

## Wealth Distribution and Social Mobility in the US: A Quantitative Approach<sup>†</sup>

By JESS BENHABIB, ALBERTO BISIN, AND MI LUO\*

*We quantitatively identify the factors that drive wealth dynamics in the United States and are consistent with its skewed cross-sectional distribution and with social mobility. We concentrate on three critical factors: (i) skewed earnings, (ii) differential saving rates across wealth levels, and (iii) stochastic idiosyncratic returns to wealth. All of these are fundamental for matching both distribution and mobility. The stochastic process for returns which best fits the cross-sectional distribution of wealth and social mobility in the United States shares several statistical properties with those of the returns to wealth uncovered by Fagereng et al. (2017) from tax records in Norway. (JEL D31, E13, E21, E25)*

Wealth in the United States is unequally distributed, with a Gini coefficient of 0.82. It is skewed to the right, and displays a thick, right tail: the top 1 percent of the richest households in the United States hold over 33.6 percent of wealth.<sup>1</sup> At the same time, the United States is characterized by a nonnegligible social mobility, with an intergenerational Shorrocks mobility index 0.88.<sup>2</sup> This paper attempts to quantitatively identify the factors that drive wealth dynamics in the United States and are consistent with the observed cross-sectional distribution of wealth and with the observed social mobility.

To this end, we first develop a macroeconomic model displaying various distinct wealth accumulation factors. Once we allow for an explicit demographic structure, the model delivers implications for social mobility as well as for the cross-sectional

\* Benhabib: Department of Economics, New York University, 19 W 4th Street, FL 6, New York, NY 10012, and the National Bureau of Economic Research (email: [jess.benhabib@nyu.edu](mailto:jess.benhabib@nyu.edu)); Bisin: Department of Economics, New York University, 19 W 4th Street, FL 6, New York, NY 10012, and the National Bureau of Economic Research (email: [alberto.bisin@nyu.edu](mailto:alberto.bisin@nyu.edu)); Luo: Department of Economics, Emory University, 1602 Fishburne Drive, Atlanta, GA 30307 (email: [mi.luo@emory.edu](mailto:mi.luo@emory.edu)). Luigi Pistaferri was the coeditor for this paper. Thanks to seminar audiences at Duke, NYU, Minneapolis Fed, SED-Warsaw, Lake Baikal Summer School, SAET-Cambridge, University College of London, Wharton School, NBER Summer Institute. Special thanks to Alberto Alesina, Fernando Alvarez, Orazio Attanasio, Laurent Calvet, Tim Christensen, Tim Cogley, Mariacristina De Nardi, Pat Kehoe, Dirk Krueger, Per Krusell, Konrad Menzel, Ben Moll, Andrew Newman, Tom Sargent, Ananth Seshadri, Rob Shimer, Kevin Thom, Gianluca Violante, Daniel Xu, Fabrizio Zilibotti. Special thanks to Luigi Guiso, for many illuminating discussions and for spotting a mistake in a previous version, to the editor and the referees for their exceptional work on the paper. Generous financial support from the Washington Center for Equitable Growth is gratefully acknowledged.

<sup>†</sup>Go to <https://doi.org/10.1257/aer.20151684> to visit the article page for additional materials and author disclosure statements.

<sup>1</sup>See Díaz-Giménez, Glover, and Ríos-Rull (2011), Table 6, elaborating data from the 2007 SCF.

<sup>2</sup>See Charles and Hurst (2003), Table 2, from PSID data. By construction, mobility matrices have Shorrocks indices increasing as the transition step gets long (indeed the index converges to 1 as the step goes to  $\infty$ ).

distribution. We then match the moments generated by the model to several empirical moments of the observed distribution of wealth as well as of the social mobility matrix. While the model is very stylized and parsimonious, it allows us to identify various distinct wealth accumulation factors through their distinct role on inequality and mobility.

Many recent studies of wealth distribution and inequality focus on the relatively difficult task of explaining the thickness of the upper tail. We shall concentrate mainly on three critical factors previously shown, typically in isolation from each other, to affect the tail of the distribution, empirically and theoretically. First, a skewed and persistent distribution of *stochastic earnings* translates, in principle, into a wealth distribution with similar properties. A large literature in the context of Aiyagari-Bewley economies has taken this route, notably Castañeda et al. (2003) and Kindermann and Krueger (2015).<sup>3</sup> Another factor which could contribute to generating a skewed distribution of wealth is *differential saving rates* across wealth levels, with higher saving and accumulation rates for the rich. In the literature this factor takes the form of non-homogeneous bequests, bequests as a fraction of wealth that are increasing in wealth; see, for example, De Nardi (2004).<sup>4</sup> Stochastic idiosyncratic returns to wealth, or *capital income risk*, also has been shown to induce a skewed distribution of wealth, in Benhabib, Bisin, and Zhu (2011); see also Quadrini (2000) and Cagetti and De Nardi (2006), which focuses on entrepreneurial risk.<sup>5</sup> Finally, allowing rates of return on wealth to be increasing in wealth might also add to the skewness of the distribution. This could be due, e.g., to the existence of economies of scale in wealth management, as in Kacperczyk, Nosal, and Stevens (2015), or to fixed costs of holding high return assets, as in Kaplan, Moll, and Violante (2016). See Saez and Zucman (2016), Fagereng et al. (2016, 2017), and Piketty (2014, p. 447) for evidence about the relationship between returns and wealth.

While all of these factors possibly contribute to produce skewed wealth distributions, their relative importance remains to be ascertained.<sup>6</sup> In our quantitative analysis we find that all of the factors we study (stochastic earnings, differential savings, and capital income risk) have a fundamental role in generating the thick right tail of the wealth distribution and sufficient social mobility in the wealth accumulation process. We also identify a distinct role for these factors. Capital income risk and differential savings both contribute to generating the thick tail. Their effect on social mobility is however more nuanced: both differential savings and capital income risk increase social mobility across the distribution, more pronouncedly at the top in the case of capital income risk, while decreasing the probability of escape from the

<sup>3</sup> Several papers in the literature include a stochastic length of life (typically, “perpetual youth”) to complement the effect of skewed earnings on wealth. We do not include this in our model as it has counterfactual demographic implications.

<sup>4</sup> See also Piketty (2014), which directly discusses the saving rates of the rich.

<sup>5</sup> Stochastic discount factors, as introduced by Krusell and Smith (1998), induce a skewed distribution of wealth through a similar mechanism. However, such discount factors are nonmeasurable, while microdata allowing estimates of capital income risk are instead rapidly becoming more available; see, e.g., the tax records for Norway studied by Fagereng et al. (2016, 2017) and the Swedish data studied by Bach, Calvet, and Sodini (2017).

<sup>6</sup> Other possible factors which qualitatively would induce skewed wealth distributions include a precautionary savings motive for wealth accumulation. In fact, the precautionary motive, by increasing the savings rate at low wealth levels under borrowing constraints and random earnings, works in the opposite direction of savings rates increasing in wealth. We do not exploit this channel for simplicity, assuming that life-cycle earnings profiles are random across generations but deterministic within lifetimes.

bottom 20 percent. On the other hand, stochastic earnings have a limited role in filling the tail of the wealth distribution but are fundamental in inducing enough mobility in the wealth process. Finally, a rate of return of wealth increasing in wealth itself is also apparently supported in our estimates, improving the fit of the model across the wealth distribution (though, without directly observing return data, this mechanism is somewhat poorly identified).

The rest of the paper is structured as follows. Section I lays out the theoretical framework. Section II explains our quantitative approach and data sources we use. Section III shows the baseline results with the model fit for both targeted and untargeted moments. The main extensions and robustness exercises we perform are also discussed in this section. Section IV presents several counterfactual exercises, where we re-estimate the model shutting down one factor at a time. Section V introduces an empirical exercise where we relax the stationarity assumption on the wealth distribution and measure the transition speed our model delivers. Section VI concludes.

### I. Wealth Dynamics and Stationary Distribution

Most models of the wealth dynamics in the literature focus on deriving skewed distributions with thick tails, e.g., Pareto distributions (power laws).<sup>7</sup> While this is also our aim, we more generally target the whole wealth distribution and its inter-generational mobility properties. To this end we study a simple microfounded model (a standard macroeconomic model in fact) of life-cycle consumption and savings. While very parsimonious, the model exploits the interaction of the factors identified in the Introduction that tend to induce skewed wealth distributions: stochastic earnings, differential saving and bequest rates across wealth levels, and stochastic returns on wealth.

Each agent's life span is finite and deterministic,  $T$  years. Every period  $t$ , consumers choose consumption  $c_t$  and accumulate wealth  $a_t$ , subject to a no-borrowing constraint. Consumers leave wealth  $a_T$  as a bequest at the end of life  $T$ . Each agent's preferences are composed of a per-period utility from consumption,  $u(c_t)$ , at any period  $t = 1, \dots, T$ , and a warm-glow utility from bequests at  $T$ ,  $e(a_T)$ . Their functional forms display constant relative risk aversion,

$$u(c_t) = \frac{c_t^{1-\sigma}}{1-\sigma}, \quad e(a_T) = A \frac{a_T^{1-\mu}}{1-\mu}.$$

Wealth accumulates from savings and bequests. Idiosyncratic rates of return  $r$  and life-time labor earnings profiles  $w = \{w_{it}\}_{t=1}^T$  are drawn from a distribution at birth, possibly correlated with those of the parent, deterministic within each generation.<sup>8</sup>

<sup>7</sup> See Benhabib and Bisin (2018) for an extensive survey of the theoretical and empirical literature on the wealth distribution.

<sup>8</sup> As we noted, assuming deterministic earning profiles amounts to disregarding the role of intragenerational life-cycle uncertainty and hence of precautionary savings. While the assumption is motivated by simplicity, see Keane and Wolpin (1997); Huggett, Ventura, and Yaron (2011); and Cunha, Heckman, and Schennach (2010) for evidence that the life-cycle income patterns tend to be determined early in life.

We emphasize that  $r$  and  $w$  are stochastic over generations only: agents face no uncertainty within their life span. Lifetime earnings profiles are hump-shaped, with low earnings early in life. Borrowing constraints limit how much agents can smooth lifetime earnings.

