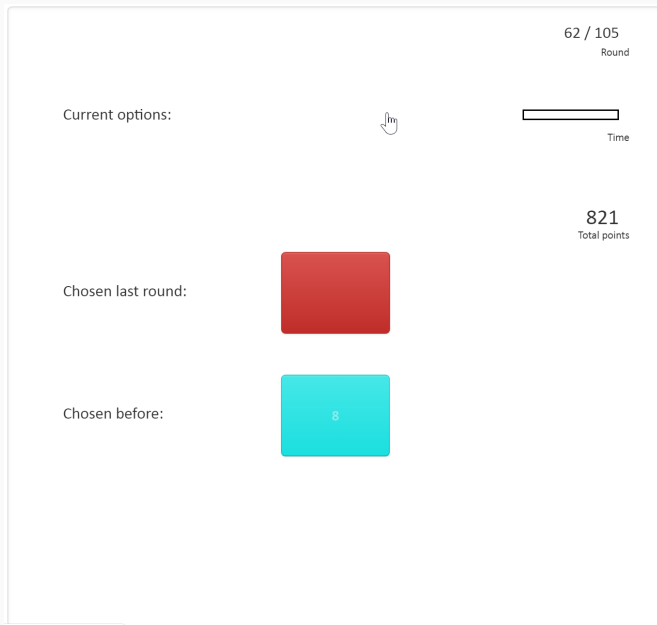
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# Design: Example Screen


62 / 105  
Round

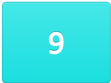
Current options: 

Time 

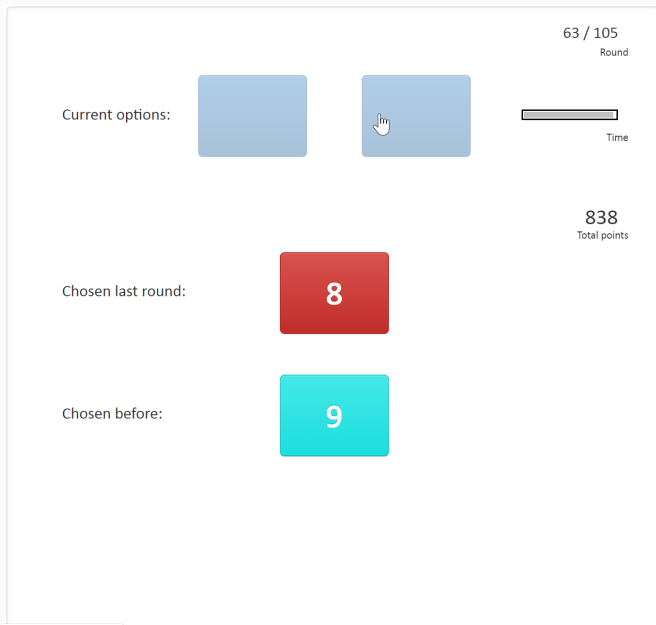
+ 8  
+ 9

838  
Total points

Chosen last round: 







Chosen before: 

# Design: Example Screen





## Design: Payoff Vectors







Option		Payoff Vectors	
color e.g.	(total value)	(immediate, delayed)	
	(18)	<b>Group A</b> (11, 7) <sub>A</sub>	<b>Group B</b> (7, 11) <sub>B</sub>
	(16)	(6, 10) <sub>A</sub>	(10, 6) <sub>B</sub>
	(14)	(9, 5) <sub>A</sub>	(5, 9) <sub>B</sub>
	(12)	(4, 8) <sub>A</sub>	(8, 4) <sub>B</sub>
	(10)	(7, 3) <sub>A</sub>	(3, 7) <sub>B</sub>
	(8)	(2, 6) <sub>A</sub>	(6, 2) <sub>B</sub>

Hypotheses: (11, 7)<sub>A</sub> chosen more often than (7, 11)<sub>B</sub>; (10, 6)<sub>B</sub> more than (6, 10)<sub>A</sub>; ...

