

# Image and Video Processing

#### **Feature Detection and Feature Descriptors**

Yao Wang Tandon School of Engineering, New York University

#### Lecture Outline

- Need for Features and Feature Descriptors
- Feature Detectors
  - Desired properties of features
  - Harris Detector
  - Scale Space
  - Harris-Laplace detector
  - SIFT detector
  - Scale and orientation detection
- Feature descriptors
  - SIFT
  - SURF
- Image classification using Bag of Visual Words

#### Why do we want to detect ad describe features?

- To establish correspondence between two images
  - Stitching of panorama
  - Image registration based on feature correspondence
- To describe an entire image or object for classification
  - Based on properties of all features detected in an image or object
  - Through the idea of bag of visual words

#### **Feature Correspondences**



#### Interest points extracted with Harris Detector (~ 500 points)

From <a href="https://courses.cs.washington.edu/courses/cse455/16wi/notes/index.html">https://courses.cs.washington.edu/courses/cse455/16wi/notes/index.html</a>, lecture on interest operators

#### **Panorama Stitching**



From <a href="https://courses.cs.washington.edu/courses/cse455/16wi/notes/index.html">https://courses.cs.washington.edu/courses/cse455/16wi/notes/index.html</a>, lecture on descriptorsYao Wang, 2020ECE-GY 6123: Image and Video Processing

#### **Panorama Stitching**



http://www.cs.ubc.ca/~mbrown/autostitch/autostitch.html From https://courses.cs.washington.edu/courses/cse455/16wi/notes/index.html, lecture on descriptors Yao Wang, 2020 ECE-GY 6123: Image and Video Processing

#### What Features Are Good?



Figure 4.3 Image pairs with extracted patches below. Notice how some patches can be localized or matched with higher accuracy than others.

> From Szeliski, Computer Vision: Algorithms and Applications, 2010 ECE-GY 6123: Image and Video Processing

#### What features are good?



no change in all directions

no change along the edge direction

significant change in all directions

From Szeliski, Computer Vision: Algorithms and Applications, 2010

#### **Mathematical Formulation**

 We would like a feature to be located where a slight shift in any direction causes a large difference, i.e. we want the following energy function to be large for any Δu=[Δx, Δy]<sup>T:</sup>

$$E_{\rm AC}(\Delta \boldsymbol{u}) = \sum_{\boldsymbol{i}} w(\boldsymbol{x}_{\boldsymbol{i}}) [I_0(\boldsymbol{x}_{\boldsymbol{i}} + \Delta \boldsymbol{u}) - I_0(\boldsymbol{x}_{\boldsymbol{i}})]^2$$

- Sum is over a window centered at the point being examined.
- W(x) is usually a Gaussian function

#### **Taylor Expansion and Moment Matrix**

$$\begin{split} E_{\mathrm{AC}}(\Delta \boldsymbol{u}) &= \sum_{i} w(\boldsymbol{x}_{i}) [I_{0}(\boldsymbol{x}_{i} + \Delta \boldsymbol{u}) - I_{0}(\boldsymbol{x}_{i})]^{2} \\ &\approx \sum_{i} w(\boldsymbol{x}_{i}) [I_{0}(\boldsymbol{x}_{i}) + \nabla I_{0}(\boldsymbol{x}_{i}) \cdot \Delta \boldsymbol{u} - I_{0}(\boldsymbol{x}_{i})]^{2} \\ &= \sum_{i} w(\boldsymbol{x}_{i}) [\nabla I_{0}(\boldsymbol{x}_{i}) \cdot \Delta \boldsymbol{u}]^{2} \\ &= \Delta \boldsymbol{u}^{T} \boldsymbol{A} \Delta \boldsymbol{u}, \end{split}$$

$$A = \begin{bmatrix} \sum_{x} w(x) I_{x}^{2} & \sum_{x} w(x) I_{x} I_{y} \\ \sum_{x} w(x) I_{x} I_{y} & \sum_{x} w(x) I_{y}^{2} \end{bmatrix} \quad \nabla I = \begin{bmatrix} I_{x} \\ I_{y} \end{bmatrix}, \quad \Delta u = \begin{bmatrix} \Delta x \\ \Delta y \end{bmatrix}$$

A is called Moment Matrix

ECE-GY 6123: Image and Video Processing

## **CSE486, Penn State** Taylor Series for 2D Functions

$$f(x+u, y+v) = f(x, y) + uf_x(x, y) + vf_y(x, y) +$$
  
First partial derivatives  
$$\frac{1}{2!} \left[ u^2 f_{xx}(x, y) + uv f_{xy}x, y + v^2 f_{yy}(x, y) \right] +$$
  
Second partial derivatives

$$\frac{1}{3!} \left[ u^3 f_{xxx}(x,y) + u^2 v f_{xxy}(x,y) + u v^2 f_{xyy}(x,y) + v^3 f_{yyy}(x,y) \right]$$
  
Third partial derivatives

 $+ \ldots$  (Higher order terms)

#### First order approx

$$f(x+u,y+v) \approx f(x,y) + uf_x(x,y) + vf_y(x,y)$$

http://www.cse.psu.edu/~rtc12/CSE486/lecture06.pdf ECE-GY 6123: Image and Video Processing