Let  $\beta < 1$  denote the discount rate. Let  $V_t(a_t)$  denote the present discounted utility of an agent with wealth  $a_t$  at the beginning of period  $t$ . Given initial wealth  $a_0$ , earnings profile  $w$ , and rate of return  $r$ , each agent's maximization problem, written recursively, then is

$$V_t(a) = \max_{c, a'} u(c) + \beta V_{t+1}(a')$$

subject to

$$a' = (1 + r)a - c + w,$$

$$0 \leq c \leq a, \quad t = 1, \dots, T - 1,$$

$$V_T(a) = u(c) + e(a').$$

The solution of the recursive problem can be represented by a map,

$$a_T = g(a_0; r, w).$$

Following Benhabib, Bisin, and Zhu (2011), we exploit the map  $g(\cdot)$  as the main building block to construct the stochastic wealth process across generations. Adding an apex  $n$  to indicate the generation and slightly abusing notation, we denote with  $\{r^n, w^n\}_n$  the stochastic process over generations for the rate of return on wealth  $r$  and earnings  $w$ . We assume it is a finite irreducible Markov chain. We assume also that  $r^n$  and  $w^n$  are independent, though each is allowed to be serially correlated, with transition  $P(r^n | r^{n-1})$  and  $P(w^n | w^{n-1})$ . The life-cycle structure of the model implies that the initial wealth of the  $n$ th generation coincides with the final wealth of the  $(n - 1)$ th generation:  $a^n = a_0^n = a_T^{n-1}$ . We can then construct a stochastic difference equation for the initial wealth of dynasties, induced by  $\{r^n, w^n\}_n$ , mapping  $a^{n-1}$  into  $a^n$ :

$$a^n = g(a^{n-1}; r^n, w^n).$$

This difference equation in turn induces a stochastic process  $\{a^n\}_n$  for initial wealth  $a$ .

It can be shown that, under our assumptions, the map  $g(\cdot)$  can be characterized as follows:

- If  $\mu = \sigma$ , then  $g(a_0; r, w) = \alpha(r, w)a_0 + \beta(r, w)$ ;
- If  $\mu < \sigma$ , then  $\frac{\partial^2 g}{\partial a_0^2}(a_0; r, w) > 0$ .

In the first case,  $\mu = \sigma$ , the savings rate is  $\alpha(r, w)$  and it is independent of wealth. In this case, the wealth process across generations is represented then by a linear stochastic difference equation in wealth, which has been closely studied in the math literature (see De Saporta 2005). Indeed, if  $\mu = \sigma$ , under general conditions,<sup>9</sup> the stochastic process  $\{a^n\}_n$  has a stationary distribution whose tail is independent of the distribution of earnings and asymptotic to a Pareto law,

$$\Pr(a > \underline{a}) \sim Q\underline{a}^{-\gamma},$$

where  $Q \geq 1$  is a constant and  $\lim_{N \rightarrow \infty} E\left(\prod_{n=0}^{N-1} (\alpha(r^{-n}, w^{-n}))^\gamma\right)^{\frac{1}{N}} = 1$ .<sup>10</sup>

If instead, keeping  $\sigma$  constant,  $\mu < \sigma$ , differential savings rate emerge, increasing with wealth. In this case, a stationary distribution might not exist; but if it does,

$$\Pr(a > \underline{a}) \geq Q\underline{a}^{-\gamma},$$

and hence it displays a thick tail.

Finally, the model is straightforwardly extended to allow for the Markov states of the stochastic process for  $r$  to depend on the initial wealth of the agent  $a$ . In this case, the intergenerational wealth dynamics have properties similar to the  $\mu < \sigma$  case: a stationary distribution might not exist; but if it does, it displays a thick tail.

## II. Quantitative Analysis

The objective of this paper, as we discussed in the introduction, consists in measuring the relative importance of various factors which determine the wealth distribution and the social mobility matrix in the United States. The three factors are stochastic earnings, differential saving and bequest rates across wealth levels, and stochastic returns on wealth. These are represented in the model by the properties of the dynamic process and the distribution of  $(r^n, w^n)$  and by the parameters  $\mu$  and  $\sigma$ , which imply differential savings (the rich saving more) when  $\mu < \sigma$ .

### A. Methodology

We estimate the parameters of the model described in the previous section using a method of simulated moments (MSM) estimator: (i) we fix (or externally calibrate) several parameters of the model; (ii) we select some relevant moments of the wealth process as target in the estimation; and (iii) we estimate the remaining parameters by matching the targeted moments generated by the stationary distribution induced by the model and those in the data. The quantitative exercise is predicated then on

<sup>9</sup>More precisely, the tail of earnings must be not too thick and furthermore  $\alpha(r^n, w^n)$  and  $\beta(r^n, w^n)$  must satisfy the restrictions of a *reflective process*. See Grey (1994); Hay, Rastegar, and Roitershtein (2011); and Benhabib, Bisin, and Zhu (2011) for a related application.

<sup>10</sup>While  $a$  denotes initial wealth, it can be shown that when the distribution of initial wealth has a thick tail, the distribution of wealth also does. See Benhabib, Bisin, and Zhu (2011) for the formal result.

the assumption that the wealth and social mobility observed in the data are generated by a stationary distribution.<sup>11</sup>

More formally, let  $\theta$  denote the vector of the parameters to be estimated. Let  $m_h$ , for  $h = 1, \dots, H$ , denote a generic empirical moment; and let  $d_h(\theta)$  the corresponding moment generated by the model for a given parameter vector  $\theta$ . We minimize the deviation between each targeted moment and the corresponding simulated moment. For each moment  $h$ , define  $F_h(\theta) = d_h(\theta) - m_h$ . The MSM estimator is

$$\hat{\theta} = \arg \min_{\theta} \mathbf{F}(\theta)' \mathbf{W} \mathbf{F}(\theta)$$

where  $\mathbf{F}(\theta)$  is a column vector in which all moment conditions are stacked, i.e.,  $\mathbf{F}(\theta) = [F_1(\theta), \dots, F_H(\theta)]^T$ . The weighting matrix  $\mathbf{W}$  in the baseline is a diagonal matrix with identical weights for all but the last moment of both the wealth distribution and the mobility moments, which are overweighted (ten times), according to the prior that matching the tail of the distribution is a fundamental objective of our exercise.<sup>12</sup> This is also a reasonable approximation to optimal weighting: an efficient two-step estimation with the optimal weighting matrix produces no relevant changes on estimated parameters nor on fit; see online Appendix C.4 for details.

The model is solved with the *collocation method* by Miranda and Fackler (2004): see online Appendix A.1. The objective function is highly nonlinear in general and therefore, following Guvenen (2016), we employ a global optimization routine for the MSM estimation: see online Appendix A.2.

In our quantitative exercise we proceed as follows.

- (i) We fix  $\sigma = 2$ ,  $T = 36$ ,  $\beta = 0.97$  per annum. We feed the model with a stochastic process for individual earnings profiles,  $w^n$ , and its transition across generations,  $P(w^n | w^{n-1})$ . Both the earning process and its transition are taken from data; respectively from the PSID and the federal income tax records studied by Chetty et al. (2014).
- (ii) We target as moments:
  - the bottom 20 percent, 20–40 percent, 40–60 percent, 60–80 percent, 80–90 percent, 90–95 percent, 95–99 percent, and the top 1 percent wealth shares; and
  - the diagonal of the (age-independent) social mobility Markov chain transition matrix defined over quintiles.
- (iii) We estimate:
  - preference parameters  $\mu, A$ ; and

<sup>11</sup>Very few studies in the literature deal with the transitional dynamics of wealth and its speed of transition along the path, though this issue has been put at the forefront of the debate by Piketty (2014). Notable and very interesting exceptions are Gabaix et al. (2016); Kaymak and Poschke (2016); and Hubmer, Krusell, and Smith (2017). We extend the analysis to possibly nonstationary distributions in Section V as a robustness check. Our preliminary results are encouraging, in the sense that the model seems to be able to capture the transitional dynamics with parameters estimates not too far from those obtained under stationarity.

<sup>12</sup>See Altonji and Segal (1996) for a justification for the adoption of an identity weighting matrix.

TABLE 1—LIFE-CYCLE EARNINGS (\$THOUSANDS) PROFILES

| Percentile | Age range |         |         |         |         |         |
|------------|-----------|---------|---------|---------|---------|---------|
|            | [25–30]   | [31–36] | [37–42] | [43–48] | [49–54] | [55–60] |
| 0–10       | 9.760     | 11.55   | 12.06   | 12.81   | 11.74   | 8.222   |
| 10–20      | 19.95     | 24.01   | 25.2    | 26.42   | 24.66   | 19.08   |
| 20–30      | 26.85     | 32.58   | 34.96   | 36.46   | 33.56   | 26.78   |
| 30–40      | 33.05     | 40.33   | 43.95   | 45.55   | 42.23   | 34.39   |
| 40–50      | 39.02     | 47.70   | 52.42   | 54.37   | 51.18   | 42.96   |
| 50–60      | 45.05     | 54.84   | 60.70   | 63.09   | 60.34   | 51.91   |
| 60–70      | 51.40     | 65.10   | 69.42   | 72.89   | 70.63   | 61.65   |
| 70–80      | 59.16     | 73.06   | 80.37   | 85.09   | 82.78   | 74.35   |
| 80–90      | 70.33     | 87.21   | 97.51   | 103.5   | 101.4   | 93.42   |
| 90–100     | 100.3     | 138.1   | 169.5   | 182.4   | 183.4   | 180.4   |

Source: Calculated from the cleaned PSID data provided by Heathcote, Perri, and Violante (2010).

- a parameterization of the stochastic process for  $r$  defined by 5 states  $r_i$  and 5 diagonal transition probabilities,  $P(r^n = r_i | r^{n-1} = r_i)$ ,  $i = 1, \dots, 5$ , restricting instead the  $5 \times 5$  transition matrix to display constantly decaying off-diagonal probabilities except for the last row for which we assume constant off-diagonal probabilities.<sup>13</sup>

In total, therefore, the baseline model is exactly identified: we target 12 moments and we estimate 12 parameters.

In Section IIID we modify the stochastic process for  $r$  to allow returns to depend on the initial wealth  $a$  of the agent. We do this parsimoniously, without increasing the dimensionality of the parameter space. In Section IIID we experiment with an alternative social mobility matrix, defined over the same percentiles of the wealth distribution. This adds three moments to the estimation and the model is hence over-identified.

## B. Data

Our quantitative exercise requires data for labor earnings, wealth distribution, and social mobility.