(11, 7)<sub>A</sub> and (6, 10)<sub>A</sub> further apart than (6, 10)<sub>A</sub> and (9, 5)<sub>A</sub>.

Potentially even: (9, 5)<sub>A</sub> preferred to (6, 10)<sub>A</sub>.

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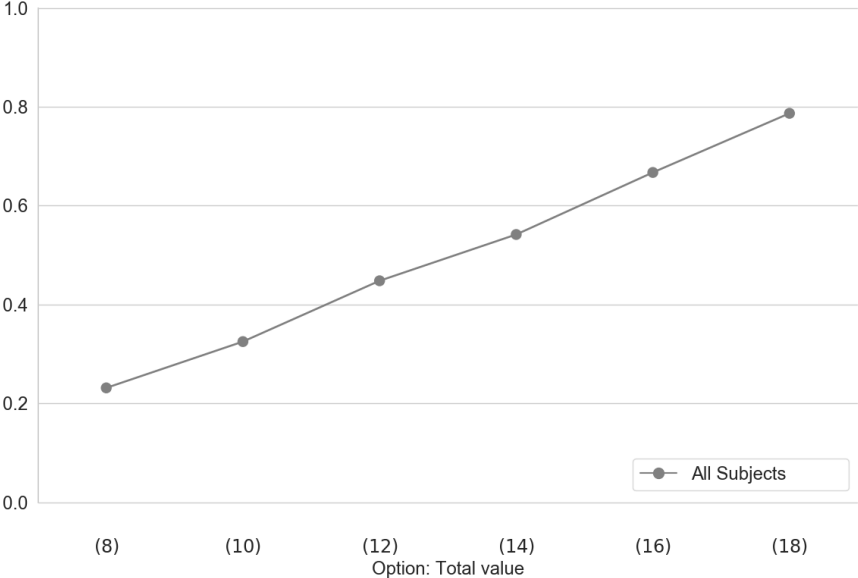
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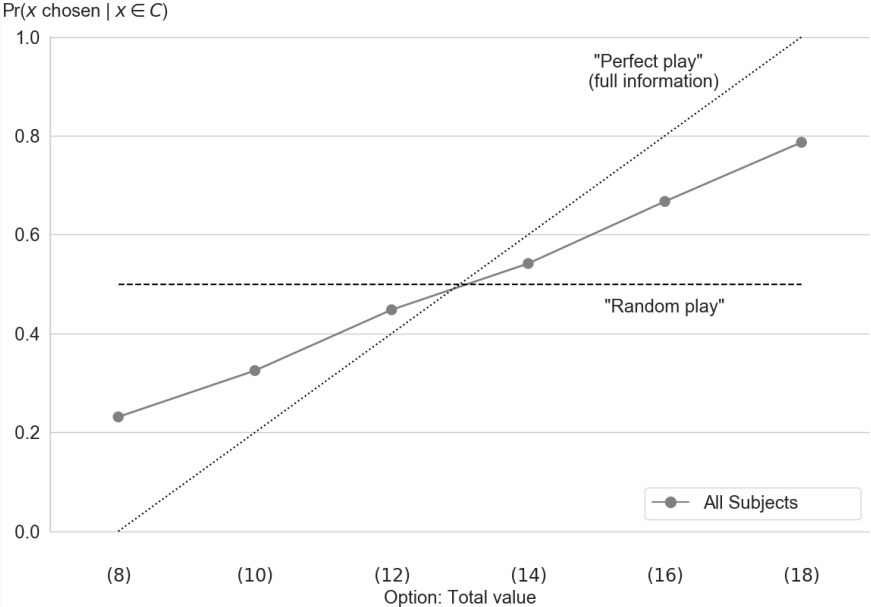
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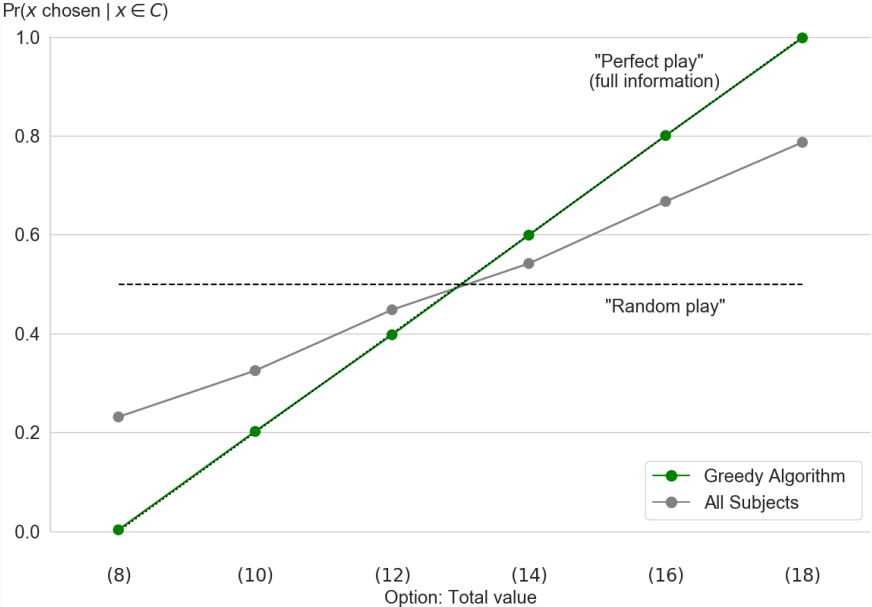
$\Pr(x \text{ chosen} \mid x \in C)$