# Using eigenvalues of A to evaluate the goodness of a feature point

Eigenvectors  $\phi_i$  and eigenvalues  $\lambda_i$  of A are defined as  $A\phi_i = \lambda_i \phi_i, \quad i = 0, 1 \qquad \phi_0 \text{ and } \phi_1 \text{ are orthonormal}$ Once  $\phi_i$  and  $\lambda_i$  are found, A can be represented as  $A = \begin{bmatrix} \phi_1 & \phi_0 \end{bmatrix} \begin{vmatrix} \lambda_1 & & & & \phi_1^T \\ & \lambda_0 & & & \phi_0^T \end{vmatrix}$ Assuming  $\lambda_0 \ll \lambda_1$  and if  $\Delta u = \phi_0$ ,  $E(\phi_0) = \phi_0^T \begin{bmatrix} \phi_1 & \phi_0 \end{bmatrix} \begin{vmatrix} \lambda_1 & \\ & \lambda_0 \end{vmatrix} \begin{bmatrix} 0 \\ 1 \end{bmatrix} = \phi_0^T \begin{bmatrix} \phi_1 & \phi_0 \end{bmatrix} \begin{vmatrix} 0 \\ & \lambda_0 \end{vmatrix} = \lambda_0$ 

- The eigenvector  $\phi_0$  is the direction with the minimal change
- We want to find features points where the minimal eigenvalue is large! = we want both eigenvalues to be large!

#### **Robert Collins CSE486, Penn State Plotting Derivatives as 2D Points**



ECE-GY 6123: Image and Video Processing

# **CSE486, Penn StFitting Ellipse to each Set of Points**



http://www.cse.psu.edu/~rtc12/CSE486/lecture06.pdf ECE-GY 6123: Image and Video Processing

#### Harris Detector

- Feature points should be where both eigenvalues are large!
  - Difference between geometric mean and arithmetic mean should be large!
- Harris detector interest measure:

$$H = \lambda_0 \lambda_1 - \alpha (\lambda_0 + \lambda_1)^2, \quad \alpha = 0.06$$
  
Because  $A = \begin{bmatrix} \phi_1 & \phi_0 \end{bmatrix} \begin{bmatrix} \lambda_1 & \\ & \lambda_0 \end{bmatrix} \begin{bmatrix} \phi_1^T \\ & \phi_0^T \end{bmatrix} = \begin{bmatrix} a_{00} & a_{01} \\ & a_{01} & a_{11} \end{bmatrix}$   
Det $(A) = \lambda_1 \lambda_0 = a_{00} a_{11} - a_{01}^2$   
Trace $(A) = \lambda_1 + \lambda_0 = a_{00} + a_{11}$   
Therefore H=Det $(A) - \alpha$ Trace $(A)^2$   
No need to calculate the eigenvalues!

C.Harris and M.Stephens. "A Combined Corner and Edge Detector." Proceedings of the 4th Alvey Vision Conference: pages 147—151, 1988.

#### Harris Corner Point Detection Algorithm

- Compute the horizontal and vertical gradient images I<sub>x</sub> and I<sub>y</sub> by convolving the original image with derivative of Gaussian filters (usually with σ=1)
- Form three images  $I_x^2$ ,  $I_y^2$ , and  $I_x I_y$
- For each pixel, form a neighborhood window. Apply Gaussian weighting (usually with σ=2), and form the A matrix, and determine the Harris interest value

$$A = \begin{bmatrix} \sum_{x} w(x) I_{x}^{2} & \sum_{x} w(x) I_{x} I_{y} \\ \sum_{x} w(x) I_{x} I_{y} & \sum_{x} w(x) I_{y}^{2} \end{bmatrix} \qquad H = \det(A) - \alpha \ (Trace(A))^{2}$$

- Repeat the above process for each pixel to form the Harris interest measure image (Harris image)
- Find all local maxima in the Harris image and remove those points where the interest value < a threshold.
- The process of finding local maxima is also known as non-maximal Suppression. ECE-GY 6123: Image and Video Processing

#### Filter for Taking Derivatives

- Apply Gaussian filtering first to smooth the image, STD depends on noise level or desired smoothing effect
- Then take derivative in horizontal and vertical directions
- = Convolve the image with a Derivative of Gaussian filter

$$G(x,y) = e^{-\frac{x^2 + y^2}{2\sigma^2}}$$
$$H_x(x,y) = \frac{\partial G}{\partial x} = -\frac{x}{\sigma^2} e^{-\frac{x^2 + y^2}{2\sigma^2}}$$
$$H_y(x,y) = \frac{\partial G}{\partial y} = -\frac{y}{\sigma^2} e^{-\frac{x^2 + y^2}{2\sigma^2}}$$

• Sample the above continuous filter to get digital filter. Hy is rotated version of Hx

### Gaussian Filter (Review)

• Analog form: STD  $\sigma$  controls the smoothing strength

$$G(\mathbf{x},\mathbf{y}) = \exp\left\{-\frac{x^2 + y^2}{2\sigma^2}\right\},\,$$

- Take samples, truncate after a few STD, normalize the sum to 1. Usually  $\sigma >= 1$
- Size of mask nxn, typically n>=2σ+1 (2σ on each side), Ex: σ=1, n=7.
  - Show filter mask,
  - Show frequency response
- Essentially a weighted average filter with decreasing weights away from the center
- A good filter for removing noise. σ should be chosen based on noise STD.
- Can also be applied to an image patch pixel-wise as a weighting map.