*Labor Earnings.*—We use ten deterministic life-cycle household-level earnings profiles at different deciles, as estimated by Heathcote, Perri, and Violante (2010) from the Panel Study of Income Dynamics (PSID), 1967–2002.<sup>14</sup> We construct the profiles as follows. For each of six age brackets we compute the averages of the earnings deciles, corresponding to the columns of Table 1. The deterministic lifetime profiles are then constructed assuming agents stay in the same decile for their

<sup>13</sup>Formally,  $P(r^n = r_i | r^{n-1} = r_j) = P(r^n = r_i | r^{n-1} = r_i)e^{-\lambda_j}$ ,  $i = 1, 2, 3, 4$ ,  $j \neq i$ ,  $\lambda$  such that  $\sum_{j=1}^5 P(r^n = r_i | r^{n-1} = r_j) = 1$ ; and  $P(r^n = r_5 | r^{n-1} = r_j) = \frac{1}{4}(1 - P(r^n = r_5 | r^{n-1} = r_5))$ . We adopt a restricted specification in order to reduce the number of parameters we need to estimate. This particular specification performs better than one with constant off-diagonal probabilities as well as one with decaying off-diagonal probabilities in all rows.

<sup>14</sup>We detrend life-cycle earning profiles by conditioning out year dummies in a log-earnings regression; see online Appendix B.1 for the details of the procedure.

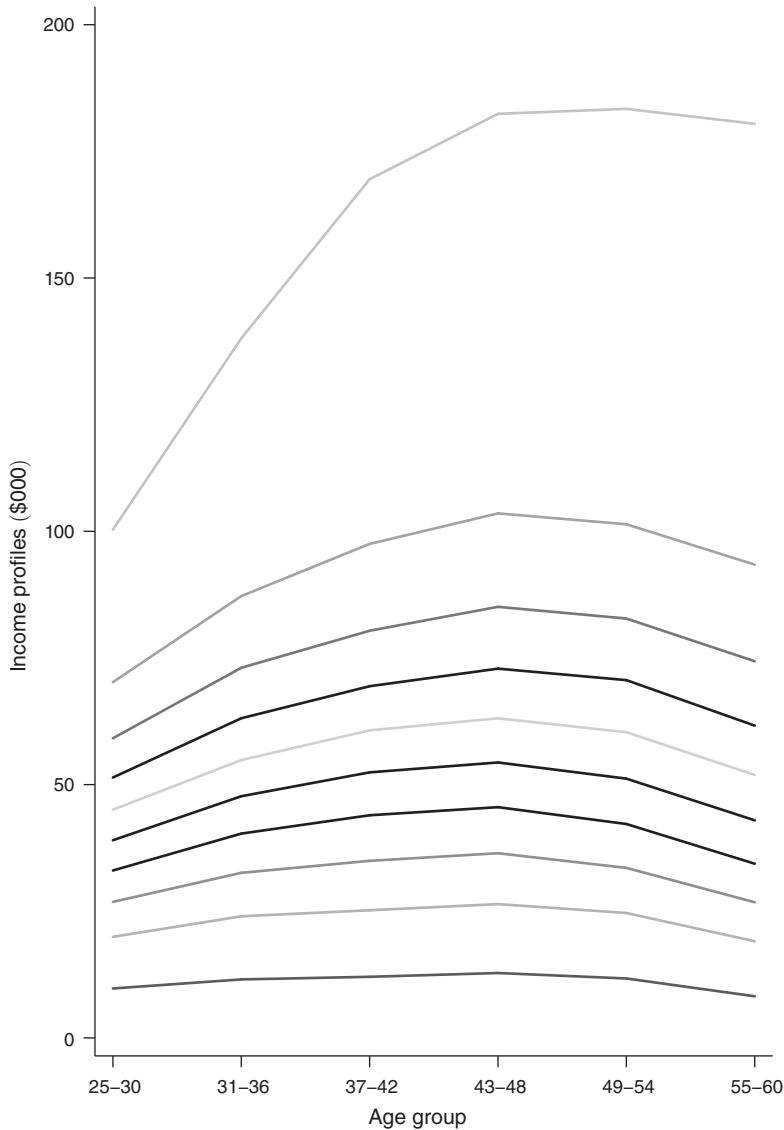


FIGURE 1. LIFE-CYCLE EARNINGS PROFILES BY DECILES

Source: The data source is the same as in Table 1.

whole lifetime, corresponding to the ten rows of Table 1. Agents randomly draw one of these earnings profiles at the beginning of life according to an intergenerational transition matrix. These profiles are drawn in Figure 1.<sup>15</sup>

<sup>15</sup>The panel data on earnings from the US Social Security Administration (SSA) are not yet generally available. However, the crucial aspect of earnings data, for our purposes, is that they are far from skewed enough to account by themselves for the skewness of the wealth distribution. This is in fact confirmed on SSA data directly by Guvenen et al. (2016, Section 7.2.II) and by De Nardi, Fella, and Paz-Pardo (2016). See also Hubmer, Krusell, and Smith (2017).



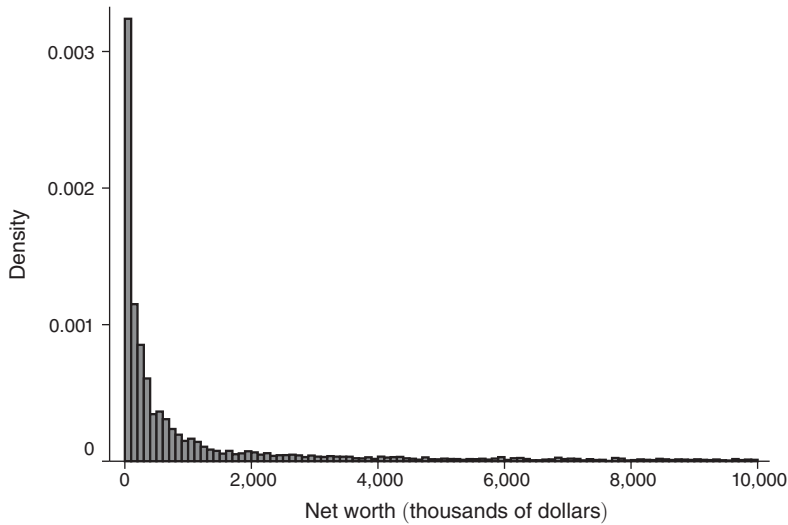


FIGURE 2. WEALTH DISTRIBUTION IN THE SCF 2007 (WEIGHTED)

Source: Net wealth, from 2007 SCF, truncated at 0 on the left and, for the purpose of the figure only, truncated at 10 million on the right.

The intergenerational transition matrix for earnings we use is from Chetty et al. (2014). The data in Chetty et al. (2014) refer to the 1980–1982 US birth cohort and their parental income. We reduce it to a ten-state Markov chain.<sup>16</sup>

*Wealth Distribution.*—We use wealth distribution data from the Survey of Consumer Finances (SCF) 2007.<sup>17</sup> The wealth variable we use is *net wealth*, the sum of net financial wealth and housing, minus any debts. The distribution is very skewed to the right. We take the shares from the cleaned version in Díaz-Giménez, Glover, and Ríos-Rull (2011). Figure 2 displays the histogram of the wealth distribution.

Table 2 displays the wealth share moments we use.

*Social Mobility.*—As for wealth transition across generations, we use the mobility matrix calculated by Charles and Hurst (2003), Table 2, from PSID data. This matrix is constructed by means of pairs of simultaneously alive parent and child of different ages. To eliminate age effects, the matrix is obtained by computing transitions from the residuals of the wealth of parents and children after conditioning on age and age squared.

The resulting matrix is shown in Table 3. The matrix shows substantial mobility, with a Shorrocks index of 0.88.<sup>18</sup>

<sup>16</sup>See online Appendix B.2 for details.

<sup>17</sup>As noted, the wealth distribution in our methodology is to be interpreted as stationary. Choosing 2007 avoids the nonstationary changes due to the Great Recession.

<sup>18</sup>Formally, for a square mobility transition matrix  $A$  of dimension  $m$ , the Shorrocks index given by  $s(A) = \frac{m - \sum_j a_{jj}}{m - 1} \in (0, 1)$ , with 0 indicating complete immobility.

TABLE 2—WEALTH DISTRIBUTION MOMENTS

| Percentile   | 0–20   | 20–40 | 40–60 | 60–80 | 80–90 | 90–95 | 95–99 | 99–100 |
|--------------|--------|-------|-------|-------|-------|-------|-------|--------|
| Wealth share | –0.002 | 0.001 | 0.045 | 0.112 | 0.120 | 0.111 | 0.267 | 0.336  |

Source: Calculated by Díaz-Giménez, Glover, and Ríos-Rull (2011) from the 2007 SCF.

TABLE 3—INTERGENERATIONAL SOCIAL MOBILITY TRANSITION MATRIX

| Percentile (parent) | Percentile (child) |       |       |       |        |
|---------------------|--------------------|-------|-------|-------|--------|
|                     | 0–20               | 20–40 | 40–60 | 60–80 | 80–100 |
| 0–20                | 0.36               | 0.29  | 0.16  | 0.12  | 0.07   |
| 20–40               | 0.26               | 0.24  | 0.24  | 0.15  | 0.12   |
| 40–60               | 0.16               | 0.21  | 0.25  | 0.24  | 0.15   |
| 60–80               | 0.15               | 0.13  | 0.20  | 0.26  | 0.26   |
| 80–100              | 0.11               | 0.16  | 0.14  | 0.24  | 0.36   |

Source: From Table 2 in Charles and Hurst (2003). Note that we exchange the row and the column from their version.

In Section IIID we reproduce the estimation exercise in our baseline using an alternative social mobility matrix, using the 2007–2009 SCF panel data, with transitions computed for a synthetic agent over his/her age profile.<sup>19</sup>

### III. Estimation Results

The baseline estimation results are reported in Section IIIA, Table 4. The targeted simulated moments of the estimated model are reported and compared to their counterpart in the data in Section IIIB, Table 5. Some independent evidence which bears on the fit of the model is discussed in Section IIIC. Extensions where we re-estimate the model to allow for rates of return dependent on wealth and to match an alternative social mobility matrix constructed using the 2007–2009 SCF panel data are discussed, respectively, in Section IIID.

#### A. Parameter Estimates

The upper part of Table 4 reports the estimates of the preference parameters. The lower part of Table 4 reports the estimated state space and diagonal of the transition matrix of the five-state Markov process for  $r$  we postulate. It also reports, to ease the interpretation of the estimates, the implied mean and standard deviation of the process,  $E(r)$ ,  $\sigma(r)$ ; as well as its autocorrelation,  $\rho(r)$ , computed fitting an AR(1) on simulated data from the estimated process.<sup>20</sup> The standard errors, also reported in the table, are obtained by bootstrapping; details are in online Appendix A.3.

<sup>19</sup>In addition in online Appendix B.3, we also describe another alternative social mobility matrix based on the social mobility matrix of Kennickell and Starr-McCluer (1997) using the SCF panel 1983–1989.