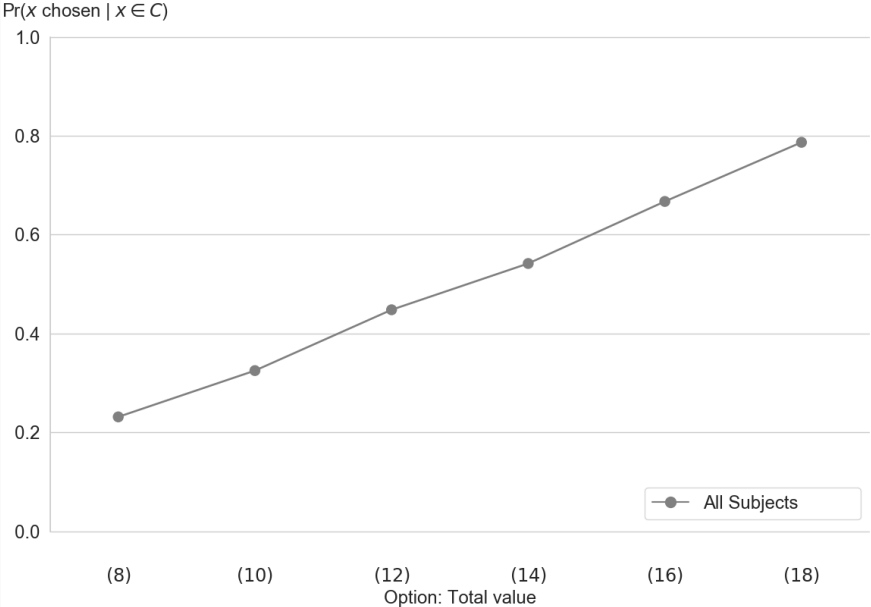
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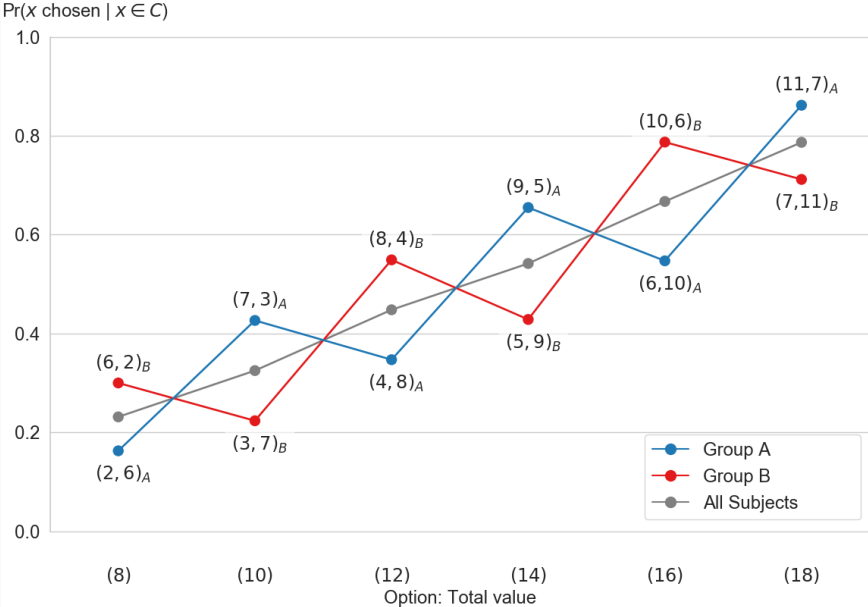
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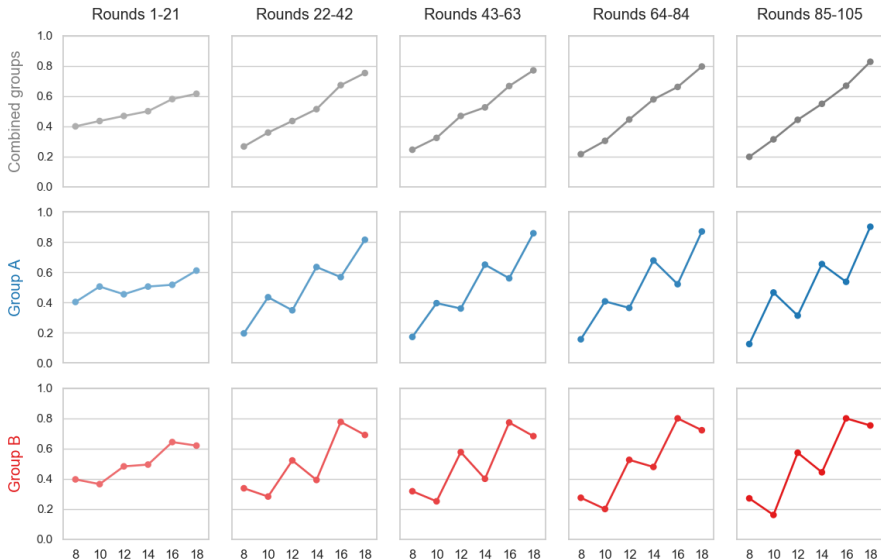
# Results: Choice Frequencies



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# Results: Bias over time





- Estimated latent utility function:  $u(x) = x_1 + 0.4x_2$
- Elicited beliefs are in accordance with choice behavior.
- Considerable heterogeneity in degree of biasedness.
  - Correlated to impatience in hypothetical intertemporal choice.
  - (To do: Incentivized choice or field measures of impatience.)
- Treatment: Learning by observation
  - Subjects passively presented with feedback for 63 rounds.
  - Directly afterwards: 42 own decisions.
  - Bias attenuated; low right after the learning phase, then gradually increasing.
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## Summary: Further Results

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- Relation to actual reward discounting – ideally with field measure
- Relation to working memory
  - known to affect reward discounting (WESLEY/BICKEL 2014)
- Potential explanation: Differential precision in memory
- Investigate this using...
  - response time data
  - more fine-grained belief data
  - variations in timing, payoff vectors