#### Ex: 7x7 Gaussian Filter Generation

0.0000	0.0002	0.0011	0.0018	0.0011	0.0002	0.0000
0.0002	0.0029	0.0131	0.0216	0.0131	0.0029	0.0002
0.0011	0.0131	0.0586	0.0966	0.0586	0.0131	0.0011
0.0018	0.0216	0.0966	0.1592	0.0966	0.0216	0.0018
0.0011	0.0131	0.0586	0.0966	0.0586	0.0131	0.0011
0.0002	0.0029	0.0131	0.0216	0.0131	0.0029	0.0002
0.0000	0.0002	0.0011	0.0018	0.0011	0.0002	0.0000
0.0018 0.0011 0.0002 0.0000	0.0216 0.0131 0.0029 0.0002	0.0966 0.0586 0.0131 0.0011	0.1592 0.0966 0.0216 0.0018	0.0966 0.0586 0.0131 0.0011	0.0216 0.0131 0.0029 0.0002	0.0018 0.0011 0.0002 0.0000



function gauss(s)

x=[-3.0:1.0:3.0]; gauss=exp(-x.^2/(2\*s^2)); gauss2=gauss'\*gauss; gauss2=gauss2/(sum(sum(gauss2))); H=gauss2; disp(H); figure(1); surf(gauss2); figure(2); freqz2(gauss2); title('Gaussian Filter \sigma=1');



#### **Derivative Filter Examples**

	0.0366 0.0821 0 -0.0821 -0.0366	0.1642 0.3679 0 -0.3679 -0.1642	σ=1, n=5 0.2707 0.6065 0 -0.6065 -0.2707	0.1642 0.3679 0 -0.3679 -0.1642	0.0366 0.0821 0 -0.0821 -0.0366	σ =1, n=3 (similar to Sobel) 0.3679 0.6065 0.3679 0 0 0 -0.3679 -0.6065 -0.3679
Frequency response of filter						

Low-pass along the edge, and band-pass in orthogonal direction (across edge)

#### **Corner Response Example** CSE486, Penn State





#### Harris R score.

#### Ix, Iy computed using Sobel operator Windowing function w = Gaussian, sigma=1

http://www.cse.psu.edu/~rtc12/CSE486/lecture06.pdf

**Robert Collins** 

ECE-GY 6123: Image and Video Processing

### Pop Quiz!

• Which pixels (center of different patches) are good features?



- What does Harris detector detects?
- How to determine the moment matrix A?
- What do the eigenvectors and eigenvalues of A indicate?

#### How good is Harris Detector?

- Invariant to brightness offset. Why?
- Invariant to shift and rotation. Why?
- Not invariant to scaling!



#### Other detectors

- Vary in terms of the interest measure
- Hessian Detector:
  - Form a Hessian matrix (Using 2<sup>nd</sup> order gradients)
  - Using the Determinant of the Hessian matrix as the interest measure

$$\mathbf{H}[x,y] = \begin{bmatrix} f_{xx}[x,y] & f_{xy}[x,y] \\ f_{xy}[x,y] & f_{yy}[x,y] \end{bmatrix}$$
$$= \begin{bmatrix} D_{xx}[x,y] * f[x,y] & D_{xy}[x,y] * f[x,y] \\ D_{xy}[x,y] * f[x,y] & D_{yy}[x,y] * f[x,y] \end{bmatrix}$$

det **H**[x,y] =  $f_{xx}[x,y]f_{yy}[x,y] - (f_{xy}[x,y])^2$ 

- Maximally Stable Extremal Regions
- Problem: second order gradient is sensitive to noise

#### **Derivative and Laplacian of Gaussian**



ECE-GY 6123: Image and Video Processing

Local maxima of magnitude of normalized Laplacian images in both position and scale are good feature points!



From <a href="https://courses.cs.washington.edu/courses/cse455/16wi/notes/index.html">https://courses.cs.washington.edu/courses/cse455/16wi/notes/index.html</a>, lecture on interest operatorsYao Wang, 2020ECE-GY 6123: Image and Video Processing2

# Normalized Laplacian Operator for Feature Detection

- The local maxima of the absolute value of σ<sup>2</sup>∇<sup>2</sup>G (normalized Laplacian) produce the most stable image features compared to a range of other possible image functions, such as the gradient, Hessian, or Harris corner function.
- Can apply the Laplacian operator using different σ to detect feature points at different scales.