<sup>20</sup>The full transition matrix for  $r$  is reported in online Appendix C.1.

TABLE 4—PARAMETER ESTIMATES: BASELINE

|                     | Preferences                |                                 |                               |                    |                    |
|---------------------|----------------------------|---------------------------------|-------------------------------|--------------------|--------------------|
|                     | $\sigma$                   | $\mu$                           | $A$                           | $\beta$            | $T$                |
|                     | [2]                        | 0.5993<br>(0.0061)              | 0.0006<br>(0.0004)            | [0.97]             | [36]               |
|                     | Rate of return process     |                                 |                               |                    |                    |
| State space         | 0.0011<br>(0.0069)         | 0.0094<br>(0.0118)              | 0.0258<br>(0.0004)            | 0.0560<br>(0.0059) | 0.0841<br>(0.0043) |
| Transition diagonal | 0.0338<br>(0.6162)         | 0.2676<br>(0.5570)              | 0.1360<br>(0.0699)            | 0.2630<br>(1.3659) | 0.0208<br>(0.2678) |
| Statistics          | $E(r)$<br>3.06%<br>(0.02%) | $\sigma(r)$<br>2.69%<br>(0.01%) | $\rho(r)$<br>0.103<br>(0.486) |                    |                    |

Note: Standard errors in parentheses; fixed parameters in brackets.

TABLE 5—MODEL FIT: BASELINE

| Percentile                  | Wealth distribution |       |       |       |        |       |       |        |
|-----------------------------|---------------------|-------|-------|-------|--------|-------|-------|--------|
|                             | 0–20                | 20–40 | 40–60 | 60–80 | 80–90  | 90–95 | 95–99 | 99–100 |
| Wealth share (data)         | –0.002              | 0.001 | 0.045 | 0.112 | 0.120  | 0.111 | 0.267 | 0.336  |
| Wealth share (model)        | 0.049               | 0.077 | 0.111 | 0.110 | 0.110  | 0.076 | 0.142 | 0.325  |
| Percentile                  | Social mobility     |       |       |       |        |       |       |        |
|                             | 0–20                | 20–40 | 40–60 | 60–80 | 80–100 |       |       |        |
| Transition diagonal (data)  | 0.36                | 0.24  | 0.25  | 0.26  | 0.36   |       |       |        |
| Transition diagonal (model) | 0.349               | 0.197 | 0.201 | 0.210 | 0.340  |       |       |        |

The curvature parameter  $\mu$  is statistically significant, while the bequest intensity parameter  $A$  is small and less precisely estimated. As for the rate of return process  $r$ , while some of the elements of the state space and of the transition diagonal, individually taken, are statistically insignificant, the mean  $E(r)$  and the variance  $\sigma(r)$  of the rate of return process are significant. The correlation  $\rho(r)$  is not surprisingly also imprecisely estimated (because the transition matrix is in-and-of itself imprecisely estimated and because the auto-correlation parameter is not a statistic pertaining directly to the  $r$  process but is estimated by fitting an AR(1) process on simulated data). A Quandt likelihood ratio (QLR) test against the null hypothesis that the rate of return process is a constant  $r$  squarely rejects the null.

### B. Model Fit

The simulations of our estimated model seem to capture the targeted moments reasonably well. Table 5 compares the moments in the data with those obtained simulating the model. In the case of social mobility, we compute age-independent social mobility moments, in the simulations, after conditioning on age and age-squared, thereby reproducing Charles and Hurst's (2003) procedure to construct their social mobility matrix which we use as moments to match in the data.

### C. Discussion and Interpretation

We discuss and interpret here the estimates we obtain. We also put them in the context of independent evidence which bears on nontargeted moments regarding savings, bequests, rates of return, and wealth mobility.

*Differential Savings and Bequests.*—Our estimates point to the existence of the differential saving factor as a component of the observed wealth dynamics in the United States. Indeed, our estimate of  $\mu$  is 0.5993, which is significantly lower than 2, the value of  $\sigma$  we fixed; therefore  $\mu < \sigma$  and, as we noted, savings out of wealth increase with wealth itself: the rich save proportionally more than the poor.

Of course, the strength of this factor depends on the intensity parameter  $A$  as well. To better evaluate the quantitative role of differential savings and bequests in our estimation, we calculate the average savings rates implied by our model at the estimated parameters and compare them with the empirical values calculated by Saez and Zucman (2016) using 2000–2009 data on wealth accumulation with the capitalized income tax method: see Table 6. Interestingly, the implied (year-to-year synthetic) savings rate schedule shares its main characteristic feature with the one reported by Saez and Zucman (2016): it is very steep (even steeper in fact). Rates range from slightly negative (–3.4 percent of the bottom 90 percent) to 45 percent for the top 1 percent of the population.

To gain a more precise sense of the mechanism driving differential savings, we also look at bequests, since in our model differential savings are mostly motivated by a bequest motive.<sup>21</sup> The distribution of bequests implied by our model at the estimated parameters is very skewed, mapping closely the stationary wealth distribution. This is consistent with Health Retirement Survey (HRS) data studied by Hurd and Smith (2003). In particular, retirement savings in the data do not decline along the age path and, furthermore, this pattern is more accentuated for the 75 percent percentile, as our estimates also imply.<sup>22</sup> Bequests implied by the model are about 18.9 percent of GDP, substantially higher than its empirical counterpart: Wang (2016) estimates them to be between 2.4 percent to 4.7 percent of GDP, using the HRS data (see also Hendricks 2002). On the other hand, bequests in the model should more correctly be interpreted to include at least part of inter vivos transfers, which can account for the difference. Indeed, Cox (1990) and Gale and Scholz (1994) estimate inter vivos transfer to be about the same order of magnitude as bequests, while Luo (2017), working with SCF (2013) data, has them close to 13 percent of GDP.

*Returns to Wealth.*—The wealth accumulation process in our estimates indicates a substantial role of capital income risk as a factor driving wealth and mobility. Indeed the rate of return on wealth displays a standard deviation which is significantly

<sup>21</sup> The bequest motive stands on relative solid grounds: it is well documented that retirees do not run down their wealth as predicted by the classical life-cycle consumption-savings model (Poterba, Venti, and Wise 2011).

<sup>22</sup> Our model does not have a role for accidental bequests. Therefore, while the literature on retirement savings distinguishes between precautionary saving motives for uncertain medical expenses (De Nardi et al. 2010), uncertain and potentially large long-term care expenses (Ameriks et al. 2015a), family needs (Ameriks et al. 2015b), and the genuine bequest motive, we necessarily lump all these into aggregate bequests.

TABLE 6—SAVINGS RATES

| Wealth percentile                           | 0–90  | 90–99 | 99–100 |
|---|-------|-------|--------|
| Savings rate percent (model)                | –3.40 | 21.4  | 45.0   |
| Savings rate percent (Saez and Zucman 2016) | –4    | 9     | 35     |

different than 0. The standard deviation  $\sigma(r) = 2.69$  percent is however smaller than previous direct estimates. This is the case, e.g., for the return estimates by Case and Shiller (1989) and Flavin and Yamashita (2002) on the housing market, by Campbell and Lettau (1999) and Campbell et al. (2001) on individual stocks of publicly traded firms, and by Moskowitz and Vissing-Jørgensen (2002) on private equity and entrepreneurship. A wide dispersion in returns to wealth is also documented by Fagereng et al. (2017) and Bach, Calvet, and Sodini (2017) using, respectively, Norwegian and Swedish data.

Such comparisons require however great caution. First of all, in our model,  $r$  is assumed constant throughout each agent's lifetime, disregarding the whole variation across the life cycle. The rate of return we estimate should ideally be then compared with the permanent components of individual returns across generations, which are hardly available. Furthermore, rate of returns heterogeneity in the data is in part a consequence of differences in the risk composition of investment portfolio, which also we disregard in the model; see Calvet and Sodini (2014) and Bach, Calvet, and Sodini (2017) for evidence in Swedish data. For our purposes, therefore, the most appropriate outside validation perspective is provided by Fagereng et al. (2017), in that their Norwegian administrative data allow them to estimate the permanent components of individual returns across generations and to control for portfolio composition. In this comparison, the consistency of our estimates with Fagereng et al.'s (2017) data is striking: see Table 7.<sup>23</sup>

*Social Mobility.*—Table 8 is the complete transition matrix we obtain from our estimate. The implied nontargeted moments (the off-diagonal cells) align quite well with the mobility matrix in Charles and Hurst (2003, Table 2), reported here in Table 3. Note that we slightly overestimate the mobility from the top to the bottom of the distribution and vice versa. The Shorrocks index in the estimated mobility matrix is 0.92, slightly higher than the 0.88 in the data.

#### D. Extensions and Robustness

In this section we discuss alternative estimation strategies we have pursued as extensions and robustness checks on our baseline analysis.

*Rate of Return Dependent on Wealth.*—A positive correlation between the rate of return on wealth and wealth has been documented by Piketty's (2014, see especially p. 447) analysis of university endowments, and by Fagereng et al.'s (2017) careful

<sup>23</sup>Fagereng et al. (2017) also find rate of returns increasing in wealth. We shall discuss this in the next section.

TABLE 7—RATE OF RETURN PROCESS

| Statistics             | $E(r)$ | $\sigma(r)$ | $\rho(r)$ |
|------------------------|--------|-------------|-----------|
| Model estimates        | 3.06%  | 2.69%       | 0.103     |
| Fagereng et al. (2017) | 2.98%  | 2.82%       | 0.1       |

*Note:* Fagereng et al.'s (2017) permanent component has zero-mean by construction: we report their mean of returns.

TABLE 8—INTERGENERATIONAL SOCIAL MOBILITY TRANSITION MATRIX: CALIBRATED

| Percentile (parent) | Percentile (child) |       |       |       |        |
|---------------------|--------------------|-------|-------|-------|--------|
|                     | 0–20               | 20–40 | 40–60 | 60–80 | 80–100 |
| 0–20                | 0.349              | 0.216 | 0.197 | 0.131 | 0.108  |
| 20–40               | 0.175              | 0.197 | 0.245 | 0.233 | 0.149  |
| 40–60               | 0.180              | 0.193 | 0.201 | 0.253 | 0.173  |
| 60–80               | 0.151              | 0.207 | 0.201 | 0.210 | 0.231  |
| 80–100              | 0.150              | 0.183 | 0.157 | 0.171 | 0.340  |

study of Norwegian administrative data.<sup>24</sup> Such a correlation of course does not imply that the rate of return increases with wealth. Even in the context of our model, agents with relatively high wealth would have experienced on average high realizations of the rate of return  $r$ , as shown in Figure 3. Indeed, for the simulated model at the parameters estimates in the previous section, a fractile regression between  $r$  and wealth  $a$  produces a small but strongly significant coefficient of 0.010 (standard error 0.0004).

