# <span id="page-0-0"></span>Behavioral Epidemiology Models

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# Epidemics - by Country

### Italy and Spain's daily death tolls are plateauing, but in the UK and US every day brings more new deaths than the last

Daily coronavirus deaths (7-day rolling ayg.), by number of days since 3 daily deaths first recorded



### FT graphic: John Burn-Murdoch / @iburnmurdoch

Source: FT analysis of European Centre for Disease Prevention and Control: Worldometers: FT research, Data updated April 04, 19:00 GMT **OFT** 

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### $\triangleright$  But this is a different issue.

- I How can we compare different countries? Indeed, several possible determinants of the dynamics vary:
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	- $\triangleright$  demographic characteristics, e.g., age structure, health conditions ...
	- $\triangleright$  socio-economic characteristics, e.g., income, public health conditions, dominant living arrangements, social contacts, ...
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	- $\triangleright$  We concentrate on models in this lecture.

Nothing is less real than realism. Details are confusing. It is only by selection, by elimination, by emphasis that we get to the real meaning of things (Georgia O'Keeffe).

- Models are theoretical exercises of abstraction: *ignoring many details in order to* focus on the most important elements of the problem.
- $\blacktriangleright$  There is no such thing as the right degree of abstraction for all analytic purposes. The proper degree of abstraction depends on the objective of the analysis.
	- $\triangleright$  A model that is a gross oversimplification for one purpose may be needlessly complicated for another.
	- $\triangleright$  A map might be an appropriate metaphor for a model: we rarely need 1:1 maps; and sometimes we need a map of the whole American continent, sometimes one of the upper east side of NYC.

I Models are not necessarily mathematical models. The following example (taken from Krugman, Development, Geography, and Economic Theory, 1995, MIT Press; Ch. 3) illustrates this point:

Dave Fultz at the University of Chicago in the late 40's showed that a dishpan filled with water, on a slowly rotating turntable, with an electric heating device bent around the outside of the pan provides a good representation of the basic pattern of weather. The dishpan was build to model the temperature differential between the poles and the equator and the force generated by the earth's spin (abstracting from most of the the intricacies and complexities of the earth geography) and was successfully shown to exhibit phenomena which could be interpreted as tropical trade winds, cyclonic storms of the temperate regions, and the jet stream.

I But often models are in fact mathematical models: the most sophisticated weather forecasts nowadays require the estimation of the parameters of a large number (very large, hundreds) of equations.

Models in both in Epidemiology and Economics are mathematical models.

**But** 

Models in in Epidemiology are more like those employed in sophisticated weather forecasts: lots of equations, very detailed data:

built for prediction accuracy.

Models in Economics are more like Fulz model, abstract, stylized, representation of the interaction of a priori important factors,

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- Last, but not least,
	- $\triangleright$  Models in Economics include (explicitly, formally) behavioral factors (rational ) choice of agents.
- I We shall introduce the (stylized, abstract) core component of epidemiological models - the SIR model
- $\triangleright$  We shall introduce a spatial extension of SIR for concreteness
- We shall introduce rational choice/behavior into these models i.e., some economics
- All the way simulating the dynamics of an epidemic to illustrate the models and their different implications
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	- $\triangleright$  I am an economist after all :)

Stylized model (Kermack and McKendrick 1927) - without bells and whistles for prediction accuracy:



 $\mathcal{R}_0 = \beta/\gamma$ : number of agents a single infected agent infects, on average, at  $I_0 = R_0 = 0$ .

 $\beta = \pi c$ : infection rate per-contact times random matching contacts per unit of time.