#### Scale-space image processing

Corresponding image features can appear at different scales



- Like shift-invariance, scale-invariance of image processing algorithms is often desirable.
- Scale-space representation is useful to process an image in a manner that is both shift-invariant and scale-invariant

[courtesy B. Girod, (c) 2013 Stanford University]

From http://web.stanford.edu/class/ee368/Handouts/Lectures/2016\_Autumn/14-ScaleSpace\_16x9.pdf

#### **Gaussian Scale Space**



A Gaussian pyramid with multiple scales at the same resolution:

$$L(x, y, \sigma_n) = G(x, y, \sigma_n) * I(x, y), \quad \sigma_n = \sigma_0 k^n$$
$$G(x, y, \sigma) = \frac{1}{2\pi\sigma^2} e^{-(x^2 + y^2)/2\sigma^2}$$

Typically,  $\sigma_0 = 1, k = \sqrt{2}$ 

With the above choice, every octave has 3 scales n = 0,1,2

In the left example,  $k=2^{1/4}$ , so each octave has 5 scales

$$n = 0, 1, 2, 3, 4$$

One can apply Laplacian at each scale and each resolution, and find the local maximum cross scale and spatial neighbor to detect stable feature points.

#### Using Difference of Gaussian to Approximate Normalized Laplacian

$$G(x, y, \sigma) = \frac{1}{2\pi\sigma^2} e^{-(x^2 + y^2)/2\sigma^2}$$

$$G_x(x, y, \sigma) = -\frac{x}{2\pi\sigma^4} e^{-(x^2 + y^2)/2\sigma^2}$$

$$G_{xx}(x, y, \sigma) = -\left(1 - \frac{x^2}{\sigma^2}\right) \frac{1}{2\pi\sigma^4} e^{-(x^2 + y^2)/2\sigma^2} = -\left(1 - \frac{x^2}{\sigma^2}\right) \frac{1}{\sigma^2} G(x, y, \sigma)$$

$$\nabla G(x, y, \sigma) = G_{xx}(x, y, \sigma) + G_{yy}(x, y, \sigma) = -\left(2 - \frac{x^2 + y^2}{\sigma^2}\right) \frac{1}{\sigma^2} G(x, y, \sigma)$$

It is easy to show that the Gaussian function satisfy the following equation

$$\frac{\partial G}{\partial \sigma} = \sigma \nabla^2 G = \sigma \left( \frac{\partial^2 G}{\partial x^2} + \frac{\partial^2 G}{\partial y^2} \right)$$
  
Because  $\frac{\partial G}{\partial \sigma} \approx \frac{G(x, y, k\sigma) - G(x, y, \sigma)}{k\sigma - \sigma}$   
Therefore  $G(x, y, t\sigma) - G(x, y, \sigma) \approx (k-1)\sigma \frac{\partial G}{\partial \sigma} = (k-1)\sigma^2 \nabla^2 G$ 

This means that difference of Gaussian filtered images produces images of  $\sigma^2 \nabla^2 G$  up to a constant scaling factor!

ECE-GY 6123: Image and Video Processing

# Using Difference of Gaussian (DoG) to Approximate Normalized Laplacian (LoG)



From https://courses.cs.washington.edu/courses/cse455/13au/: Lecture on "interest points"



[courtesy B. Girod, (c) 2013 Stanford University]

From http://web.stanford.edu/class/ee368/Handouts/Lectures/2016\_Autumn/14-ScaleSpace\_16x9.pdf

ECE-GY 6123: Image and Video Processing



#### Generating Laplacian Scale Space using Difference of Gaussian

Note: In this example, t represents  $\sigma^2$ , k=2 <sup>1/4,</sup> and each octave ( $\sigma$ doubles) consists of 5 scales. Lowe has found 3 scales (using k=sqrt(2)) is best (two LOG images at each scale)

[courtesy B. Girod, (c) 2013 Stanford University]

From http://web.stanford.edu/class/ee368/Handouts/Lectures/2016\_Autumn/14-ScaleSpace\_16x9.pdf

#### Scale Space: Gaussian vs. Laplacian



[courtesy B. Girod, (c) 2013 Stanford University]

In the above notation: 
$$t = \sigma^2$$
,  $\sigma = \sqrt{t}$ 

From http://web.stanford.edu/class/ee368/Handouts/Lectures/2016\_Autumn/14-ScaleSpace\_16x9.pdfYao Wang, 2020ECE-GY 6123: Image and Video Processing

### Pop Quiz

- You need to write a program to generate the Gaussian and Laplacian scale space, what would be the steps in the program?
- Steps:
  - Generate Guassian filters with varying scales  $\sigma_n = \sigma_0 k^{n_r}$
  - Convolve the image with Gaussian filters with  $\sigma_n$ . Down sample everytime scale doubles -> Gaussian scale space
  - Take difference of two adjacent images in the same resolution -> Laplacian scale space
- How is this different from the Laplacian Pyramid?
  - Laplacian pyramid image at level k = difference between image at level k – upsampled image from level k-1
  - Laplacian image at scale k = Gaussian image at scale k –Gaussian image at k-1
  - No explicit upsampling operation, directly approximate Laplacian filtering
  - Can have multiple scales at the same resolution

# SIFT scale space pyramid: octave 1








L



#### Finding Extrema in the Laplacian Scale Space



Initially locate the extrema (maximum or minimum) by comparing with 26 neighboring pixels. This position is then refined with a shift.