Allowing rates of return on wealth to be increasing in wealth might however add to the skewness of the distribution. In this section we therefore extend our analysis to allow for the rate of return process  $r$  to depend on wealth, explicitly introducing a dependence of the stochastic rate of return  $r$  on wealth percentiles. The functional form we introduce allows for  $r$  to depend on wealth  $a$  as follows:

$$(1) \quad r = r_0 + b \times p(a),$$

where  $p(a) = 1, 2, \dots, 8$  numbers the wealth percentiles we identify as moments and  $r_0$  is a five-state Markov process as in the baseline model for  $r$ . Note that this formulation maps a positive slope  $b$  into a convex relationship between  $r$  and  $a$ .<sup>25</sup> We restrict the parameter space by fixing the distance between the two lowest estimates of  $r_0$  to that of the baseline, so that the empirical model is again exactly identified as the baseline. We then estimate the parameters of the model as well as

<sup>24</sup>See also Kacperczyk, Nosal, and Stevens (2015). On the other hand, Saez and Zucman (2016) find no correlation between post-tax returns and wealth levels (see their online Appendix, Figures B30 and B31: <http://gabriel-zucman.eu/files/SaezZucman2016QJEAppendix.pdf>). Also, Bach, Calvet, and Sodini (2017) find that the correlation is largely due, in the Swedish administrative data they observe, to the portfolio composition by risk class changing with wealth.

<sup>25</sup>This formulation also implies a standard deviation for  $r$  which is increasing in wealth, as documented by Fagereng et al. (2017) for Norwegian data.

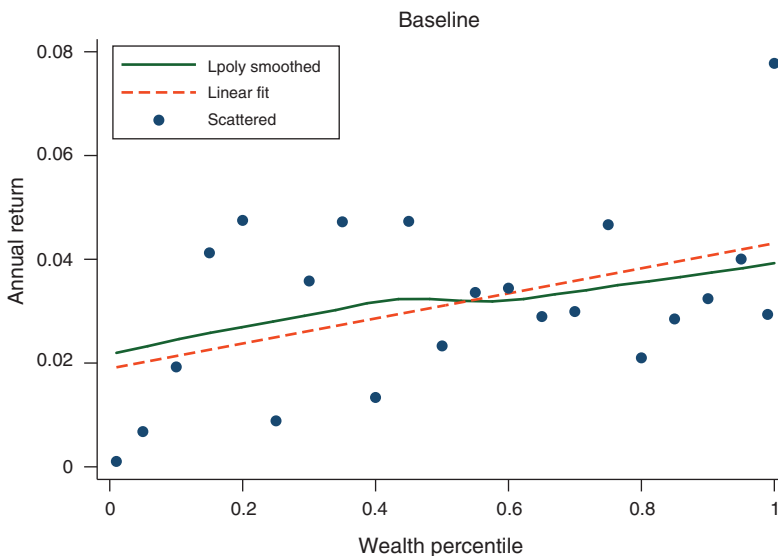


FIGURE 3. CORRELATION BETWEEN MEAN  $r$  AND WEALTH PERCENTILES

TABLE 9—PARAMETER ESTIMATES:  $r$  DEPENDENT ON WEALTH

|                        | Preferences                  |                                   |                                 |                    |                      |
|------------------------|------------------------------|-----------------------------------|---------------------------------|--------------------|----------------------|
|                        | $\sigma$<br>[2]              | $\mu$<br>1.0574<br>(0.0023)       | $A$<br>0.0080<br>(0.0007)       | $\beta$<br>[0.97]  | $T$<br>[36]          |
|                        | Rate of return process       |                                   |                                 |                    |                      |
| State space            | 0.0027<br>(0.0031)           | 0.0110<br>—                       | 0.0152<br>(0.0011)              | 0.0456<br>(0.0068) | 0.0815<br>(0.0072)   |
| Transitional diagonal  | 0.0328<br>(0.7044)           | 0.0469<br>(0.0730)                | 0.5953<br>(0.1448)              | 0.3344<br>(1.3415) | 0.1531<br>(0.0150)   |
| Wealth dependence, $b$ | 0.0043<br>(0.0255)           |                                   |                                 |                    |                      |
| Statistics             | $E(r_0)$<br>2.57%<br>(0.02%) | $\sigma(r_0)$<br>2.34%<br>(0.01%) | $\rho(r_0)$<br>0.153<br>(0.149) | $E(r)$<br>3.94%    | $\sigma(r)$<br>2.48% |

Note: Standard errors in parentheses; fixed parameters in brackets.

TABLE 10—MODEL FIT:  $r$  DEPENDENT ON WEALTH

| Percentile                  | Wealth distribution |       |       |       |        |       |       |        |
|-----------------------------|---------------------|-------|-------|-------|--------|-------|-------|--------|
|                             | 0–20                | 20–40 | 40–60 | 60–80 | 80–90  | 90–95 | 95–99 | 99–100 |
| Wealth share (data)         | –0.002              | 0.001 | 0.045 | 0.112 | 0.120  | 0.111 | 0.267 | 0.336  |
| Wealth share (model)        | 0.028               | 0.067 | 0.099 | 0.100 | 0.114  | 0.083 | 0.173 | 0.336  |
|                             | Social mobility     |       |       |       |        |       |       |        |
| Percentile                  | 0–20                | 20–40 | 40–60 | 60–80 | 80–100 |       |       |        |
| Transition diagonal (data)  | 0.36                | 0.24  | 0.25  | 0.26  | 0.36   |       |       |        |
| Transition diagonal (model) | 0.267               | 0.221 | 0.236 | 0.231 | 0.296  |       |       |        |

the wealth dependence parameter  $b$  that enters the stochastic rate of return process. The results of our estimation are reported in Tables 9 and 10.

The estimate of the preference for bequest parameter  $A$  is significant and larger than in the baseline case, where  $r$  is not allowed to depend on wealth. Most importantly, the estimate of  $\mu$  is also larger: allowing  $r$  to depend on wealth substitutes for the dependence of savings on wealth. The estimate of the parameter  $b$ , which captures the dependence of the rate of return on wealth is positive. The point estimate implies that going from the bottom 20 percent to the top 1 percent in the wealth distribution would increase the annual expected return by about 3 percentage points, from 3 percent to 6 percent. While  $b$  is unsurprisingly not well identified, it is reassuring that the point estimates of the preference parameters are not much changed when we allow for  $r$  to depend on wealth with respect to the baseline.

Furthermore, the fit of the wealth distribution is somewhat improved: while the distribution of wealth implied by the model is still less skewed than the data's, we improve match even more precisely the top 1 percent share and, most importantly, we improve in matching all shares in the top 20 percent (and correspondingly in the bottom 60 percent). With regards to social mobility, this specification loses fit on the top and the bottom 20 percent, producing mobility for both the rich and the poor marginally in excess of the baseline model (and the data), a result of the fact that the dependence of the rates of return on wealth is compensated by a reduced dependence of savings.<sup>26</sup>

Fagereng et al. (2017) also estimate the dependence of the rate of return  $r$  on wealth, their rich and detailed Norwegian dataset allowing them to do so precisely, directly controlling for the effects of a variety of factors like age, education, and portfolio composition. Their findings provide stronger evidence of dependence than ours, with average returns within generations more significantly increasing in wealth: see their Figure 11(b). In particular, they document a very steep increase of  $r(a)$  at the top, which we cannot precisely identify with our data.

*Alternative Social Mobility Matrix.*—The Charles and Hurst (2003) social mobility matrix we use in our baseline estimation, as we noted, is constructed by means of pairs of simultaneously alive parents and child. By construction, therefore, this mobility matrix does not account for any transition induced by bequests. Furthermore, the matrix is only available for wealth transitions between quintiles, while, e.g., transitions in and out of the top 1 percent are in principle one of the most relevant characteristics of the stochastic process of wealth accumulation.

In this section we reproduce the estimation exercise in our baseline using an alternative social mobility matrix, with transitions computed for a synthetic agent over his/her age profile. More precisely, each element of the social mobility matrix takes the form of  $\Pr(a_0^n \in p | a_0^{n-1} \in p')$ , where  $p, p'$  are generic percentiles of the wealth distribution. Using the model assumption that  $a_0^n = a_T^{n-1}$  we can reduce these intergenerational transition probabilities into intra-generational ones and reduce the problem to compute  $\Pr(a_T^{n-1} \in p | a_0^{n-1} \in p')$ . We then divide agents' lifetime  $T$  into  $k$ -periods age groups and use the Markov assumption to obtain

<sup>26</sup>See online Appendix C.3 for the complete estimated social mobility matrix.



TABLE 11—INTERGENERATIONAL SOCIAL MOBILITY TRANSITION MATRIX

| Percentile (parent) | Percentile (child) |       |       |       |       |       |       |        |
|---------------------|--------------------|-------|-------|-------|-------|-------|-------|--------|
|                     | 0–20               | 20–40 | 40–60 | 60–80 | 80–90 | 90–95 | 95–99 | 99–100 |
| 0–20                | 0.223              | 0.222 | 0.215 | 0.187 | 0.081 | 0.038 | 0.029 | 0.006  |
| 20–40               | 0.221              | 0.220 | 0.215 | 0.188 | 0.082 | 0.039 | 0.029 | 0.006  |
| 40–60               | 0.208              | 0.209 | 0.210 | 0.194 | 0.090 | 0.046 | 0.036 | 0.008  |
| 60–80               | 0.199              | 0.201 | 0.207 | 0.198 | 0.095 | 0.052 | 0.040 | 0.009  |
| 80–90               | 0.175              | 0.178 | 0.197 | 0.207 | 0.110 | 0.067 | 0.054 | 0.012  |
| 90–95               | 0.182              | 0.184 | 0.200 | 0.205 | 0.106 | 0.062 | 0.050 | 0.011  |
| 95–99               | 0.125              | 0.125 | 0.166 | 0.216 | 0.141 | 0.114 | 0.094 | 0.021  |
| 99–100              | 0.086              | 0.084 | 0.142 | 0.228 | 0.170 | 0.143 | 0.121 | 0.028  |

$\Pr(a_T^{n-1} \in p | a_0^{n-1} \in p')$  from the observation of  $\Pr(a_k^{n-1} \in p | a_0^{n-1} \in p')$ ,  $\Pr(a_{2k}^{n-1} \in p | a_k^{n-1} \in p')$  and so on for all age groups. In practice, from the 2007–2009 SCF two-year panel,<sup>27</sup> and in we first construct age-dependent two-year transition matrices for age groups running from 30–31 to 66–67.<sup>28</sup> We then multiply these age-dependent two-year transition matrices for all age groups, to construct the intergenerational social mobility matrix.