# Epidemiological models: Spatial-SIR

N people located randomly in a 1-sized square

## I 5 states:

- **S**:  $\Theta$  Susceptibles (can become infected)
- $\mathsf{A}: \bigodot$  Asymptomatics (infected, but unaware)
- **Y**:  $\odot$  sYmptomatics (infected, aware)
- **D**: Dead
- **R**:  $\odot$  Recovered
- **Transitions between states**
- Contagion occurs if: within contagion circle + random draw



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## How the infection evolves in space

## People move in random direction at given speed





Days

## SIR and Spatial-SIR: Simulations of the calibrated model



Take the calibrated Spatial-SIR, and change one factor at a time

number of clusters,  $I_0$ [, and their spatial distribution](#page-0-0) [size,](#page-25-0) N  $\blacktriangleright$ [density,](#page-28-0)  $\frac{\text{area}}{N}$  $\blacktriangleright$ [speed of movement,](#page-0-0)  $\mu$ 

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- Dynamics is invariant to the initial condition:
	- $\triangleright$  Scaling in size obtains if we scale initial conditions,
	- $\triangleright$  but only if the initial conditions are appropriately homogeneously spaced.



- <span id="page-28-0"></span> $\blacktriangleright$  City density has distinct role from the inverse of the probability of infection:
	- $\triangleright$  Lower density flattens the curve of infected

### Figure: The effect of varying city density with constant population



- The peak of Infected  $\frac{1}{N}$  is very sensitive to density:
	- $\triangleright$  halving density flattens dramatically the peak (more than a half, after more than twice as many days).

### Figure: The effect of varying city density with constant population



# Behavioral Spatial-SIR

- Growth rate of cases is  $\beta = \pi c$ : infection rate times contacts. Rational agents
	- $\triangleright$  will choose to limit their social interactions, their contacts  $c$  the more so, the higher the risk of being infected:

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c = \alpha(\frac{I_t}{N})c_0
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 $\triangleright$  E.g.,

$$
\alpha(\frac{l_t}{N}) = \begin{cases} 1 & \text{if } \frac{l_t}{N} \leq \underline{l} \\ \left(\frac{l}{\frac{l_t}{N}}\right)^{1-\phi} & \text{if } \frac{l_t}{N} > \underline{l} \end{cases}.
$$

Figure: Reduction in contacts according to a very cautious behavioral response



- $\blacktriangleright$  Behavioral response in Spatial-SIR
	- $\triangleright$  Peak of active cases is halved,
	- $\triangleright$  Total cases reduced by 10%.



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- I Epidemiological model built for prediction but without rational choice/behavior delivered hardly meaningful worst-case scenarios

#### 16 March 2020

Imperial College COVID-19 Response Team

#### Report 9: Impact of non-pharmaceutical interventions (NPIs) to reduce COVID-19 mortality and healthcare demand

Neil M Ferguson, Daniel Lavdon, Gemma Nediati-Gilani, Natsuko Imai, Kylie Ainslie, Marc Baguelin, Sangeeta Bhatia, Adhiratha Boonyasiri, Zulma Cucunubá, Gina Cuomo-Dannenburg, Amy Dighe, Ilaria Dorigatti, Han Fu, Katy Gaythorpe, Will Green, Arran Hamlet, Wes Hinsley, Lucy C Okell, Sabine van Elsland, Hayley Thompson, Robert Verity, Erik Volz, Haowei Wang, Yuanrong Wang, Patrick GT Walker, Caroline Walters, Peter Winskill, Charles Whittaker, Christl A Donnelly, Steven Riley, Azra C Ghani.

On behalf of the Imperial College COVID-19 Response Team

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In the (unlikely) absence of any control measures or spontaneous changes in individual behavior, we would expect a peak in mortality (daily deaths) to occur after approximately 3 months. In such scenarios, given an estimated R0 of 2.4, we predict 81% of the G.B. and U.S. populations would be infected over the course of the epidemic... In total, in an unmitigated epidemic, we would predict approximately (510,000 deaths in G.B. and 2.2 million in the U.S., not accounting for the potential negative effects of health systems being overwhelmed on mortality.

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- B "the (unlikely) absence of any control measures or spontaneous changes in individual behavior"
- $\triangleright$  is a zero-probability scenario for economists whose core job modeling "spontaneous changes in individual behavior."

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	- $\triangleright$  Another lecture :)

## Peak into simulating a lockdown



Figure 8: Counterfactual: Reopen when stably declining

 $\blacktriangleright$  Economists playing Epidemiologists

## **Conclusions**

Economists playing Epidemiologists



 $\blacktriangleright$