*Figure 2.* Maxima and minima of the difference-of-Gaussian images are detected by comparing a pixel (marked with X) to its 26 neighbors in  $3 \times 3$  regions at the current and adjacent scales (marked with circles).

#### SIFT Feature Detector (Lowe 1999, 2004)



[courtesy B. Girod, (c) 2013 Stanford University]

From http://web.stanford.edu/class/ee368/Handouts/Lectures/2016\_Autumn/14-ScaleSpace\_16x9.pdf

#### Harris-Laplacian Detector

- Detect Harris corners at multiple scales (on the Gaussian filtered images at scales σ<sub>n</sub>, n=0,1,...,)
- For each detected Harris corner x<sub>h</sub>,y<sub>h</sub> at any scale, determine the characteristic scale (the scale at which Laplacian/DoG achieves maximum or minimum)

$$\sigma_h = \operatorname{argmax} \left| \sigma^2 \nabla L(x_h, y_h, \sigma) \right|$$

- Keep the point at  $x_h, y_h, \sigma_h$
- Ref: K. Mikolajczyk and C. Schmid, "Indexing Based on Scale Invariant Interest Points," Proc. Eighth Int'l Conf. Computer Vision, pp. 525-531, 2001.

#### Key Point Detection: Harris-Laplacian vs SIFT



[courtesy B. Girod, (c) 2013 Stanford University]

From http://web.stanford.edu/class/ee368/Handouts/Lectures/2016\_Autumn/14-ScaleSpace\_16x9.pdf

ECE-GY 6123: Image and Video Processing

#### **Comparison of Different Feature Detectors**

- Evaluation criterion:
  - Repeatability under scaling, rotation, view angle change (affine transform), and noise
- Mikolajczyk, K., Tuytelaars, T., Schmid, C., Zisserman, A., Matas, J., Schaffalitzky, F., Kadir, T., and Van Gool, L. J. (2005). A comparison of affine region detectors. International Journal of Computer Vision, 65(1-2):43– 72.
  - Code for different detectors: http://www.robots.ox.ac.uk/vgg/research/affine/.
  - Multiscale Harris and Hessian are better than SIFT detector.
  - Hessian slightly better than Harris.

#### **Comparison of Feature Detectors**



[courtesy B. Girod, (c) 2013 Stanford University]

From http://web.stanford.edu/class/ee368/Handouts/Lectures/2016\_Autumn/14-ScaleSpace\_16x9.pdf

ECE-GY 6123: Image and Video Processing

#### Feature Descriptor

- Why do we need them?
  - To find corresponding features between two images
- Simple approach
  - Using the image values surrounding a feature point as its descriptor
  - Compare two descriptors using Euclidean distance or other norms
  - Not robust to changes in view angle/distance and positions and sensitive to occlusion and lighting/contrast changes

#### Need for rotation invariance





From https://courses.cs.washington.edu/courses/cse455/08wi/lectures/features.pdf



by Diva Sian

by scgbt

From https://courses.cs.washington.edu/courses/cse455/08wi/lectures/features.pdf

#### **General Approach for Feature Descriptors**

- Desirable properties
  - Invariant to shift, scale and rotations and contrast differences
- General approach:
  - Determine the scale where a feature is most stable
  - Determine the orientation of the small patch surrounding this feature point at this scale
  - Characterize a small patch tilted in this orientation and scale with a descriptor
  - The descriptor should be invariant to intensity shift or scaling, and small position shift
  - Most popular: SIFT descriptor by David Lowe (UBC)
    - http://www.cs.ubc.ca/~lowe/keypoints/



#### Feature Descriptors

From https://courses.cs.washington.edu/courses/cse455/08wi/lectures/features.pdf

Descriptor use normalized patches where the dominant line in an original patch is rotated to a standard direction (e.g. vertical!) and the original patch is scaled to the same size!



Figure 4.10 Multi-scale oriented patches (MOPS) extracted at five pyramid levels (Brown, Szeliski, and Winder 2005) © 2005 IEEE. The boxes show the feature orientation and the region from which the descriptor vectors are sampled.

A descriptor is generated for each feature point detected at a particular scale by extracting a patch surrounding the point based on its scale and orientation.

> From Szeliski, Computer Vision: Algorithms and Applications, 2010 ECE-GY 6123: Image and Video Processing

#### **Determination of Dominant Orientation**



#### Histogram of Orientation of Gradient (HoG)

- Extract a patch surrounding the detected feature point at the detected scale
- Derive image gradient I<sub>x</sub> and I<sub>y</sub> and determine the magnitude and orientation for every pixel. Zero out weak edges (set small magnitude to 0)
  - Using Derivative of Gaussian filters with the same  $\sigma$  as the detected scale,
  - Or using central difference on the Gaussian filtered image at that scale

 $m(x, y) = \sqrt{(L(x+1, y) - L(x-1, y))^2 + (L(x, y+1) - L(x, y-1))^2}$  $\theta(x, y) = \tan^{-1}((L(x, y+1) - L(x, y-1))/(L(x+1, y) - L(x-1, y)))$ 