The matrix we obtain with this procedure accounts for the wealth transitions along the whole working life of agents and, as a consequence, it accounts for any transition induced by bequests (as well as in vivos transfers) the agents receive in this period. Furthermore, transitions are computed for the same percentiles we use as wealth distribution moments. On the other hand, this alternative approach to social mobility might produce spurious mobility due to measurement error in wealth.<sup>29</sup>

We report the alternative social mobility matrix we construct in Table 11.

Indeed it displays substantial social mobility, more than the Charles and Hurst (2003) matrix used in our baseline: the Shorrocks mobility index is 0.98 (against 0.88 in the baseline).<sup>30</sup>

Re-estimating the model adopting this mobility matrix, we obtain the parameter estimates in Table 12.

Very interestingly, the estimates are quite close to those we obtain in the baseline. Furthermore, the same can be said for the fit: see Table 13.

We match quite accurately the larger set of social mobility moments we target from this alternative matrix we constructed: importantly, in the top 10 percent of the distribution, while we overestimate the probability of staying in the top 1 percent, we underestimate the probability of staying in the 90–99 percent.<sup>31</sup>

<sup>27</sup>We should note that the 2007–2009 period is one of substantial wealth destruction, in the stock and real estate markets. This is at issue with our stationarity assumption. We thank an anonymous referee for this observation.

<sup>28</sup>Because of limited sample dimension, we average the left and right matrices obtained using, respectively, the left-middle ages and the middle-right ages to define the age group in the two-year panel; for instance, the 30–31 age group is constructed using the average of the transitions of the 29–30 and the 31–32 groups in the data.

<sup>29</sup>Jappelli and Pistaferri (2006) discuss this issue with regards to consumption mobility and account explicitly for measurement error in the analysis: see also Biancotti, D'Alessio, and Neri (2008).

<sup>30</sup>The qualitative properties of social mobility we obtain are similar to those we obtain exploiting, by means of a related methodology, Kennickell and Starr-McCluer's (1997) 6-year transition matrix from SCF (1983–1989); see online Appendix B.3 for details. The alternative matrix we construct, besides using more recent data, exploits the more precise information contained in age-dependent transitions.

<sup>31</sup>See online Appendix C.3 for the complete estimated social mobility matrix.

TABLE 12—PARAMETER ESTIMATES: ALTERNATIVE MOBILITY MATRIX

|                     | Preferences                |                                 |                               |                    |                    |
|---------------------|----------------------------|---------------------------------|-------------------------------|--------------------|--------------------|
|                     | $\sigma$<br>[2]            | $\mu$<br>0.5653<br>(0.0260)     | $A$<br>0.0004<br>(0.0002)     | $\beta$<br>[0.97]  | $T$<br>[36]        |
|                     | Rate of return process     |                                 |                               |                    |                    |
| State space         | 0.0010<br>(0.0001)         | 0.0087<br>(0.0013)              | 0.0253<br>(0.0019)            | 0.0532<br>(0.0123) | 0.0850<br>(0.0062) |
| Transition diagonal | 0.0224<br>(0.3189)         | 0.2698<br>(0.6096)              | 0.1371<br>(0.0710)            | 0.2746<br>(0.1463) | 0.0224<br>(0.2672) |
| Statistics          | $E(r)$<br>3.00%<br>(0.85%) | $\sigma(r)$<br>2.68%<br>(0.51%) | $\rho(r)$<br>0.175<br>(0.166) |                    |                    |

Note: Standard errors in parentheses; fixed parameters in brackets.

TABLE 13—MODEL FIT: ALTERNATIVE MOBILITY MATRIX

| Percentile                  | 0–20   | 20–40 | 40–60 | 60–80 | 80–90 | 90–95 | 95–99 | 99–100 |
|-----------------------------|--------|-------|-------|-------|-------|-------|-------|--------|
| <i>Wealth distribution</i>  |        |       |       |       |       |       |       |        |
| Wealth share (data)         | –0.002 | 0.001 | 0.045 | 0.112 | 0.120 | 0.111 | 0.267 | 0.336  |
| Wealth share (model)        | 0.047  | 0.074 | 0.107 | 0.102 | 0.105 | 0.071 | 0.155 | 0.339  |
| <i>Social mobility</i>      |        |       |       |       |       |       |       |        |
| Transition diagonal (data)  | 0.223  | 0.220 | 0.210 | 0.198 | 0.110 | 0.062 | 0.094 | 0.028  |
| Transition diagonal (model) | 0.228  | 0.207 | 0.200 | 0.193 | 0.102 | 0.048 | 0.047 | 0.036  |

#### IV. Counterfactual Estimates

In this section we perform a set of counterfactual estimations of the model, under restricted conditions. More in detail, we perform three sets of counterfactuals, corresponding to shutting down each of the three main factors which can drive the distribution of wealth: (i) capital income risk, (ii) stochastic earnings, and (iii) differential savings rates.

The objective of this counterfactual analysis is twofold. First of all we aim at gauging the relative importance of the various mechanisms we identified as possibly driving the distribution of wealth. In particular, we aim at a better understanding of which mechanism mostly affects which dimension of the wealth distribution and mobility. Second, we interpret the counterfactuals as informal tests of identification of these mechanisms, lack of identification implying that shutting down one or more of the mechanism has limited effects on the fit for the targeted moments.

##### A. Re-Estimation Results

We examine the counterfactual estimates in detail in the following. The estimated parameters are in Table 14.<sup>32</sup> Table 15 reports the fit of the estimates.

<sup>32</sup>We report only the mean, standard deviation, and auto-correlation statistics for  $r$ , to save space. The estimates for the state space and the diagonal of the transition matrix are in online Appendix C.2. In online Appendix C.3 we report the complete estimated social mobility matrices.

TABLE 14—PARAMETER ESTIMATES: COUNTERFACTUALS

|              | Preferences |                    |                    |         |      |
|--------------|-------------|--------------------|--------------------|---------|------|
|              | $\sigma$    | $\mu$              | $A$                | $\beta$ | $T$  |
| Baseline     | [2]         | 0.5993<br>(0.0061) | 0.0006<br>(0.0004) | [0.97]  | [36] |
| Constant $r$ | [2]         | 0.5827<br>(0.2204) | 0.0012<br>(0.5436) | [0.97]  | [36] |
| Constant $w$ | [2]         | 0.5300<br>(0.0140) | 0.0055<br>(0.0011) | [0.97]  | [36] |
| $\mu = 2$    | [2]         | 2<br>—             | 0.0360<br>(0.0779) | [0.97]  | [36] |

|              | Rate of return process |                  |                  |
|--------------|------------------------|------------------|------------------|
|              | $E(r)$                 | $\sigma(r)$      | $\rho(r)$        |
| Baseline     | 3.06%<br>(0.02%)       | 2.69%<br>(0.01%) | 0.103<br>(0.486) |
| Constant $r$ | 2.89%<br>(0.95%)       |                  |                  |
| Constant $w$ | 3.26%<br>(0.01%)       | 2.11%<br>(0.01%) | 0.222<br>(0.218) |
| $\mu = 2$    | 3.03%<br>(0.02%)       | 3.07%<br>(0.02%) | 0.072<br>(0.180) |

Note: Standard errors in parentheses; fixed parameters in brackets.

TABLE 15—MODEL FIT: COUNTERFACTUALS

| Percentile           | Wealth distribution |       |       |       |       |       |       |        |
|----------------------|---------------------|-------|-------|-------|-------|-------|-------|--------|
|                      | 0–20                | 20–40 | 40–60 | 60–80 | 80–90 | 90–95 | 95–99 | 99–100 |
| Wealth share (data)  | –0.002              | 0.001 | 0.045 | 0.112 | 0.120 | 0.111 | 0.267 | 0.336  |
| Wealth share (model) |                     |       |       |       |       |       |       |        |
| 1. Baseline          | 0.049               | 0.077 | 0.111 | 0.110 | 0.110 | 0.076 | 0.142 | 0.325  |
| 2. Constant $r$      | 0.055               | 0.087 | 0.129 | 0.184 | 0.128 | 0.116 | 0.148 | 0.153  |
| 3. Constant $w$      | 0.002               | 0.008 | 0.057 | 0.191 | 0.171 | 0.126 | 0.186 | 0.259  |
| 4. $\mu = 2$         | 0.069               | 0.111 | 0.160 | 0.230 | 0.159 | 0.106 | 0.119 | 0.046  |

| Percentile                  | Social mobility |       |       |       |        |
|-----------------------------|-----------------|-------|-------|-------|--------|
|                             | 0–20            | 20–40 | 40–60 | 60–80 | 80–100 |
| Transition diagonal (data)  | 0.349           | 0.197 | 0.201 | 0.210 | 0.340  |
| Transition diagonal (model) |                 |       |       |       |        |
| 1. Baseline                 | 0.349           | 0.197 | 0.201 | 0.210 | 0.340  |
| 2. Constant $r$             | 0.258           | 0.265 | 0.271 | 0.244 | 0.418  |
| 3. Constant $w$             | 0.564           | 0.579 | 0.489 | 0.430 | 0.438  |
| 4. $\mu = 2$                | 0.258           | 0.271 | 0.242 | 0.250 | 0.360  |

In the counterfactual with no capital income risk, we re-estimate the model under the constraint that the rate of return is constant. The estimate of the rate of return we obtain in this case is 2.89 percent, just below its mean in the baseline. Though in our baseline estimate the implied savings rate is already too high (see Table 6), the differential savings factor compensates the lack of capital income risk to produce some skewness in the wealth distribution. As a consequence, this counterfactual estimate produces a much higher bequest motive (associated to an even more excessive savings rate): while  $\mu$  is essentially unchanged, the estimated relative preference for bequests  $A$  is doubled (though still imprecisely estimated). Nonetheless,

the estimate with  $r$  constant dramatically misses in matching the top 1 percent of the wealth distribution, which is reduced to less than half of the baseline (and the data). The wealth distribution implied by the model is less skewed, as the smaller fraction of wealth concentrated on the top is shifted to the whole rest of the distribution. In terms of social mobility, restricting the estimate to a constant  $r$  reduces also the fit on social mobility: notably, it increases mobility from the bottom 20 percent of the distribution while it reduces it from the rest of the distribution, particularly from the top.

In the counterfactual with no stochastic earnings, we feed the model an average earnings path. The resulting estimates of the preference parameters and of the rate of return process  $r$  reveal a minor strengthening of the savings factor through an increase in  $A$ , without any substantial change in  $\mu$ , and especially of capital income risk: both the mean and the auto-correlation of  $r$  are increased (the auto-correlation  $\rho(r)$  is more than doubled, though still imprecisely estimated), while the standard deviation is slightly smaller. Interestingly, in this case the estimate does not miss as much in matching the top 1 percent of the wealth distribution. This is an indication that stochastic earnings is not a first-order factor in filling the tail of the wealth distribution. On the other hand, the counterfactual with no stochastic earnings fits quite poorly the social mobility matrix, dramatically underfitting the mobility present in the data, at all quintiles. Stochastic earnings, therefore, play a fundamental role in facilitating the escape from low levels of wealth close to the borrowing constraint as well as from the top. But this counterfactual produces also too much wealth concentrated in the 60–90 percent range of the distribution, indicating that stochastic earnings play a particularly relevant role in transitioning wealth from this range to the top 1 percent.

In the counterfactual with homogeneous saving rates, we set  $\mu = 2$ , that is, we set the curvature parameter of the bequest utility equal to the curvature of consumption utility, so that agents with different wealth save at the same rate. In terms of the estimates, preferences for bequests are substantially increased and capital income is riskier (the variance of  $r$  increases). In this case, contrary to the previous counterfactual with no stochastic earnings, the model dramatically fails to match the top 1 percent of the wealth share, which is reduced to about 1/7 of the baseline (and the data). More generally, the simulated wealth distribution is much less skewed, even less skewed than the one produced by the constant  $r$  counterfactual: it produces too thin wealth shares in the 90–95, 95–99 percentiles as well. With respect to social mobility, it is noteworthy that restricting to homogeneous savings induces lower mobility out of all quintiles (but only slightly so from the top 20 percent), except from the bottom 20 percent, as is the case for the constant  $r$  counterfactual.

In summary, all the factors we study in our quantitative analysis, stochastic earnings, differential savings, and capital income risk, are well identified as crucial for generating the thick right tail of the wealth distribution and sufficient mobility. The factors seems to have a distinct role. Capital income risk and differential savings both contribute in a fundamental manner to generating the thick tail. Interestingly, both also at the same time increase social mobility (mostly from the top of the distribution for capital income risk) except from the bottom 20 percent. On the other hand, stochastic earnings have a limited role in filling the tail of the wealth distribution but are fundamental in inducing enough mobility in the wealth process, both by

limiting poverty traps at the bottom and favoring the churn at all quintiles, including at the top.<sup>33</sup>

## V. Transitional Dynamics of the Wealth Distribution

Our quantitative analysis so far is predicated on the assumption that the observed distribution of wealth is a stationary distribution, in the sense that our estimates are obtained by matching the data with the moments of the stationary distribution generated by the model. In this section we begin studying the implications of our model when we relax the stationarity assumption and try and match the transitional dynamics of the distribution of wealth.

The exercise we perform is as follows. Using the observed SCF 1962–1963 distribution of wealth as initial condition,<sup>34</sup> we estimate the parameters of the model by matching the implied distribution after 72 years (two iterations of the model) with the observed SCF 2007 distribution and the transition matrix adopted in the previous quantitative analysis; see Table 16.<sup>35</sup>

The fundamental feature of the change in the wealth distribution from 1962–1963 to 2007, in our data, is the substantial increase in inequality; see Table 17. The top 1 percent share, for instance, goes from 24.2 percent to 33.6 percent; the top 5 percent from 43.2 percent to 60.3 percent. In this respect, our new estimate shows that such a dramatic increase in wealth inequality can be obtained within the confines of our simple model, by exploiting the explanatory power of capital income risk and differential savings: see Gabaix et al. (2016) for related results. The new parameter estimates we obtain show in fact a larger bequest motive (a larger  $A$ , though compensated by a larger  $\mu$ ), with respect to their counterparts in the benchmark model, and a rate of return process with higher mean and volatility and much more auto-correlation. This induces a simulated distribution of wealth for 2007 which, with respect to the data, is even more skewed at the top. Strikingly, the bottom 40 percent of the distribution is very well matched, better than in our baseline. All in all, the match in this exercise is quite successful and the skewness of the simulated distribution more closely matches the data than even our baseline. This is obtained at the cost of not matching well the

<sup>33</sup>In apparent contrast with our results, several previous papers in the literature have obtained considerable success in matching the wealth distribution in the data with simulated models fundamentally driven by the stochastic earnings mechanism: see, e.g., Castañeda et al. (2003); Díaz, Pijoan-Mas, and Ríos-Rull (2003); Dávila et al. (2012); Kindermann and Krueger (2015); Kaymak and Poschke (2016). These simulated models, however, are driven by assumptions either about the skewness of earnings or about the working life of agents which appear counterfactual. For instance, Díaz, Pijoan-Mas, and Ríos-Rull (2003) postulate an “awesome state” in the earning process where roughly 6 percent of the top earners have 40 times the labor endowment of the median, at odds with the administrative data recently become available: e.g., in World Top Income Database 2013–2014 the average income of the top 5 percent is no more than 20 times the median income. On the other hand, Kaymak and Poschke’s (2016) calibration adds no awesome state but implies a working life span of over 100 years, at the stationary distribution, for 11 percent of the working population. See Benhabib, Bisin, and Luo (2017) and Benhabib and Bisin (2018) for detailed discussions of these issues, including the role of precautionary savings which play a relevant role in model in which the main driver of the wealth distribution is the stochastic earnings mechanism.

<sup>34</sup>More precisely, these data are from precursor surveys to the SCF: the 1962 Survey of Financial Characteristics of Consumers and the 1963 Survey of Changes in Family Finances. See <http://www.federalreserve.gov/econresdata/scf/scf6263.htm> for a discussion. Differences in methodology and quality notwithstanding, these data provide a useful benchmark as initial condition to the recent wealth dynamics.

<sup>35</sup>While the analysis does not require nor imposes any stationarity of the distribution of wealth over time, it does postulate that the model structure and parameter values stay constant after 1962. Importantly, we do not feed in the analysis the observed fiscal policy reforms since the 1960s. Doing so should improve the fit.

TABLE 16—PARAMETER ESTIMATES: TRANSITIONAL DYNAMICS

|                       | Preferences                |                                 |                               |                    |                    |
|-----------------------|----------------------------|---------------------------------|-------------------------------|--------------------|--------------------|
|                       | $\sigma$<br>[2]            | $\mu$<br>1.2377<br>(0.0297)     | $A$<br>0.0195<br>(0.0041)     | $\beta$<br>[0.97]  | $T$<br>[36]        |
|                       | Rate of return process     |                                 |                               |                    |                    |
| State space           | 0.0053<br>(0.0117)         | 0.0160<br>(0.0072)              | 0.0201<br>(0.0316)            | 0.0672<br>(0.0044) | 0.0872<br>(0.0004) |
| Transitional diagonal | 0.1094<br>(1.3759)         | 0.3689<br>(0.9192)              | 0.2966<br>(1.3058)            | 0.2260<br>(0.1453) | 0.0647<br>(0.7819) |
| Statistics            | $E(r)$<br>3.27%<br>(0.02%) | $\sigma(r)$<br>2.79%<br>(0.01%) | $\rho(r)$<br>0.210<br>(0.124) |                    |                    |

Note: Standard errors in parentheses; fixed parameters in brackets.

TABLE 17—MODEL FIT: TRANSITIONAL DYNAMICS

| Percentile                         | Wealth distribution |       |       |       |        |       |       |        |
|------------------------------------|---------------------|-------|-------|-------|--------|-------|-------|--------|
|                                    | 0–20                | 20–40 | 40–60 | 60–80 | 80–90  | 90–95 | 95–99 | 99–100 |
| Wealth share (data, SCF 1962–1963) | 0.009               | 0.043 | 0.094 | 0.173 | 0.142  | 0.115 | 0.190 | 0.242  |
| Wealth share (data, SCF 2007)      | –0.002              | 0.001 | 0.045 | 0.112 | 0.120  | 0.111 | 0.267 | 0.336  |
| Wealth share (model)               | 0.000               | 0.010 | 0.033 | 0.088 | 0.108  | 0.114 | 0.272 | 0.375  |
| Percentile                         | Social mobility     |       |       |       |        |       |       |        |
|                                    | 0–20                | 20–40 | 40–60 | 60–80 | 80–100 |       |       |        |
| Transition diagonal (data)         | 0.36                | 0.24  | 0.25  | 0.26  | 0.36   |       |       |        |
| Transition diagonal (model)        | 0.334               | 0.171 | 0.171 | 0.170 | 0.276  |       |       |        |

social mobility, by overestimating mobility, that is, the probability that children move away from their parents' wealth cell, all across the distribution.<sup>36</sup>

## VI. Conclusions

We estimate a parsimonious macroeconomic model of the distribution of wealth in the United States. While we assign special emphasis on the tail of the distribution, the model performs rather well in fitting the whole distribution of wealth in the data. Importantly, the model is also successful in fitting the social mobility of wealth in the data. Parameter estimates, especially the rate of return of wealth process, compare very closely to independent observations.

Our analysis allows us to distinguish the contributions of three critical factors driving wealth accumulation: a skewed and persistent distribution of earnings, differential saving and bequest rates across wealth levels, and capital income risk in entrepreneurial activities. All of these three factors are necessary and empirically

<sup>36</sup>See online Appendix C.3 for the complete estimated social mobility matrix.

relevant in matching both distribution and mobility, with a distinct role for each, which we identify.

Finally, we begin studying the implications of the model for the transitional dynamics of the distribution of wealth. The estimates are qualitatively similar to those in the baseline, and our model delivers fast transitional dynamics. While more work is obviously necessary in this respect, our results are quite encouraging.