- Quantize the orientation to a chosen set of bins in  $(0, 2\pi)$ .
- Apply Gaussian weighting at a larger σ (σ=1/2 width of patch size) to the gradient magnitude
- Generate a histogram, where the entry for each orientation bin is the sum of weighted gradient magnitude of all pixels with that orientation
- Finding the orientation with the peak frequency
- For more details see [Lowe2004]

#### **HoG Examples**



[courtesy B. Girod, (c) 2013 Stanford University]

From: http://web.stanford.edu/class/ee368/Handouts/Lectures/2016\_Autumn/15-Featurebased\_Image\_Matching\_16x9.pdf

#### Pop Quiz

- What will the HoG look like for following patches?
  - Assume yellow has a higher brightness than green



#### SIFT Descriptor For a Given Patch (Basic Idea)



**Figure 4.18** A schematic representation of Lowe's (2004) scale invariant feature transform (SIFT): (a) Gradient orientations and magnitudes are computed at each pixel and weighted by a Gaussian fall-off function (blue circle). (b) A weighted gradient orientation histogram is then computed in each subregion, using trilinear interpolation. While this figure shows an  $8 \times 8$  pixel patch and a  $2 \times 2$  descriptor array, Lowe's actual implementation uses  $16 \times 16$ patches and a  $4 \times 4$  array of eight-bin histograms.

> From Szeliski, Computer Vision: Algorithms and Applications, 2010 ECE-GY 6123: Image and Video Processing

### Orientation invariance: Shift of HoG to Align with Reference Orientation



Adapted from https://courses.cs.washington.edu/courses/cse455/13au/: Lecture on "interest points"

# How to deal with feature points with different scales?

- Generate patches with a fixed size at the detected scale in the Gaussian scale space
- The image is halved for every increasing octave
- The effective patch size doubles for every increasing octave!

#### **SIFT Descriptor**

- Put a patch of 16x16 around each feature point at the detected scale in the Gaussian scale space.
- Generate a HOG for the entire patch, determine the dominant orientation
- Divide it into 4x4 cells, each cell 4x4 in size
- Generate a (HoG) for each cell with 8 bins
- Shift each HoG so that the dominant orientation is in the first bin (0 degree).
- Concatenate the shifted HoG of each cell into a single descriptor
  - 16 cells \* 8 orientations= 128 dimension descriptor!
- Normalize the descriptor so that it is invariant to intensity variation
  - Set all entries >0.2 to 0.2
  - Normalize the resulting descriptor
  - Robust to contrast/brightness variation!
- SIFT descriptor can be used for feature points extracted by other methods (e.g. Harris).
  - Harris-Laplacian Detector + SIFT Descriptor is a popular combination!

#### Pop Quiz

- Why use the HoG to describe a patch?
- Invariant to brightness and position change
- Why do you want to shift the HoG based on the dominant direction
- Invariant to rotation
- Why use scale space?
- To achieve scale invariance

#### Power of SIFT Descriptor

- Extraordinarily robust matching technique
- Can handle changes in viewpoint
  - Up to about 60 degree out of plane rotation
- Can handle significant changes in illumination
  - Sometimes even day vs. night (below)
- Fast and efficient—can run in real time
  - Lots of code available
  - <u>http://people.csail.mit.edu/albert/ladypack/wiki/index.php/Know</u>
    <u>n\_implementations\_of\_SIFT</u>
  - <u>http://www.cs.ubc.ca/~lowe/keypoints/</u>

From <u>https://courses.cs.washington.edu/courses/cse455/16wi/notes/index.html</u>, lecture on descriptors

#### Can you find the toy car and frog in the picture?



From Szeliski, Computer Vision: Algorithms and Applications, 2010

ECE-GY 6123: Image and Video Processing



NASA Mars Rover images, Figure by Noah Snavely

From https://courses.cs.washington.edu/courses/cse455/16wi/notes/index.html, lecture on descriptor:

ECE-GY 6123: Image and Video Processing

#### **Other Descriptors**

- SURF (Speed-Up Robust Feature) (can be computed very fast)
- 3D SIFT
- 3D SURF
- GLOH (Gradient Location and Orientation Histogram)
- Mikolajczyk, K. and Schmid, C. (2005). A performance evaluation of local descriptors. IEEE Transactions on Pattern Analysis and Machine Intelligence, 27(10):1615–1630.
  - GLOH is best, closely followed by SURF

#### Speeded Up Robust Features (SURF)

- Compute horizontal and vertical differences in local rotated patches, using patch size of  $20\sigma \times 20\sigma$  if  $\sigma$  is the feature scale, divide the window into 4x4 cells or 3x3 cells
- Sum dx, dy, |dx| and |dy| over each cell, yielding a dimension 4 sub-descriptor
- Stack all cell-descriptors into a single descriptor



Fig. 3. The descriptor entries of a sub-region represent the nature of the underlying intensity pattern. Left: In case of a homogeneous region, all values are relatively low. Middle: In presence of frequencies in x direction, the value of  $\sum |d_x|$  is high, but all others remain low. If the intensity is gradually increasing in x direction, both values  $\sum d_x$  and  $\sum |d_x|$  are high.