## REFERENCES

- Altonji, Joseph G., and Lewis M. Segal.** 1996. "Small-Sample Bias in GMM Estimation of Covariance Structures." *Journal of Business and Economic Statistics* 14 (3): 353–66.
- Ameriks, John, Joseph Briggs, Andrew Caplin, Mi Luo, Matthew D. Shapiro, and Christopher Tonetti.** 2015b. "Measuring and Modeling Inter-generational Wealth Transfers: The Precautionary Transfer Motives." Unpublished.
- Ameriks, John, Joseph Briggs, Andrew Caplin, Matthew D. Shapiro, and Christopher Tonetti.** 2015a. "Long-Term-Care Utility and Late-in-Life Saving." Unpublished.
- Bach, Laurent, Laurent E. Calvet, and Paolo Sodini.** 2017. "Rich Pickings? Risk, Return, and Skill in the Portfolios of the Wealthy." Unpublished.
- Benhabib, Jess, and Alberto Bisin.** 2018. "Skewed Wealth Distributions: Theory and Empirics." *Journal of Economic Literature* 56 (4): 1261–91.
- Benhabib, Jess, Alberto Bisin, and Mi Luo.** 2017. "Earnings Inequality and Other Determinants of Wealth Inequality." *American Economic Review* 107 (5): 593–97.
- Benhabib, Jess, Alberto Bisin, and Mi Luo.** 2019. "Wealth Distribution and Social Mobility in the US: A Quantitative Approach: Dataset." *American Economic Review*. <https://doi.org/10.1257/aer.20151684>.
- Benhabib, Jess, Alberto Bisin, and Shenghao Zhu.** 2011. "The Distribution of Wealth and Fiscal Policy in Economies with Finitely Lived Agents." *Econometrica* 79 (1): 123–57.
- Biancotti, Claudia, Giovanni D'Alessio, and Andrea Neri.** 2008. "Measurement Error in the Bank of Italy's Survey of Household Income and Wealth." *Review of Income and Wealth* 54 (3): 466–93.
- Cagetti, Marco, and Mariacristina De Nardi.** 2006. "Entrepreneurship, Frictions, and Wealth." *Journal of Political Economy* 114 (5): 835–70.
- Calvet, Laurent E., and Paolo Sodini.** 2014. "Twin Picks: Disentangling the Determinants of Risk-Taking in Household Portfolios." *Journal of Finance* 69 (2): 867–906.
- Campbell, John Y., and Martin Lettau.** 1999. "Dispersion and Volatility in Stock Returns: An Empirical Investigation." NBER Working Paper 7144.
- Campbell, John Y., Martin Lettau, Burton G. Malkiel, and Yexiao Xu.** 2001. "Have Individual Stocks Become More Volatile? An Empirical Exploration of Idiosyncratic Risk." *Journal of Finance* 56 (1): 1–43.
- Case, Karl E., and Robert J. Shiller.** 1989. "The Efficiency of the Market for Single-Family Homes." *American Economic Review* 79 (1): 125–37.
- Castaneda, A., J. Diaz-Gimenez, and J. V. Rios-Rull.** 2003. "Accounting for the U.S Earnings and Wealth Inequality." *Journal of Political Economy* 111 (4): 818–57.
- Charles, Kerwin Kofi, and Erik Hurst.** 2003. "The Correlation of Wealth across Generations." *Journal of Political Economy* 111 (6): 1155–82.
- Chetty, Raj, Nathaniel Hendren, Patrick Kline, and Emmanuel Saez.** 2014. "Where Is the Land of Opportunity? The Geography of Intergenerational Mobility in the United States." *Quarterly Journal of Economics* 129 (4): 1553–623.
- Cox, Donald.** 1990. "Intergenerational Transfers and Liquidity Constraints." *Quarterly Journal of Economics* 105 (1): 187–217.
- Cunha, Flávio, James J. Heckman, and Susanne M. Schennach.** 2010. "Estimating the Technology of Cognitive and Noncognitive Skill Formation." *Econometrica* 78 (3): 883–931.
- Dávila, Julio, Jay H. Hong, Per Krusell, and José-Victor Ríos-Rull.** 2012. "Constrained Efficiency in the Neoclassical Growth Model with Uninsurable Idiosyncratic Shocks." *Econometrica* 80 (6): 2431–67.
- De Nardi, Mariacristina.** 2004. "Wealth Inequality and Intergenerational Links." *Review of Economic Studies* 71 (3): 743–68.
- De Nardi, Mariacristina, Giulio Fella, and Gonzalo Paz-Pardo.** 2017. "The Implications of Richer Earnings Dynamics for Consumption and Wealth." NBER Working Paper 21917.

- De Nardi, Mariacristina, Eric French, and John B. Jones.** 2010. "Why Do the Elderly Save? The Role of Medical Expenses." *Journal of Political Economy* 118 (1): 39–75.
- De Saporta, Benoîte.** 2005. "Tail of the Stationary Solution of the Stochastic Equation  $Y_{n+1} = a_n Y_n + b_n$  with Markovian Coefficients." *Stochastic Processes and Application* 115 (12): 1954–78.
- Díaz, Antonia, Josep Pijoan-Mas, and José-Victor Ríos-Rull.** 2003. "Precautionary Savings and Wealth Distribution under Habit Formation Preferences." *Journal of Monetary Economics* 50 (6): 1257–91.
- Díaz-Giménez, Javier, Andy Glover, and José-Victor Ríos-Rull.** 2011. "Facts on the Distributions of Earnings, Income, and Wealth in the United States: 2007 Update." *Federal Reserve Bank of Minneapolis Quarterly Review* 34 (1): 2–31.
- Fagereng, Andreas, Luigi Guiso, Davide Malacrino, and Luigi Pistaferri.** 2016. "Heterogeneity in Returns to Wealth and the Measurement of Wealth Inequality." *American Economic Review* 106 (5): 651–55.
- Fagereng, Andreas, Luigi Guiso, Davide Malacrino, and Luigi Pistaferri.** 2017. "Heterogeneity and Persistence in Returns to Wealth." Unpublished.
- Flavin, Marjorie, and Takashi Yamashita.** 2002. "Owner-Occupied Housing and the Composition of the Household Portfolio." *American Economic Review* 92 (1): 345–62.
- Gabaix, Xavier, Jean-Michel Lasry, Pierre-Louis Lions, and Benjamin Moll.** 2016. "The Dynamics of Inequality." *Econometrica* 84 (6): 2071–111.
- Gale, William G., and John Karl Scholz.** 1994. "Intergenerational Transfers and the Accumulation of Wealth." *Journal of Economic Perspectives* 8 (4): 145–60.
- Grey, D. R.** 1994. "Regular Variation in the Tail Behaviour of Solutions of Random Difference Equations." *Annals of Applied Probability* 4 (1): 169–83.
- Guvenen, Fatih.** 2016. *Quantitative Economics with Heterogeneity: An A-to-Z Guidebook*. Princeton, NJ: Princeton University Press.
- Guvenen, Fatih, Fatih Karahan, Serdar Ozkan, and Jae Song.** 2016. "What Do Data on Millions of US Workers Reveal about Life-Cycle Earnings Dynamics?" Unpublished.
- Hay, Diana, Reza Rastegar, and Alexander Roitershtein.** 2011. "Multivariate Linear Recursions with Markov-Dependent Coefficients." *Journal of Multivariate Analysis* 102 (3): 521–27.
- Heathcote, Jonathan, Fabrizio Perri, and Giovanni L. Violante.** 2010. "Unequal We Stand: An Empirical Analysis of Economic Inequality in the United States, 1967–2006." *Review of Economic Dynamics* 13 (1): 15–51.
- Hendricks, Lutz.** 2002. "Bequests and Retirement Wealth in the United States." Unpublished.
- Hubmer, Joachim, Per Krusell, and Anthony A. Smith.** 2017. "The Historical Evolution of the Wealth Distribution: A Quantitative-Theoretic Investigation." Unpublished.
- Huggett, Mark, Gustavo Ventura, and Amir Yaron.** 2011. "Sources of Lifetime Inequality." *American Economic Review* 101 (7): 2923–54.
- Hurd, Michael, and James P. Smith.** 2003. "Expected Bequests and Their Distribution." RAND Corporation Publications Department Working Paper 03-10.
- Japelli, Tullio, and Luigi Pistaferri.** 2006. "Intertemporal Choice and Consumption Mobility." *Journal of the European Economic Association* 4 (1): 75–115.
- Kacperczyk, Marcin, Jaromir Nosal, and Luminita Stevens.** 2015. "Investor Sophistication and Capital Income Inequality." Unpublished.
- Kaplan, Greg, Benjamin Moll, and Giovanni L. Violante.** 2016. "Monetary Policy According to HANK." Unpublished.
- Kaymak, Barış, and Markus Poschke.** 2016. "The Evolution of Wealth Inequality over Half a Century: The Role of Taxes, Transfers and Technology." *Journal of Monetary Economics* 77: 1–25.
- Keane, Michael P., and Kenneth I. Wolpin.** 1997. "The Career Decisions of Young Men." *Journal of Political Economy* 105 (3): 473–522.
- Kennickell, Arthur B., and Martha Starr-McCluer.** 1997. "Household Saving and Portfolio Change: Evidence from the 1983–89 SCF Panel." *Review of Income and Wealth* 43 (4): 381–99.
- Kindermann, Fabian, and Dirk Krueger.** 2015. "High Marginal Tax Rates on the Top 1%? Lessons from a Life Cycle Model with Idiosyncratic Income Risk." Unpublished.
- Krusell, Per, and Anthony A. Smith, Jr.** 1998. "Income and Wealth Heterogeneity in the Macroeconomy." *Journal of Political Economy* 106 (5): 867–96.
- Luo, Mi.** 2017. "Unintended Effects of Estate Taxation on Wealth Inequality." Unpublished.
- Miranda, Mario J., and Paul L. Fackler.** 2004. *Applied Computational Economics and Finance*. Cambridge, MA: MIT Press.
- Moskowitz, Tobias J., and Annette Vissing-Jørgensen.** 2002. "The Returns to Entrepreneurial Investment: A Private Equity Premium Puzzle?" *American Economic Review* 92 (4): 745–78.
- Piketty, Thomas.** 2014. *Capital in the Twenty-First Century*. Cambridge, MA: Harvard University Press.



- Poterba, James, Steven Venti, and David Wise.** 2011. "The Composition and Drawdown of Wealth in Retirement." *Journal of Economic Perspectives* 25 (4): 95–118.
- Quadrini, Vincenzo.** 2000. "Entrepreneurship, Saving, and Social Mobility." *Review of Economic Dynamics* 3 (1): 1–40.
- Saez, Emmanuel, and Gabriel Zucman.** 2016. "Wealth Inequality in the United States since 1913: Evidence from Capitalized Income Tax Data." *Quarterly Journal of Economics* 131 (2): 519–78.

**This article has been cited by:**

1. Diego Daruich, Julian Kozlowski. 2019. Explaining intergenerational mobility: The role of fertility and family transfers. *Review of Economic Dynamics* . [[Crossref](#)]
2. Thomas Fischer. 2019. Determinants of Wealth Inequality and Mobility in General Equilibrium. *SSRN Electronic Journal* . [[Crossref](#)]