Herbert Bay, Tinne Tuytelaars, and Luc Van Gool, SURF: Speeded Up Robust Features, ECCV 2006

#### Other kinds of descriptors

- There are descriptors for other purposes
  - Describing shapes
  - Describing textures
  - Describing features for image classification (e.g. bag of words, to be covered later)

From <u>https://courses.cs.washington.edu/courses/cse455/16wi/notes/index.html</u>, lecture on descriptor

#### **Bag of Visual Words for Image Classification**



- 1. Extract features
- 2. Learn "visual vocabulary"
- Quantize features using visual vocabulary
- Represent images by frequencies of "visual words"

BoW Pipeline for Image Classification

From http://www.cs.cmu.edu/~16385/l ectures/Lecture12.pdf

#### 1. Extract features

At every detected feature points generate SIFT, HOG, or other descriptors

- 2. Learn "visual vocabulary"
- Quantize features using visual vocabulary
- Represent images by frequencies of "visual words"



1. Extract features

# 2. Learn "visual vocabulary"



 Quantize features using visual vocabulary How to deduce these words ?

Group all features in the training set into a finite number of clusters (K-means clustering, GMM clustering, etc.), and represent each cluster by a "mean feature vector" (a visual word)

 Represent images by frequencies of "visual words"

From http://www.cs.cmu.edu/~16385/I ectures/Lecture12.pdf

- 1. Extract features
- 2. Learn "visual vocabulary"
- 3. Quantize features using visual vocabulary

For a new image, replace the descriptor of each feature point by the "word" that is closest to the original descriptor (nearest neighbor search)



4. Represent images by frequencies of "visual words"

> From http://www.cs.cmu.edu/~16385/I ectures/Lecture12.pdf

ECE-GY 6123: Image and Video Processing
- 1. Extract features
- 2. Learn "visual vocabulary"
- Quantize features using visual vocabulary
- 4. Represent images by frequencies of "visual words"

From http://www.cs.cmu.edu/~16385/I



# How to Learn Visual Dictionary?

- Assume you have feature vectors extracted from many training images
- Apply K-means or other clustering algorithms to all training feature vectors!
- The training images should encompass categories to be classified
- How to select initial centroids?
  - K-means++
- How to determine K?
- Belong to the problem of "unsupervised learning". Beyond the scope of this class. Self study!

### "Words" from people



From http://www.cs.cmu.edu/~16385/I ECE-GY 6123: Image and Video Processing ectures/Lecture12.pdf

#### "Words" from cars



Υ





# Histogram of Visual Words

- Count how many times each "word" appears in an image -> Histogram of words
- Can you tell the image types from the following histograms?



# How to Classify Images?

- Use the histogram of words as the descriptor for an image
- Train a classifier (e.g. Support Vector Machine) from training images

# Pop Quiz

- What are the major steps to use BoW to classify images?
- Training stage
  - For each training image, detect feature points and generate the feature descriptors;
  - Using K-means to cluster all the descriptors from all training images to a dictionary of words;
  - Express each training image by a histogram of words (BoW);
  - Train a classifier (SVM or NN) using the BoW representations.
- Given a test image
  - Generate Gaussian and Laplacian scale images
  - Detect feature points
  - Generate descriptors at detected feature points
  - Quantize each descriptor to the nearest word in the dictionary
  - Generate the histogram of words for the image
  - Apply the classifier

# Power of BoW!

#### Now beaten by Deep Networks :(

# CalTech6 dataset



class	bag of features	bag of features	Parts-and-shape model
Class	Zhang et al. (2005)	Willamowski et al. (2004)	Fergus et al. (2003)
airplanes	98.8	97.1	90.2
cars (rear)	98.3	98.6	90.3
cars (side)	95.0	87.3	88.5
faces	100	99.3	96.4
motorbikes	98.5	98.0	92.5
spotted cats	97.0	—	90.0

#### Works pretty well for image-level classification

From http://www.cs.cmu.edu/~16385/lectures/Lecture12.pdf

ECE-GY 6123: Image and Video Processing

#### But what about layout?



#### All of these images have the same color histogram

From http://www.cs.cmu.edu/~16385/lectures/Lecture12.pdf

ECE-GY 6123: Image and Video Processing

# Spatial pyramid representation

- Extension of a bag of features •
- Locally orderless representation at several levels of resolution •



Using concatenation of all these histograms to describe an image! ECE-GY 6123: Image and Video Processing

# Summary

- Criteria to select features and describe features
  - Invariance to view angle change (shift, rotation and scale, more generally affine transformation) and contrast change.
  - Robust to clutter and occlusion
    - By using local features
- Feature detectors
  - Locating corners where there are changes in multiple directions
    - Edges are not good features (not unique)
    - Harris corner detector
  - Can be observed in different scales (stable cross scales)
    - Generating Gaussian and Laplacian Scale space
    - SIFT detector: Detecting local extrema in Laplacian scale space
    - Harris-Laplacian: Harris detector in each Gaussian scale, detect characteristic scale of each feature

# Summary (Cnt'd)

- Feature Descriptors
  - Achieving invariance to contrast and position shift by using histogram of orientation of gradient (HoG)
  - Achieving rotation invariance by shifting the dominant orientation in the HoG to the same reference orientation
  - Achieve scale invariance through detecting the characteristic scales
  - Most popular: SIFT, SURF
- Use of feature detection and descriptors
  - Image classification using Bag of Words
  - Feature matching for image registration/ stitching (next lecture)

# **Reading Assignment**

- [Szeliski2012] Richard Szeliski, Computer Vision: Algorithms and Applications. 2012. Sec. 4.1, 4.2
- Optional:
- Harris, C. and Stephens, M. J. (1988). A combined corner and edge detector. In Alvey Vision Conference , pp. 147–152.
- Lowe, D. G. (2004). Distinctive image features from scale-invariant keypoints. International Journal of Computer Vision , 60(2):91–110.
- Mikolajczyk, K., Tuytelaars, T., Schmid, C., Zisserman, A., Matas, J., Schaffalitzky, F., Kadir, T., and Van Gool, L. J. (2005). A comparison of affine region detectors. International Journal of Computer Vision, 65(1-2):43–72.

- Code for different detectors: http://www.robots.ox.ac.uk/vgg/research/affine/

- Mikolajczyk, K. and Schmid, C. (2005). A performance evaluation of local descriptors. IEEE Transactions on Pattern Analysis and Machine Intelligence , 27(10):1615–1630.
- Bay, H., Tuytelaars, T., and Van Gool, L. (2006). SURF: Speeded up robust features. In Ninth European Conference on Computer Vision (ECCV 2006), pp. 404–417.
- An easy to follow tutorial: http://aishack.in/tutorials/sift-scale-invariant-feature-transform-introduction/

# Software Tools

- VLFeat, an open and portable library of computer vision algorithms, <u>http://vlfeat.org/</u>.
  - Include both SIFT detector and descriptor
  - Written in C, with interface for MATLAB
  - Matlab : <u>http://www.vlfeat.org/install-matlab.html</u> (install tutorial)
- SiftGPU: A GPU Implementation of Scale Invariant Feature Transform (SIFT), http:
  - //www.cs.unc.edu/ccwu/siftgpu/ (Wu 2010).
- SURF: Speeded Up Robust Features, http://www.vision.ee.ethz.ch/surf/ (Bay, Tuytelaars, and Van Gool 2006).
  - Python : in opencv package. Simply call by cv2.SURF
- Harris corner detector :
  - Python : in opencv package. Simply call by cv2.cornerHarris
  - MATLAB: corner( )

# **Software Tools**

- SIFT tools in python through opency
  - detector = cv2.FeatureDetector\_create("SIFT")
  - descriptor = cv2.DescriptorExtractor\_create("SIFT")
  - skp = detector.detect(img)
  - skp, sd=descriptor.compute(img,skp)
  - <u>https://jayrambhia.wordpress.com/2013/01/18/sift-keypoint-matching-using-python-opencv/</u>

# **Review Questions**

- 1. What are the desired properties of feature detectors?
- 2. What are the desired properties of feature descriptors?
- 3. Are points with high gradient magnitudes always good as a feature point?
- 4. What are the steps in detecting Harris feature points at a fixed scale?
- 5. What are the steps in generating a Laplacian of Gaussian scale space?
- 6. What are the steps in detecting Harris feature points at characteristic scales?
- 7. What are the steps in detecting SIFT feature points?
- 8. What are the steps in forming the Histogram of Orientation of Gradients (HoG) of a small patch?
- 9. What are the steps in forming the SIFT descriptor of a feature point, given its scale and orientation?
- 10. Show that difference of two Gaussian filtered images with scales  $k\sigma$  and  $\sigma$  is proportional to an image convolved with a Laplacian of Gaussian filter at the scale of  $\sigma$ . Note that this is the basis for Lowe to propose to generate the scale space of normalized Laplacian of Gaussian filtered images using differences of Gaussian filtered images.

# Written Homework

1. Consider the following images. For the center patch of each image (with size 5x5, colored in red), determine the moment matrix A and find its eigenvalues and eigenvectors and finally the Harris cornerness value. Furthermore, show that the Harris value computed using the eigenvalues are the same as that using the determinant and trace of A. Which patch has a higher Harris value? Is that as expected? For simplicity, use central difference to compute the horizontal and vertical gradient (i.e., filter [-1, 0, 1].) Show the gradient images as intermediate results. You can ignore the Gaussian weighting step when computing the A matrix.

0	0	0	0	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	1	1	1	1	1	0	0	0	0	1	1	1	1	1	0	0	0	0	1	0	0	0	0
0	0	0	0	1	1	1	1	1	0	0	0	0	1	1	1	1	1	0	0	0	1	1	1	0	0	0
0	0	0	0	1	1	1	1	1	0	0	0	0	1	1	1	1	1	0	0	1	1	1	1	1	0	0
0	0	0	0	1	1	1	1	1	0	0	0	0	1	1	1	1	1	0	1	1	1	1	1	1	1	0
0	0	0	0	1	1	1	1	1	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1

2. Compute the HoG for the center patch in each of the above images and determine the dominant orientations. Are your results as expected?

For the above two problems you can do either manually or using MATLAB/Python or a combination.